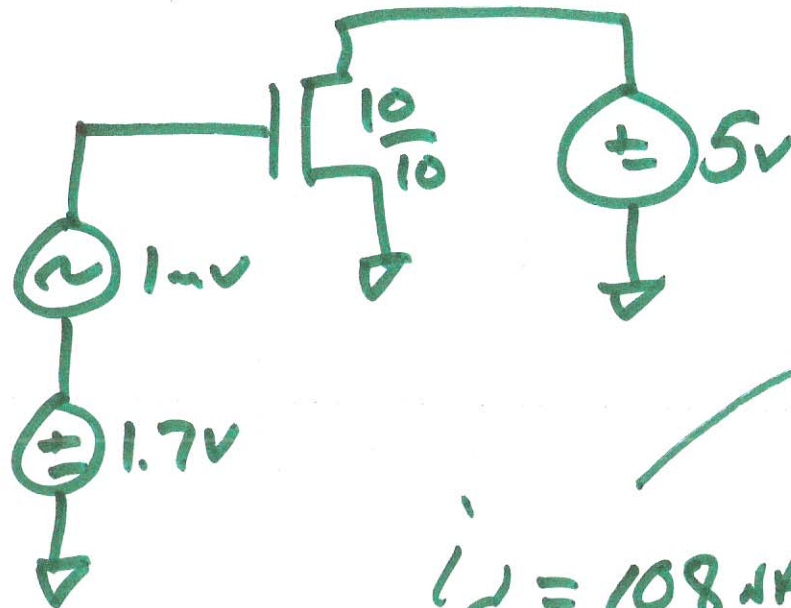


JANUARY 23, 2012

## Lecture 2



$$V_{gs} = 1\mu V$$

$$i_d = g_m V_{gs} = 1084 A \cdot 1\mu V$$

$$g_m = \frac{1}{2} K_P \frac{W}{L} (V_{gs} - V_{TH}) = 1084 A/V$$

$$= 1204 A/V (1.7 - .8) = 1084 A/V$$

~~$$= 484 A$$~~

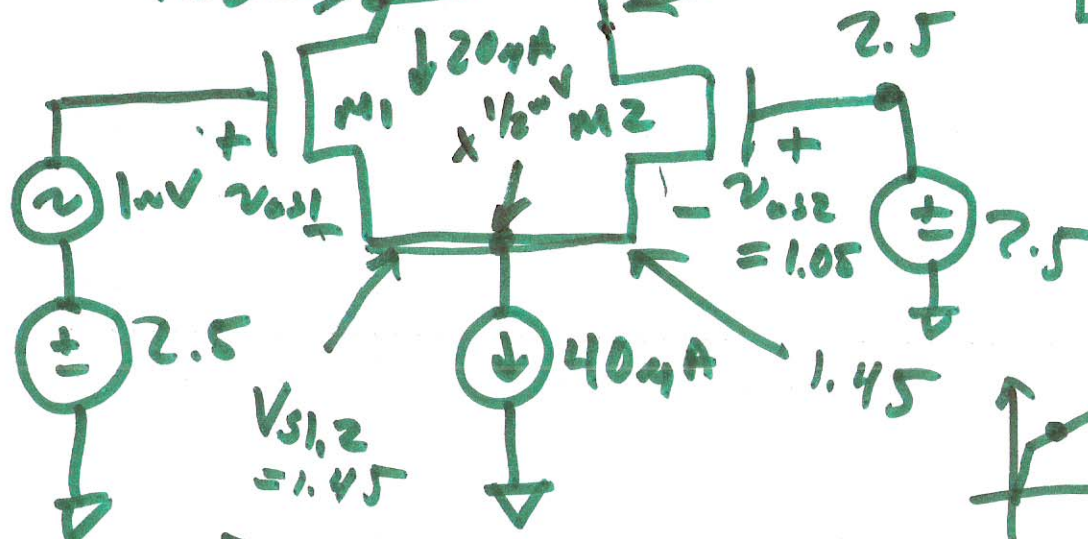
$$I_D = \frac{K_P}{2} \cdot \frac{W}{L} (1.7 - .8)^2 = .81 \cdot 604$$

$$I_D \approx 484 A$$

1)

PMOS  $\frac{39}{2} = \frac{94}{.64} + 5V$   
 NMOS  $\frac{10}{2} = \frac{34}{.64} M3$

