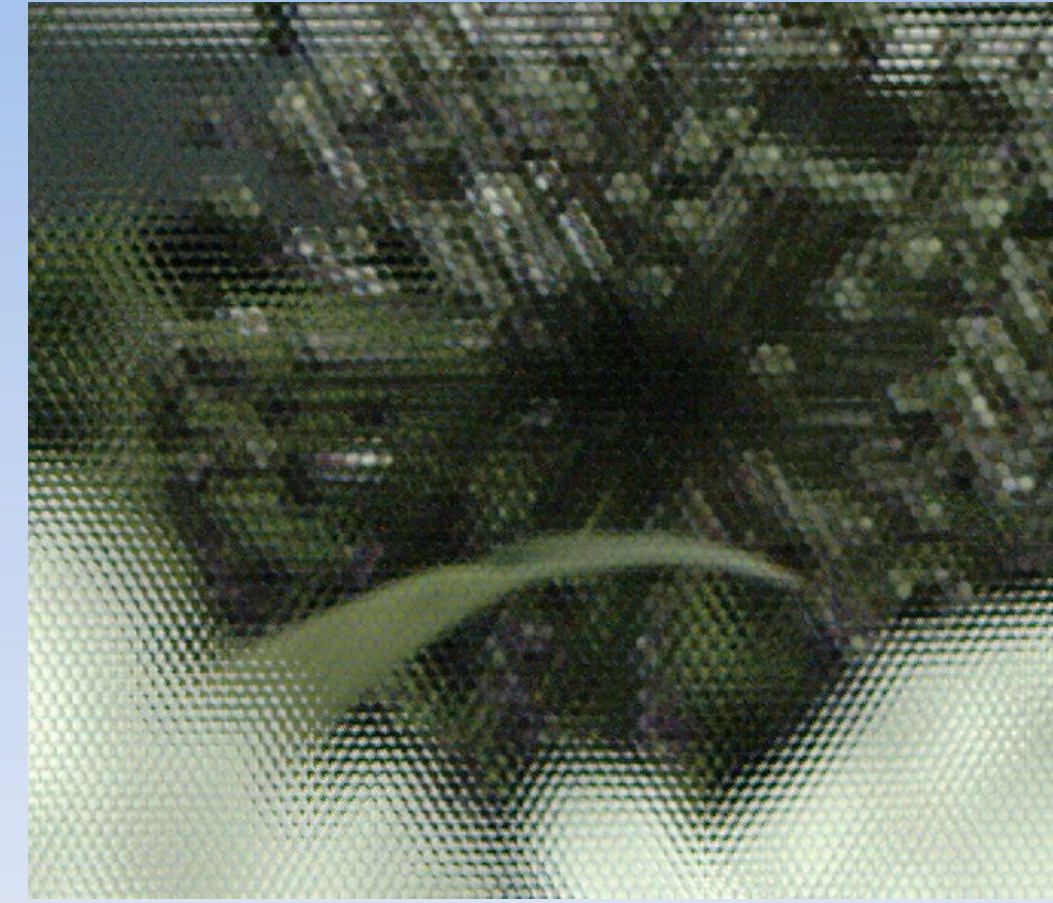
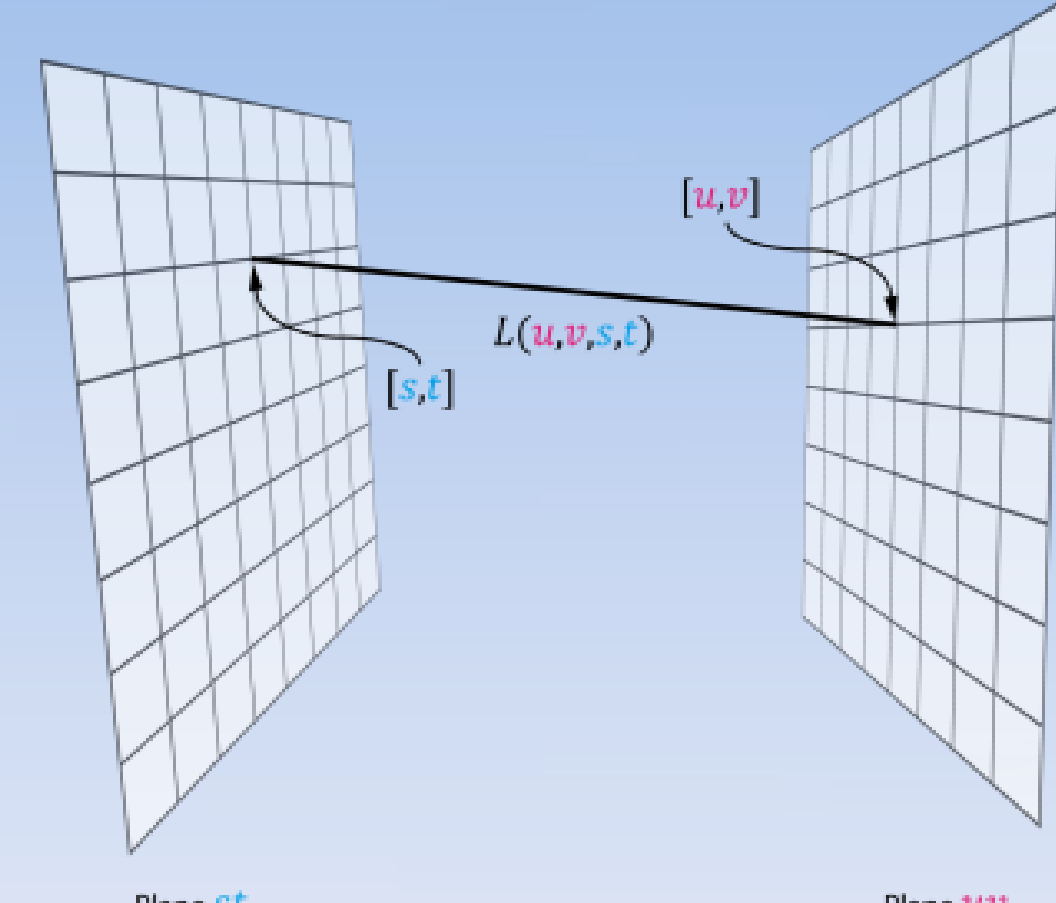


