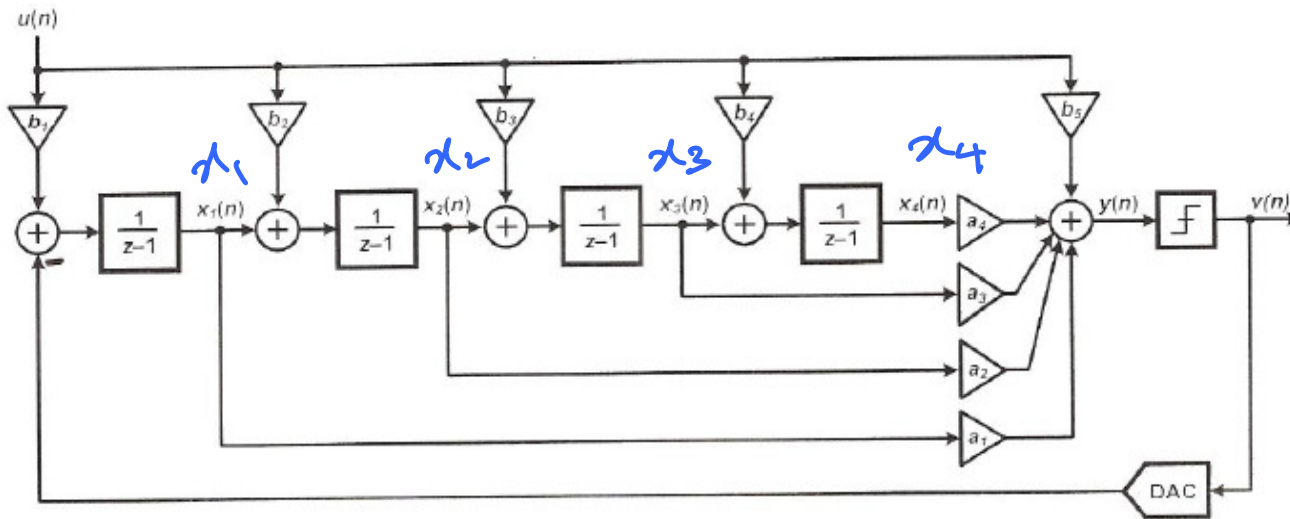
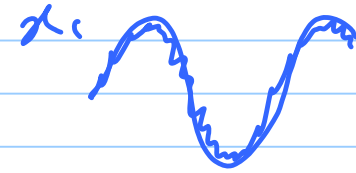
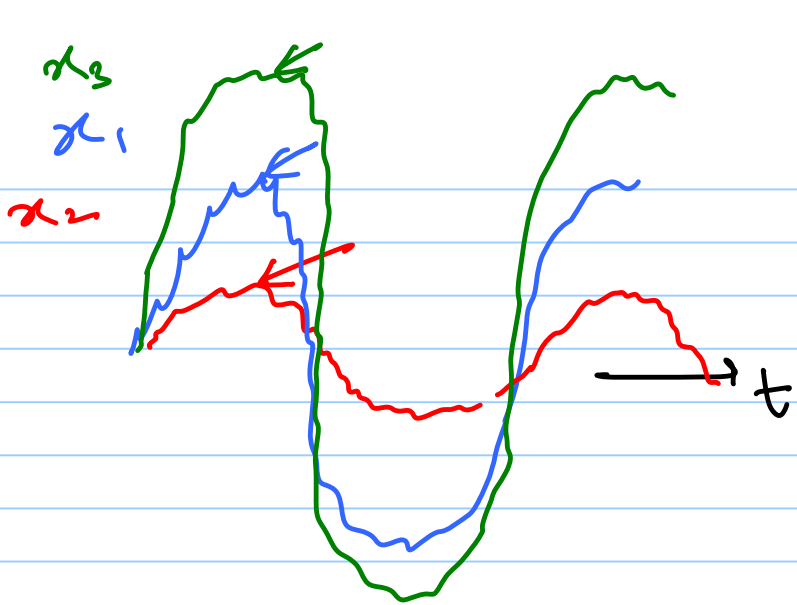