$+V_{SG3} + V_{SG4}$   
 $V_{D3} \rightarrow$  triode



$$V_{GS1,2} = \sqrt{\frac{2I_N}{\beta_N}} + V_{THN}$$

$$= 1.05V$$

$$V_{S1,2} = 1.45V$$

AC & DC Voltages

$$I_{D1} = I_{D2} = 204A$$

$$V_{SG4} = 5V$$

$$I_D = \frac{K_P}{2} \frac{W_P}{L_P} (V_{SG} - V_{THP})^2$$

$$V_{SG3} = \sqrt{\frac{2I_P}{\beta_P}} + V_{THP}$$

$$= 1.15V$$

$$V_{DS} = V_{DD} - V_{SG3}$$

$$= 3.85V$$

SAT.

$$V_{DS}^{SD} \geq V_{GS}^{SG} - V_{THP}$$

$$\geq 5 - .9 = 4.1$$

$$V_{DS,SAT} = V_{GS} - V_{THN}$$

$$I_{D1} = \frac{\beta}{2} (V_{GS} - V_{THN})^2 \quad (\text{saturation})$$

$$I_D = \beta \left( (V_{GS} - V_{THN}) V_{DS} - \frac{V_{DS}^2}{2} \right) \quad (\text{triode})$$

$$I_D = 20 \mu A, \quad V_{SG} = 5V, \quad V_{THP} = .9V$$

$$20 \mu A = 40 \mu A \cdot \frac{30}{2} \left( (5 - .9) V_{DS} - \frac{V_{DS}^2}{2} \right)$$

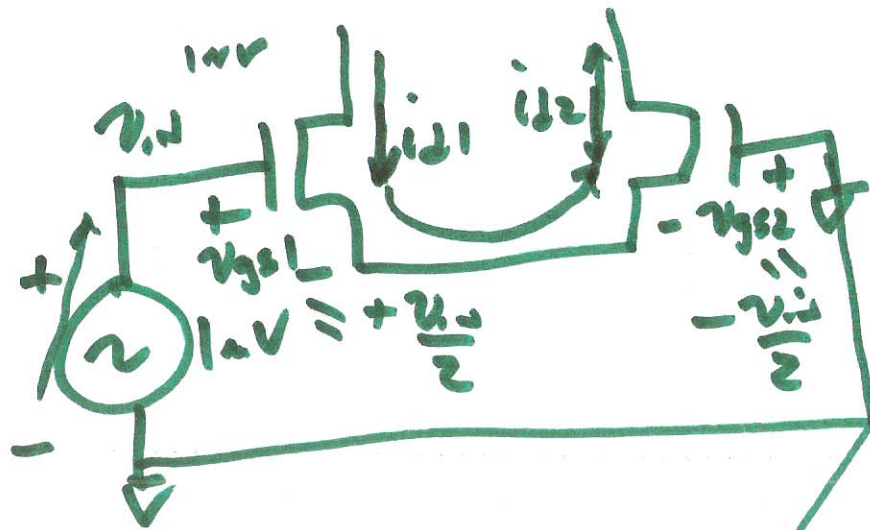
$$\frac{V_{DS}^2}{2} - 4.1 V_{DS} + \frac{1}{30} = 0$$

$$V_{DS}^2 - 8.2 V_{DS} + \frac{1}{15} = 0$$

$$V_{DS} = \frac{8.2 \pm \sqrt{(8.2)^2 - 4/15}}{2} = 8 \mu$$

$$\approx \frac{4}{30} = \frac{1}{7.5} V$$

3)