## 4D Light Field

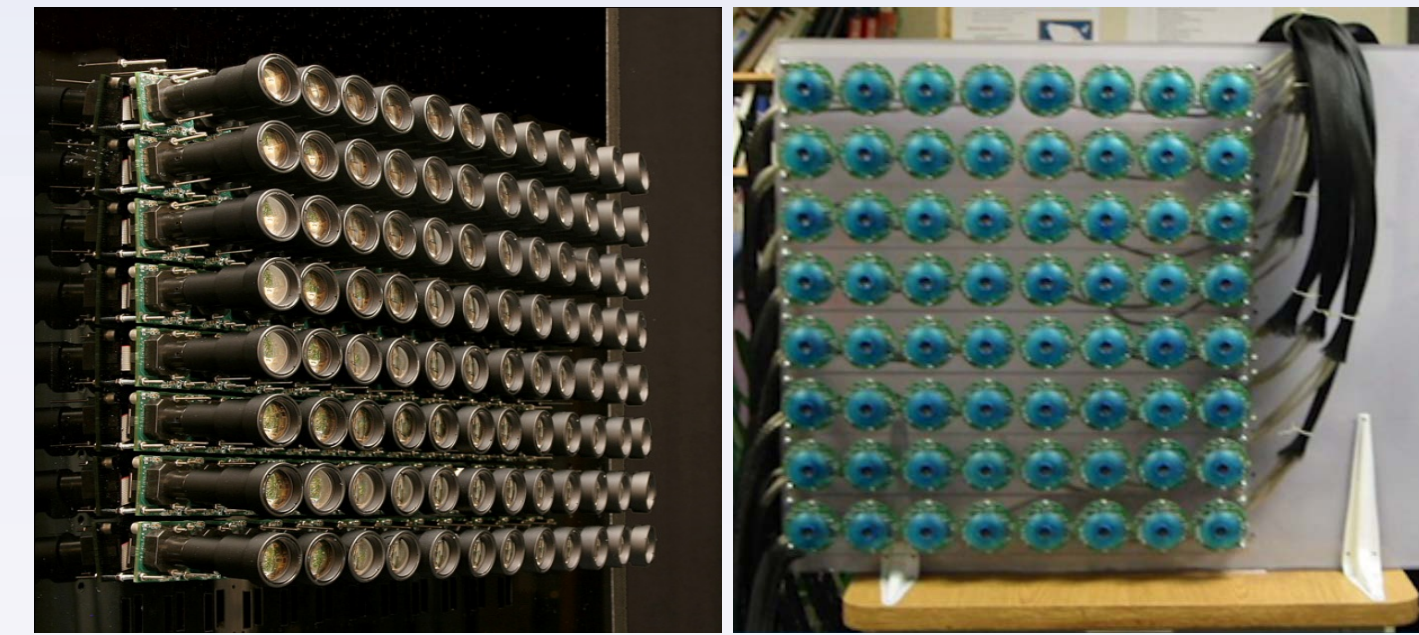


Light Field Image



Light Field Parameterization (2PP)

## Light Field Acquisition Devices



Camera Arrays



Lytro, Raytrix, Pelican Cameras

## Ray Geometric Structure in a Light Field

➤ Ray  $[s, t, u, v]$  Passing Through a 3D Point  $[x, y, z]$ :

$$\lambda[s, t, 1] + (1 - \lambda)[u, v, 0] = [x, y, z] \Rightarrow \begin{cases} zs + (1 - z)u = x \\ zt + (1 - z)v = y \end{cases}$$