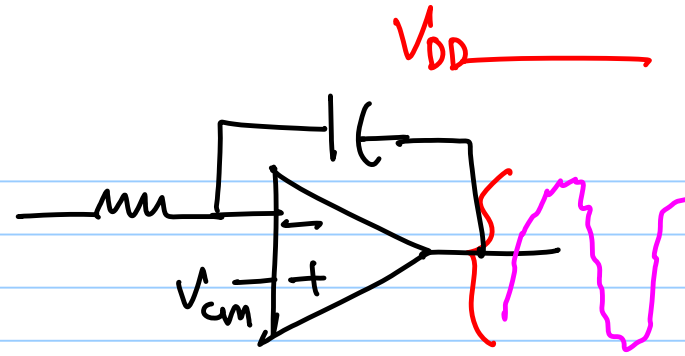
# ECE 615 - Lecture 20

## Dynamic Range Scaling



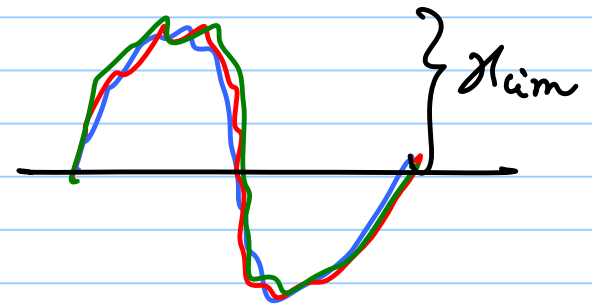


$$X = \begin{bmatrix} x_{1max} \\ x_{2max} \\ x_{3max} \end{bmatrix}$$



$$\underline{\underline{x_{lim} = \frac{1}{3} V_{DD}}}$$

⇒ scale ABCD ( ) in the Toolbox  
 ↑  
 $x_{max}$



$$x' = Sx$$

$$= \begin{bmatrix} \gamma_{s1} & & & 0 \\ & \gamma_{s2} & & \\ & & \ddots & \\ 0 & & & \gamma_{sn} \end{bmatrix} \begin{bmatrix} \lambda_{1, \max} \\ \lambda_{2, \max} \\ \vdots \\ \lambda_{n, \max} \end{bmatrix} \Rightarrow \lambda_{\min} \begin{bmatrix} | \\ | \\ | \\ | \end{bmatrix}$$

$$\gamma_i = \frac{\lambda_{\max, i}}{\lambda_{\min}}$$

DT ABCD matrix  $\Rightarrow$  state-space representation

$$x[n+1] = \underline{A} x[n] + \underline{B} \begin{bmatrix} u[n] \\ v[n] \end{bmatrix}$$

$$y[n] = \underline{C} x[n] + \underline{D} \begin{bmatrix} u[n] \\ v[n] \end{bmatrix}.$$

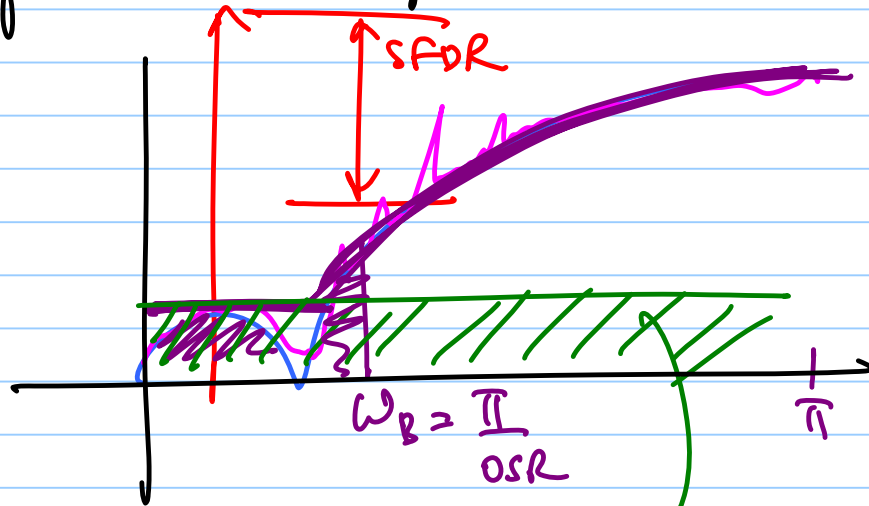
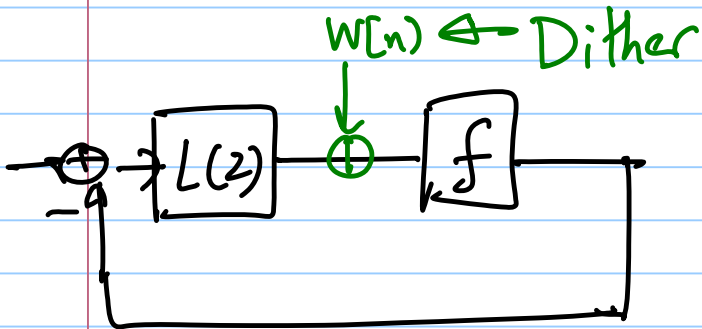
$$x_s = Sx$$

$$ABCD_s = \left[ \begin{array}{c|c} SAS^{-1} & SB \\ \hline CS^{-1} & D \end{array} \right] \Rightarrow$$

