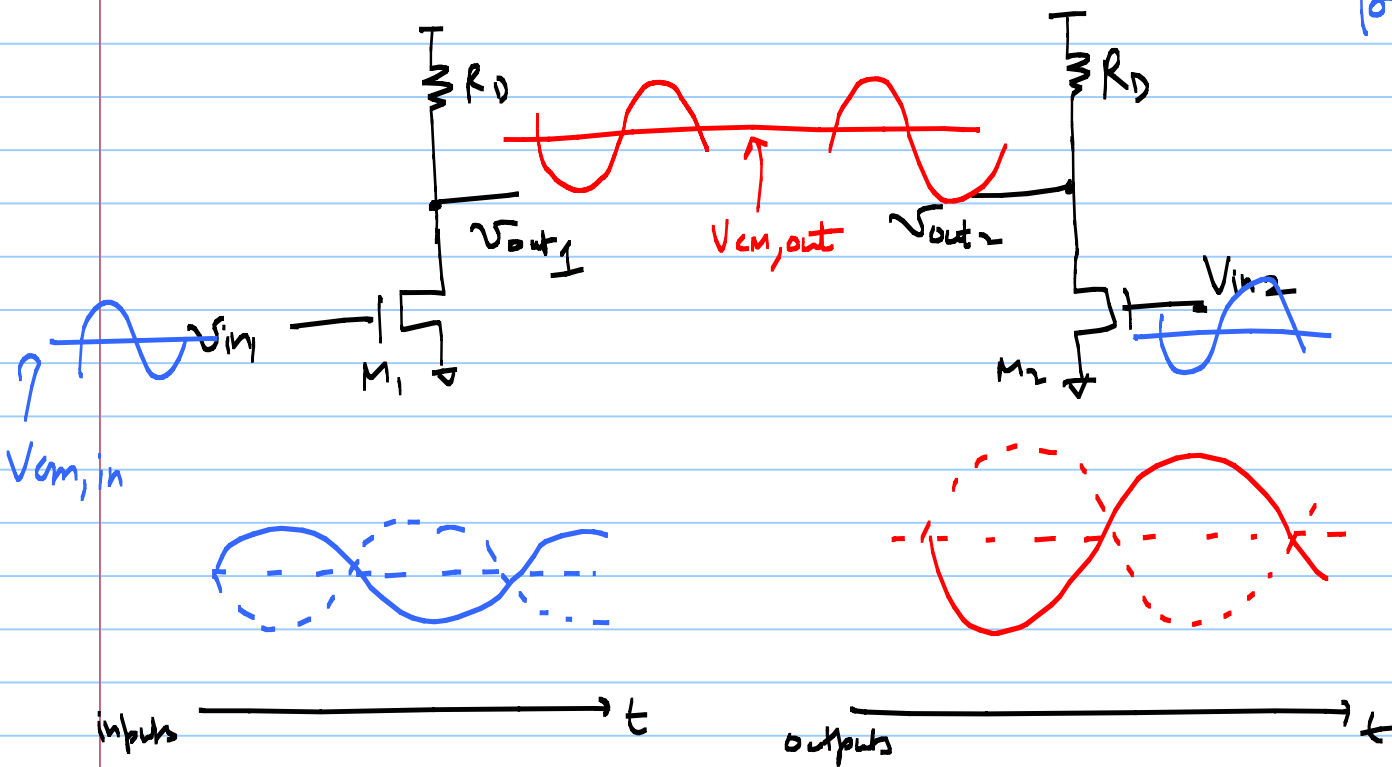


ECE 5411 - Lecture 19.

Note Title

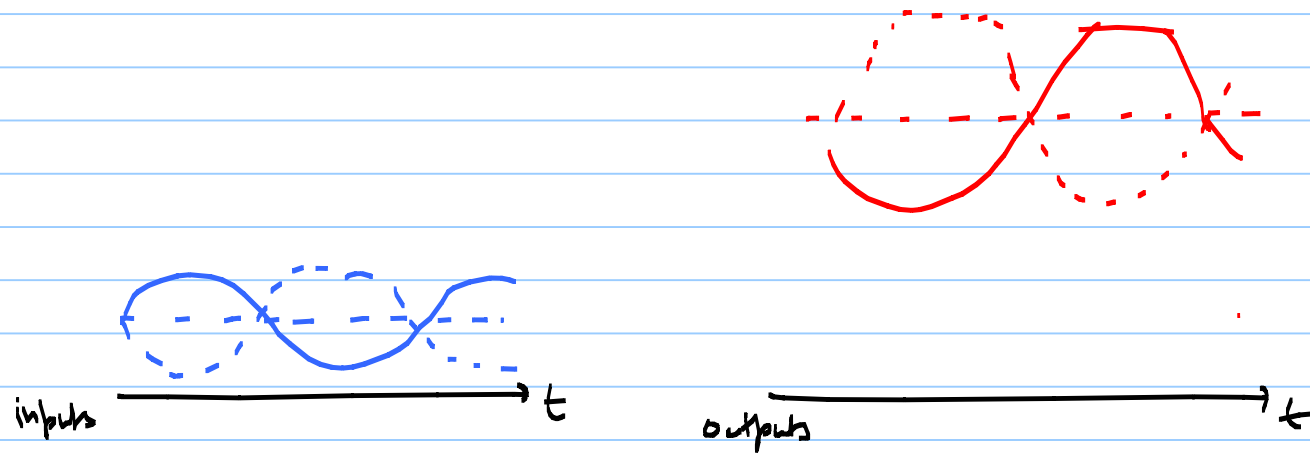
4/6/2011

* Use two identical single-ended signal paths to bootstrap the two phases.