➤ Ray  $[s, t, u, v]$  Passing Through a 3D Line  $[x, y, z] + [d_x, d_y, 0]$ :

$$(d_y - d_z)s + (d_x z - d_x) + d_y z u - d_x z v + d_x y - d_y x = 0$$

➤ Largely Linear  $\rightarrow$  Can Be Triangulated

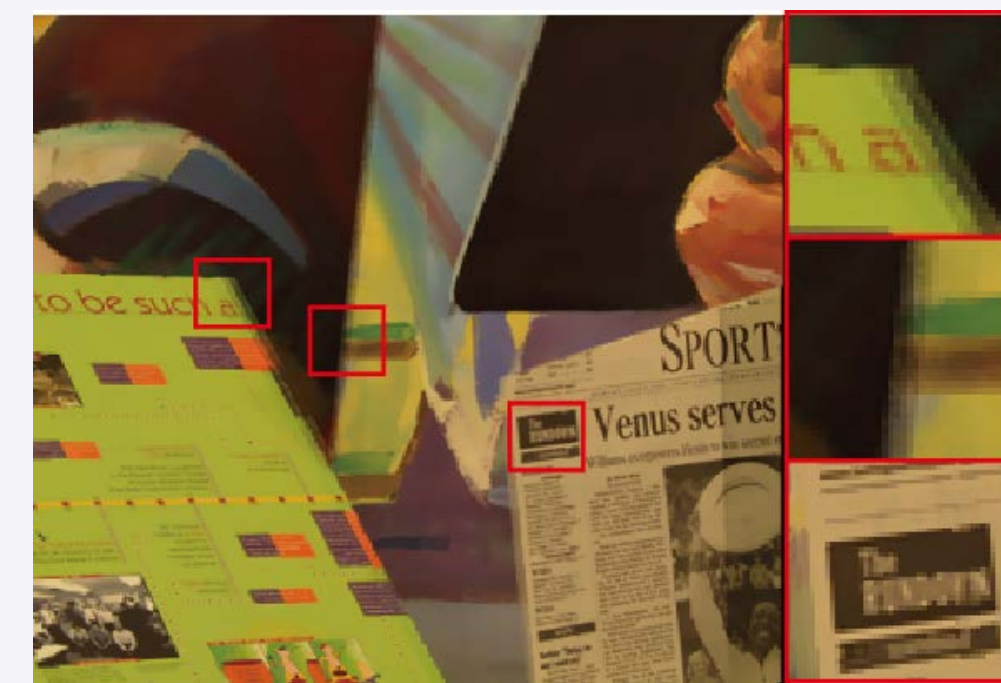
## Light Field Super-resolution via Triangulation

➤ Triangulation:

- Use scattered sample rays
- A natural interpolant for filling in the missing data
- Brute-force Delaunay Triangulation (strong aliasing)