$$\left[ \begin{array}{c|c} A & B \\ \hline C & D \end{array} \right]$$

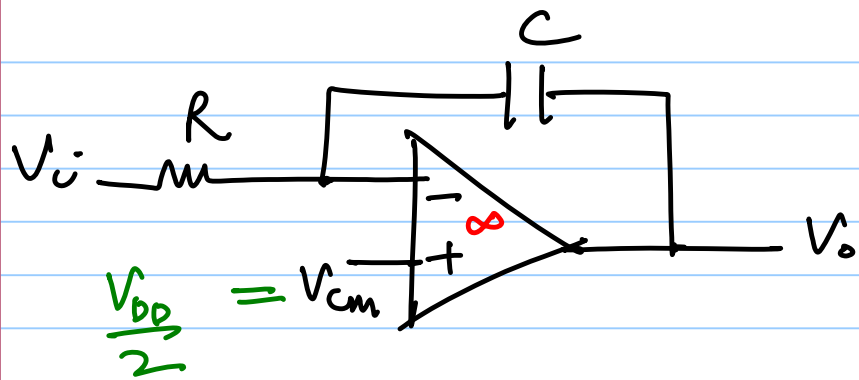
new  
 $a, b, c, d$ 's

# SQNR from system-level design



Overdesign the modulator for  
8-10 dB extra SNR

Use thermal noise from the circuit for Dithering

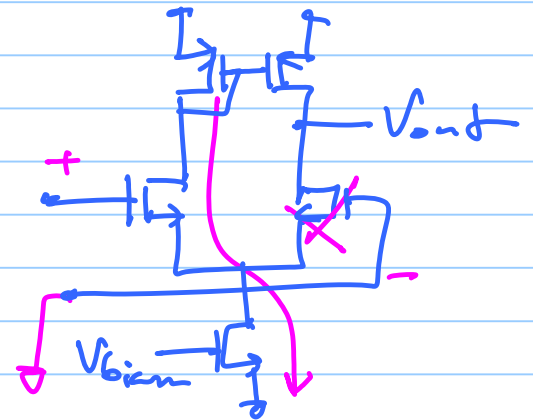


$$\frac{V_o}{V_i}(s) = \frac{1}{sRC}$$

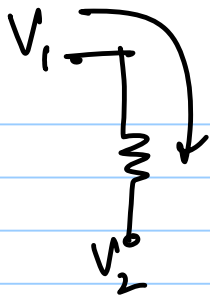
$R, C \pm 20\%$

$\frac{R_1}{R_2}$        $\frac{C_1}{C_2} \rightarrow < 0.1\%$

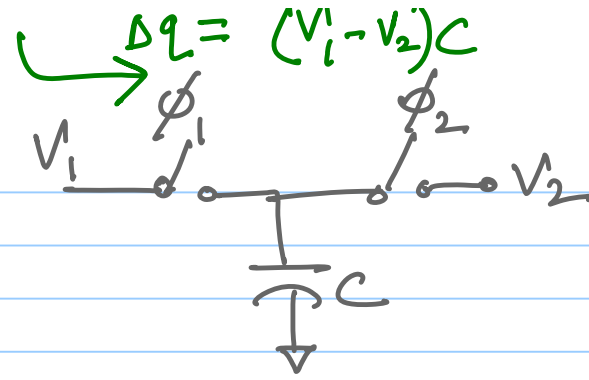
Cap ratios are tightly controlled on a chip