$$v_{in} = v_{gs1} - v_{gs2}$$

$$i_d = g_m v_{gs}, v_{gs} = \frac{i_d}{g_m}$$

$$i_{d1} = -i_{d2} = i_d$$

$$+0.14 \rightarrow 20.1 \text{ } i_d = 14 \mu\text{A}$$

$$-0.14 \rightarrow 12.9$$

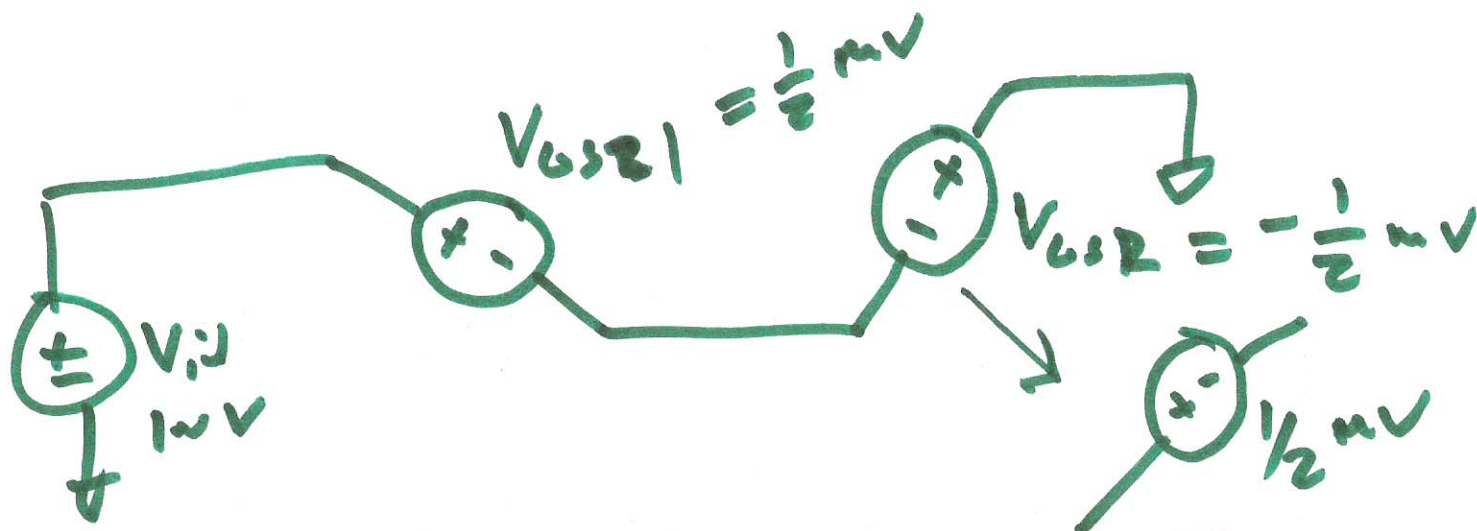
$$i_d = -0.14 \mu\text{A}$$

$$v_{in} = \frac{i_{d1}}{g_m} - \frac{i_{d2}}{g_m} = \frac{2i_d}{g_m}$$

$$v_{gs1} = \frac{v_{in}}{2}$$

$$v_{gs2} = -\frac{v_{in}}{2}$$

$$v_{in} = \frac{v_{in}}{2} - \left(-\frac{v_{in}}{2}\right) \quad i_d = g_m \frac{v_{gs}}{2}$$



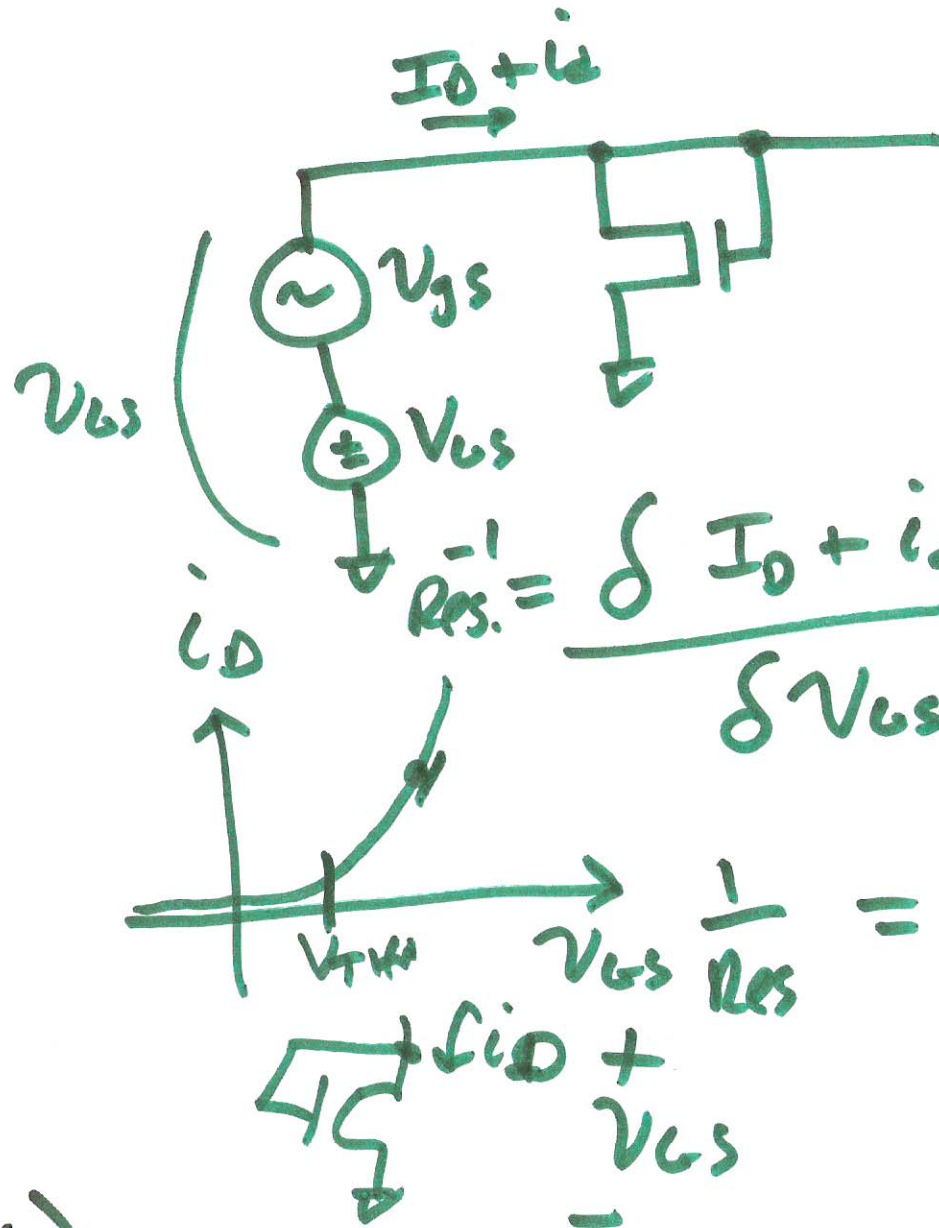
$$g_m = \sqrt{2\beta I_0} = \sqrt{2 \cdot 120\mu A/V^2 \cdot \frac{10}{2}\mu A} = 150\frac{\mu A}{V}$$