➤ Edge Constrained Delaunay Triangulation

- Aliasing Near Edges

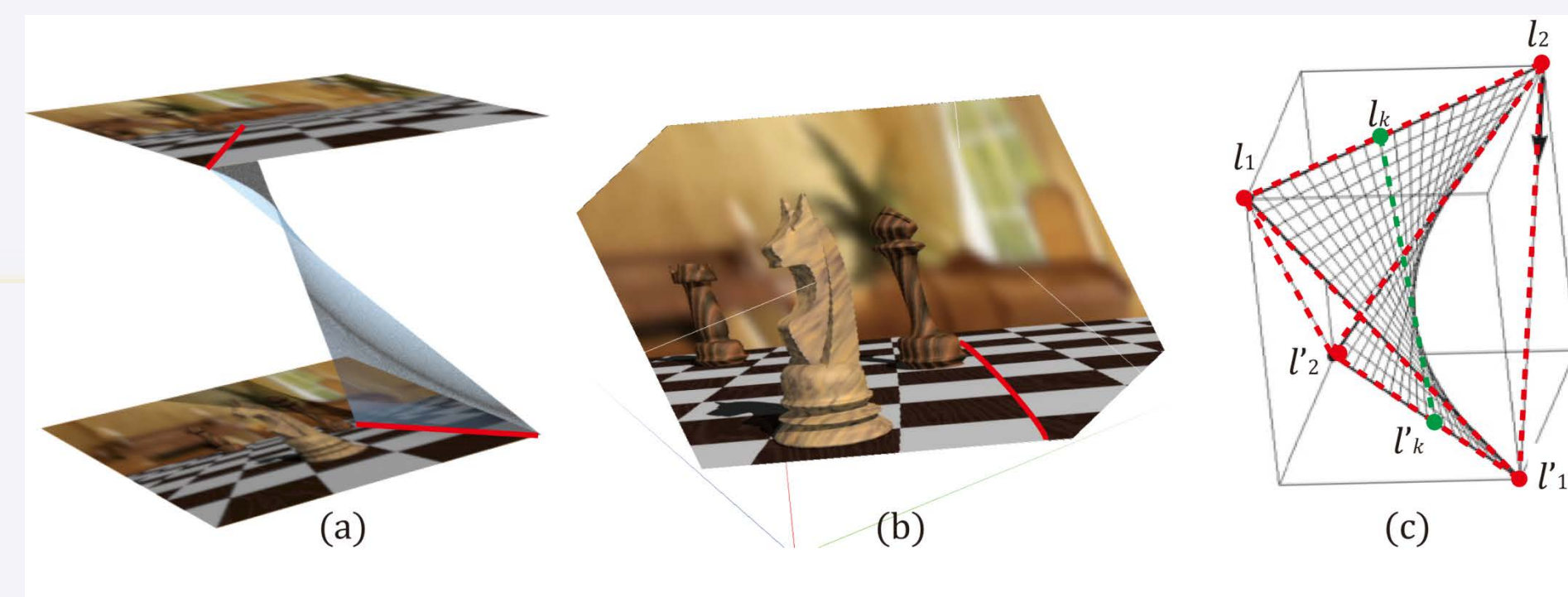


## Causes: Bilinear Ray Structure of 3D Lines

➤ Lines  $[s_0, t_0, u_0, v_0]$  not parallel to the 2PP satisfy the bilinear constraint:

$$\begin{cases} \lambda_1 s + (1 - \lambda_1)u = \lambda_2 s_0 + (1 - \lambda_2)u_0 \\ \lambda_1 t + (1 - \lambda_1)v = \lambda_2 t_0 + (1 - \lambda_2)v_0 \end{cases}$$