LM741  $\rightarrow \pm 15V$

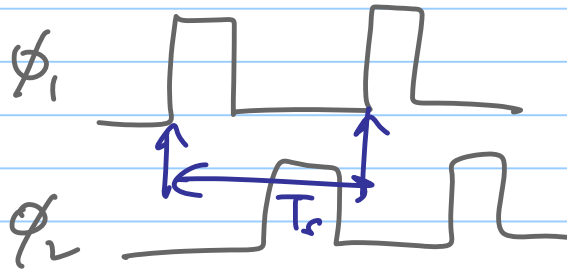


$$I = \frac{V_1 - V_2}{R}$$



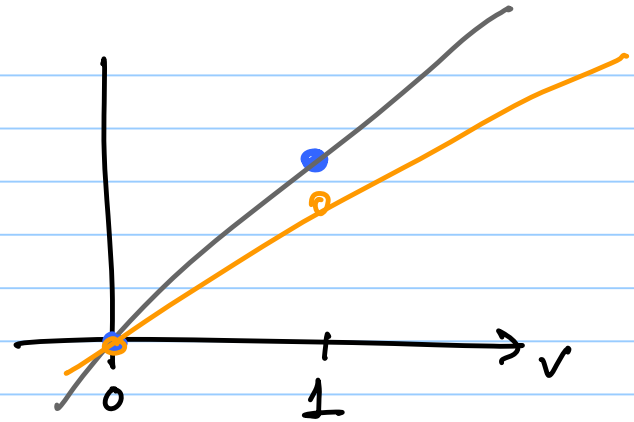
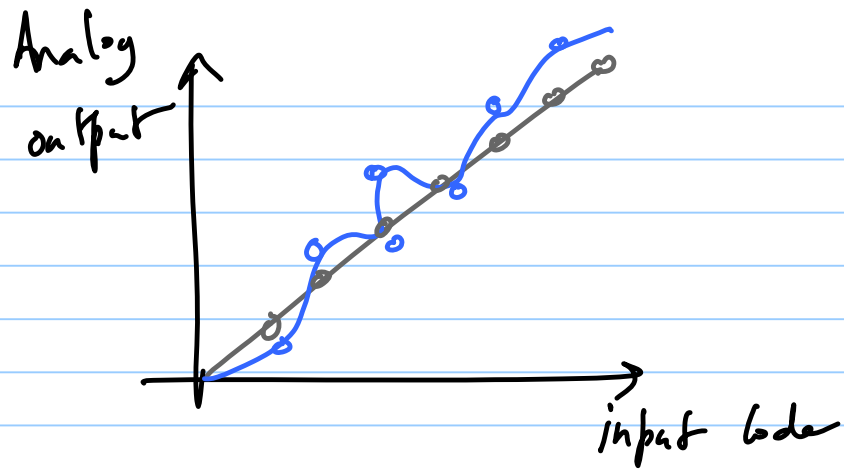
$$I = \frac{\Delta Q}{T_s} = \frac{C}{T_s} (V_1 - V_2)$$

$$= f_s C (V_1 - V_2)$$

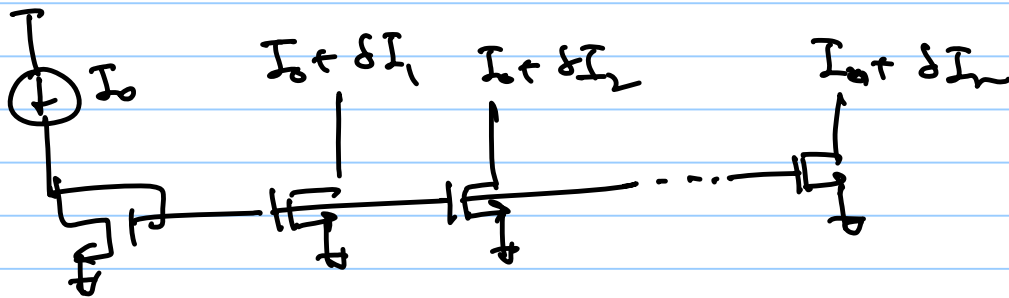


$$R = \frac{1}{f_s C}$$

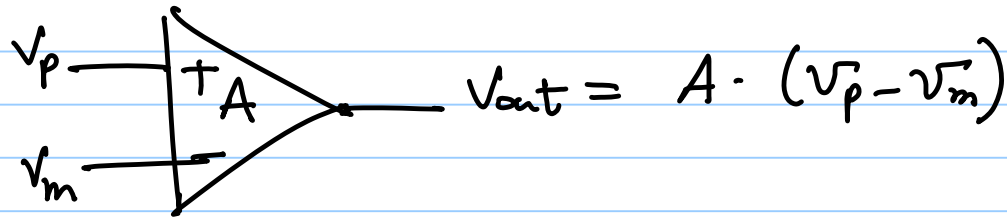
Switched-Cap Circuits  
 $\Rightarrow$  DT



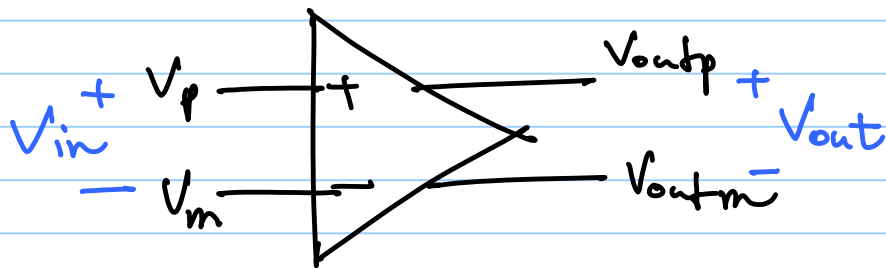
1-bit DAC is always "linear"







single-ended



$$(V_{outp} - V_{outm}) = A (V_p - V_m)$$