$$v_{gs} = \frac{1}{2}\mu V$$

$$i_d = \frac{1}{2}\mu V \cdot 150\mu A$$

$$= \underline{\underline{75nA}}$$

5.4)

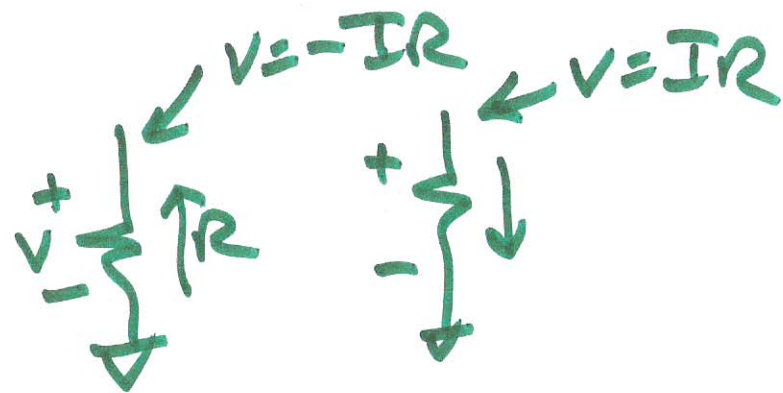
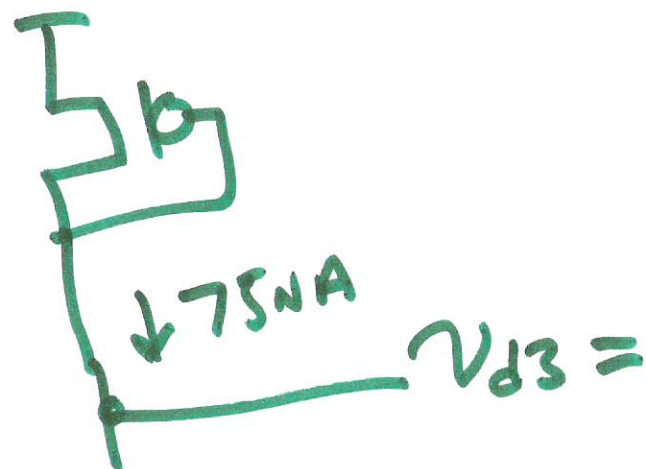


$$\text{s.s. Resistance} = \frac{v_{gs}}{i_d} = \frac{1}{g_m}$$

$$R_{es}^{-1} = \frac{\delta I_D + i_d}{\delta v_{gs}} = \frac{\delta \left( \frac{\beta_N}{2} (v_{gs} + v_{ds} - V_{TN})^2 \right)}{\delta v_{gs}}$$

$$\frac{1}{R_{es}} = \beta_N (v_{gs} - V_{TN} - v_{ds}) = g_m \approx g_m \text{ since } v_{ds} \gg v_{gs}$$

6)



$$\frac{1}{g_m} = \frac{1}{150\text{ nA}} = 6.5\text{ k}\Omega$$

$$75\text{ nA} \downarrow \quad V_{D3} = -75\text{ nA} \cdot 6.5\text{ k}\Omega = \underline{\underline{-\frac{1}{2}\text{ mV}}}$$

7)