$$\Rightarrow \frac{s - s_0}{u - u_0} = \frac{t - t_0}{v - v_0}$$

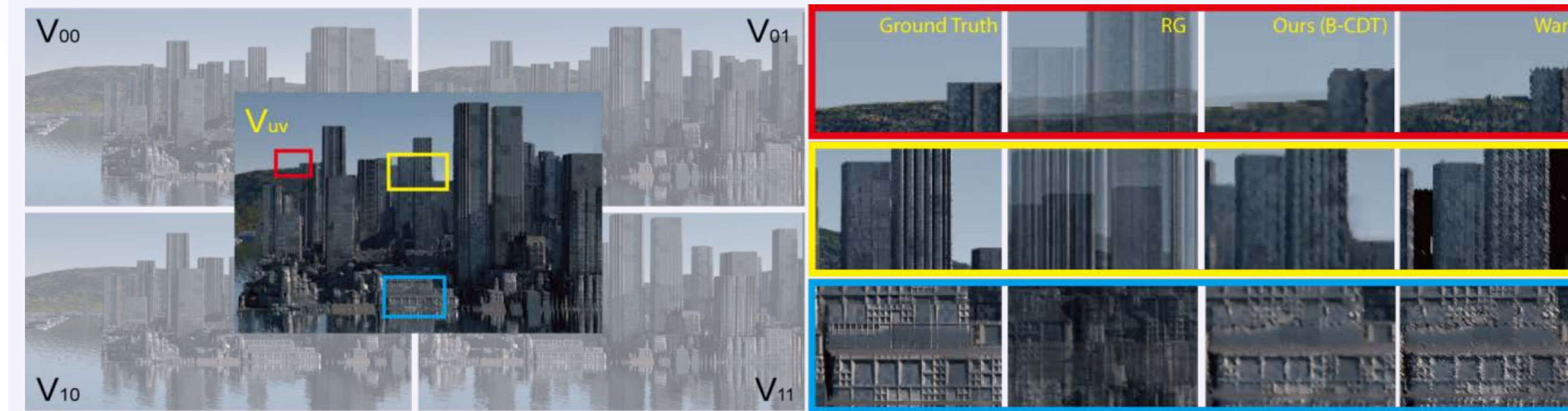
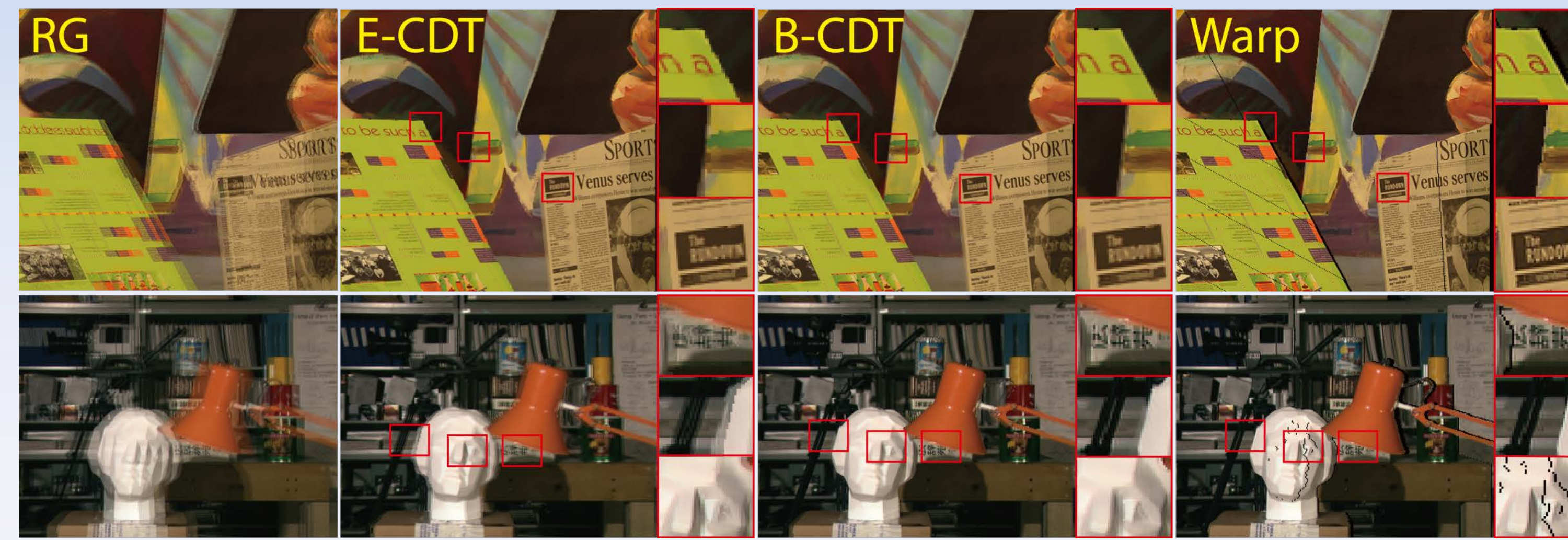


➤ Tetrahedralizing a bilinear surface introduces volume, i.e., bleeding

## Bilinear Constrained Delaunay Triangulation (B-CDT)

- Detect 3D lines in the LF
- Subdivide the corresponding bilinear surfaces into slim patches
- Triangulate each patch
- Add patch edges as additional constraints in CDT

## Light Field Triangulation Results



## How to Obtain Depth at Feature Points?

- Our Approach: Stereo Matching with 3D Line Constraints
- Traditional Multi-View Graph Cut (MVGC) Minimizes:

$$E = E_{data}(p, q) + E_{smooth}(p, q) + E_{occ}(p, q)$$

## Linearity of Disparity along a Line

➤ Proof linearity of disparity along a line segment by bilinear constraints in the ray space:

$$\frac{s + \Delta s - s_0}{u + \Delta u - u_0} = \frac{s - s_0}{u - u_0} = \frac{t - t_0}{v - v_0} \Rightarrow d = \frac{\Delta s}{\Delta u} = \frac{t - t_0}{v - v_0}$$

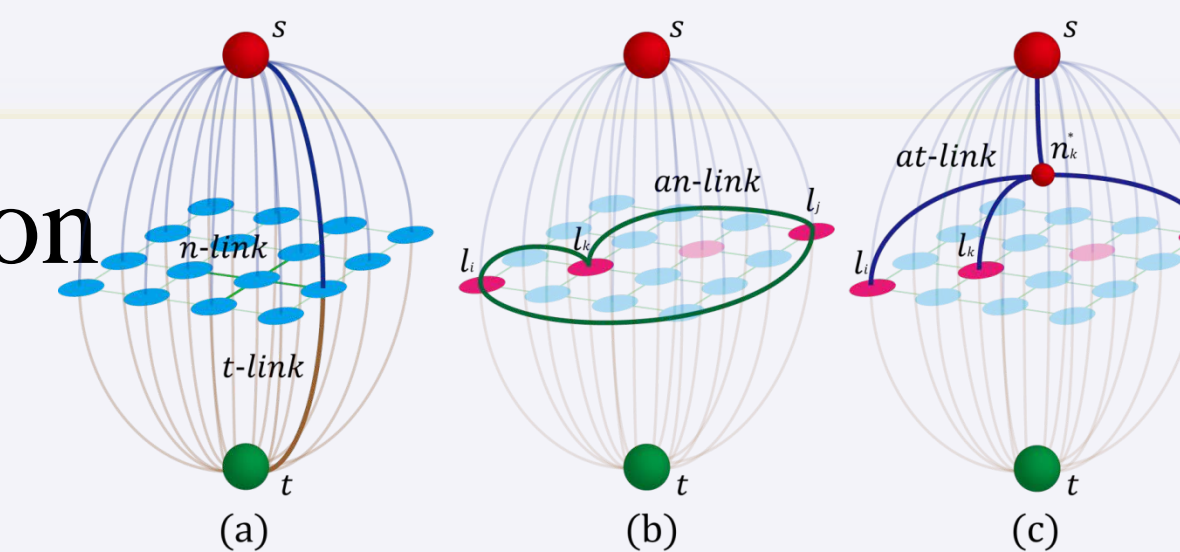
## Line Assisted Graph Cut (LAGC)

➤ Energy term for lines:

$$E_{line}(x, y, z) = \sum_{y \in [x, z]} \|\lambda L(x) - L(y) + (1 - \lambda)L(z)\|$$

➤ Non-submodular

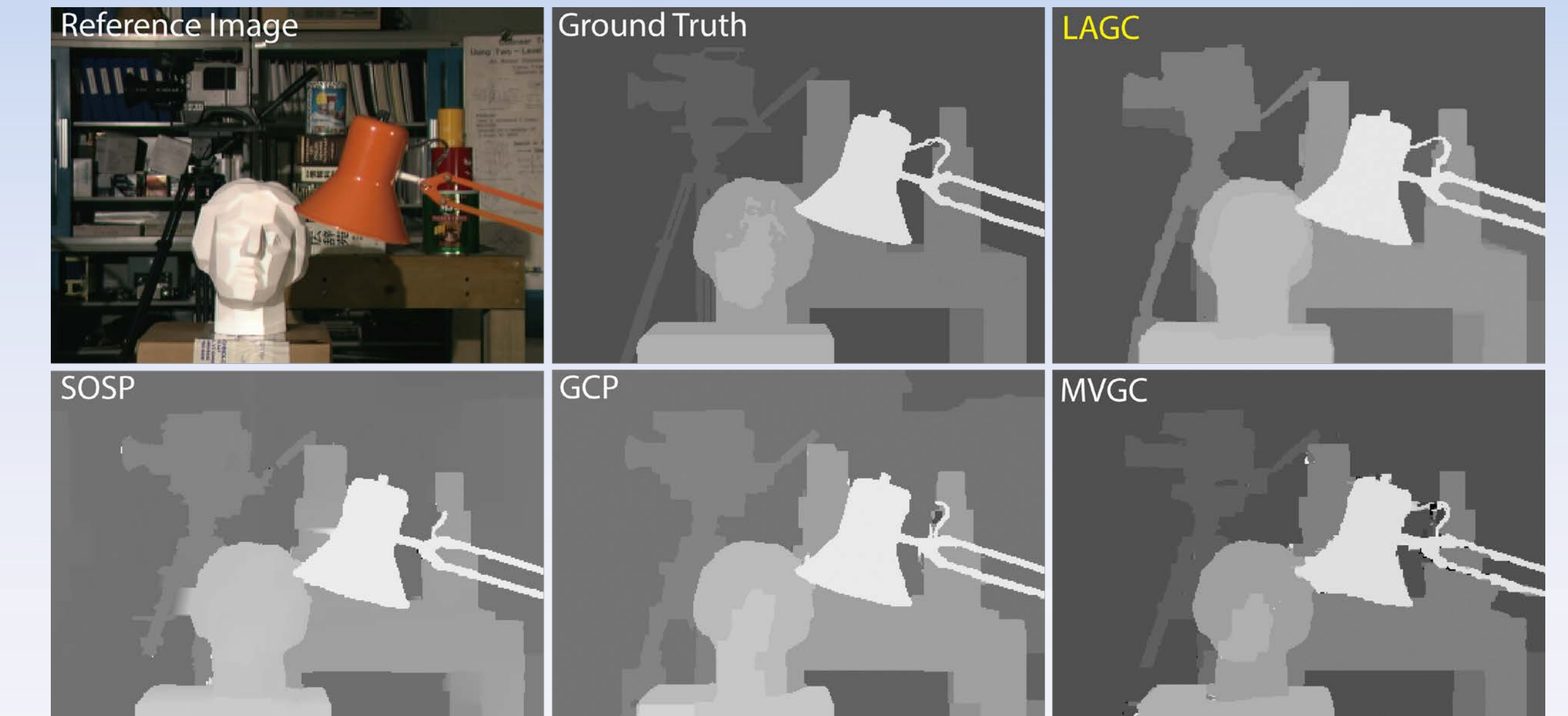
➤ Solution: Use QPBO instead of  $\alpha$ -expansion



## Experimental Results

➤ Tsukuba Dataset:

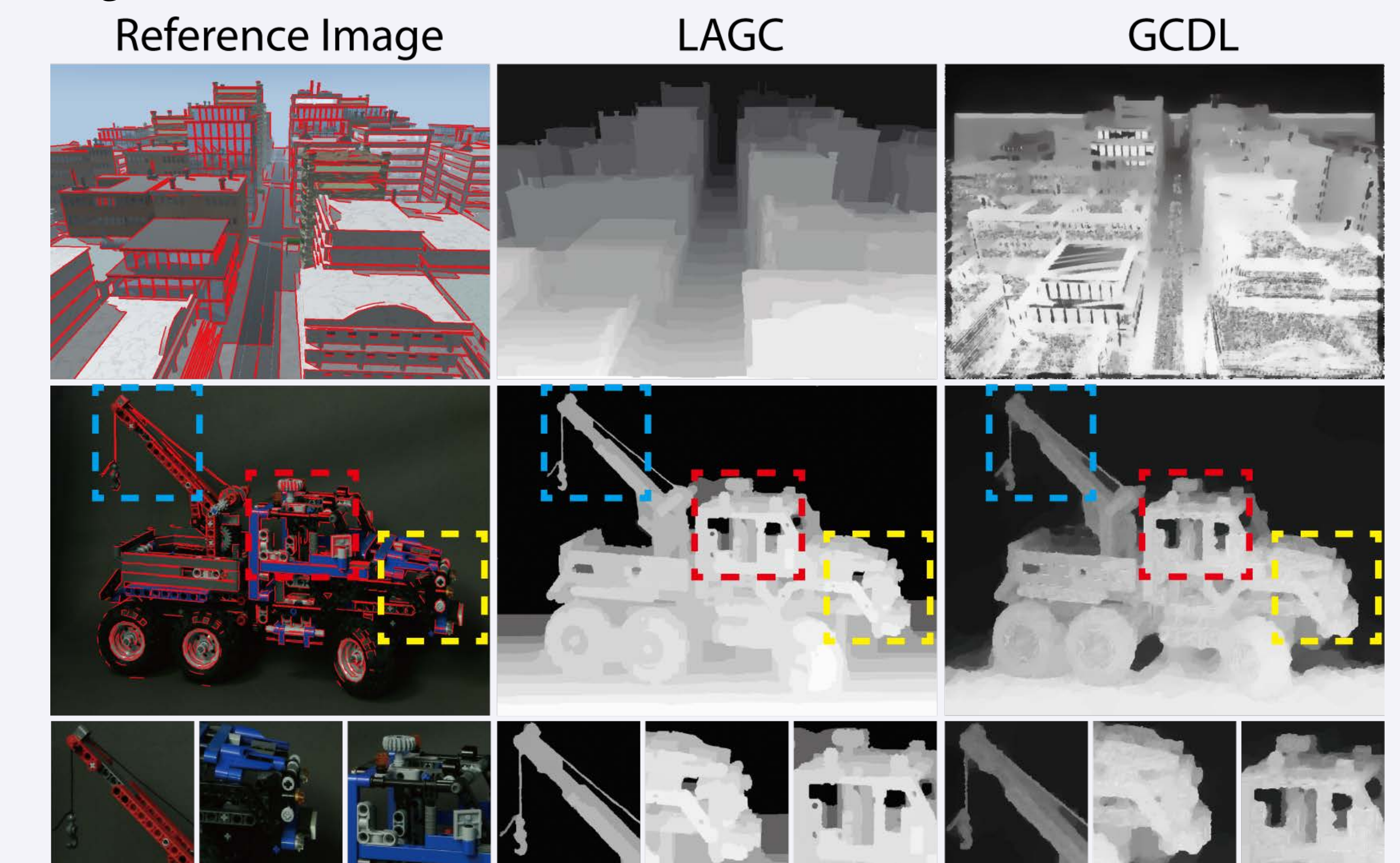
- SOSP: Second Order Smoothness Prior [Woodford et al. 08]
- GCP: Ground Control Points (Middlebury Rank 1) [Shi et al. 12]
- GCDL: Global Consistent Depth Labeling [Wanner and Goldlücke 12]



Algorithm	non-occlusion	all	discontinuity
LAGC	1.00 <sub>13</sub>	1.41 <sub>14</sub>	5.39 <sub>14</sub>
MVGC	1.27 <sub>35</sub>	1.99 <sub>50</sub>	6.48 <sub>38</sub>
SOSP	2.91 <sub>103</sub>	3.56 <sub>92</sub>	7.33 <sub>57</sub>
GCP	1.03 <sub>14</sub>	1.29 <sub>5</sub>	5.60 <sub>16</sub>

Table 1. Stereo matching using LAGC (ours), MVGC, SOSP, and GCP on Tsukuba. We show both the percentage of bad pixels and the algorithm's ranking (in subscripts)

➤ Real Light Field Dataset:



## Acknowledgments

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