* rejection of CM noise
PS noise

* 2x output swing



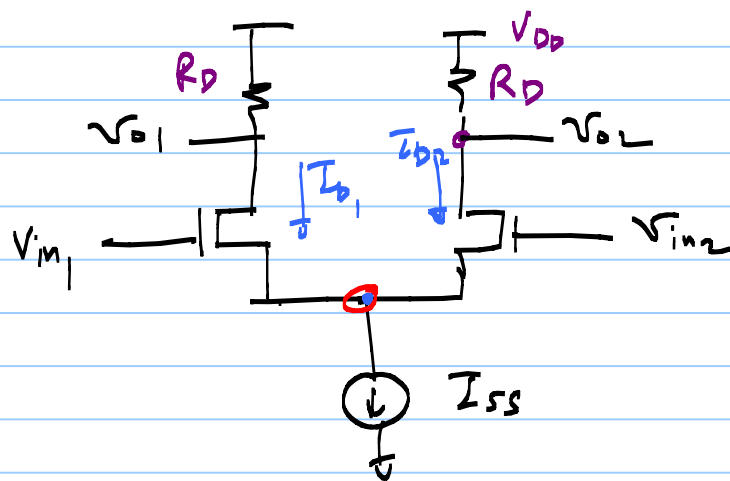
As the input CM level changes

↳ bias currents in M_1 & M_2 are changing

↳ g_m

↳ output CM level varying

* Important for biasing that the devices have minimal dependence on input CM level.



$$I_{D1} + I_{D2} = I_{SS}$$

independent of the $V_{in, CM}$.

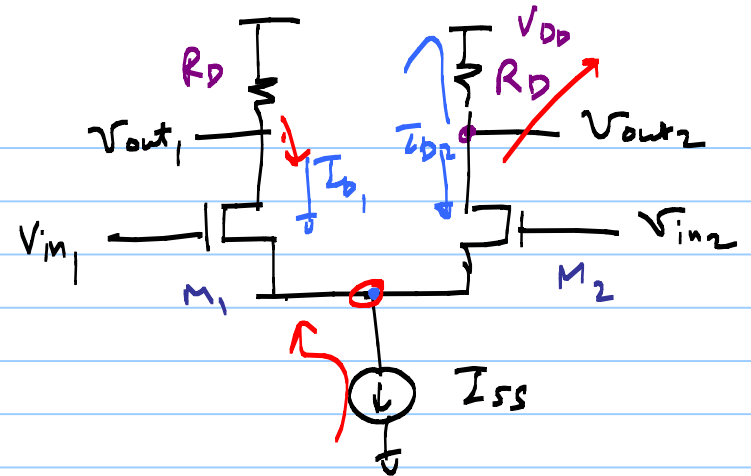
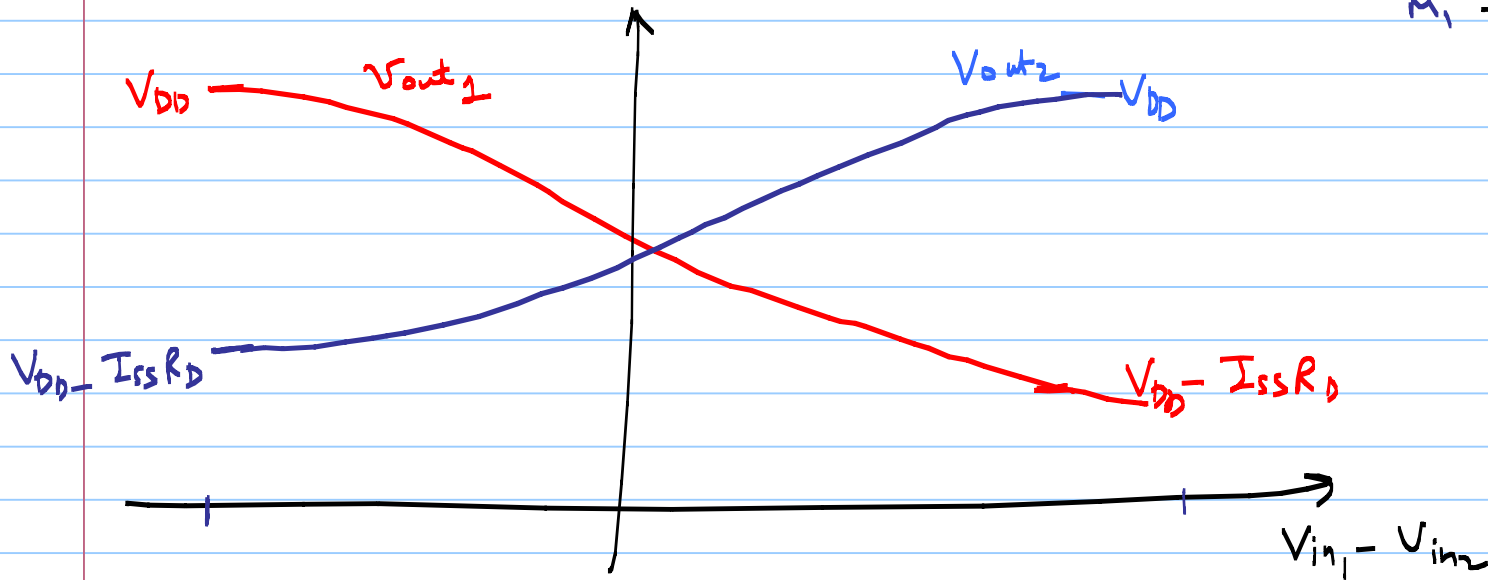
Differential pair (d.f. pair)

if $V_{in1} = V_{in2} \Rightarrow I_{D1} = I_{D2} = \frac{I_{SS}}{2}$

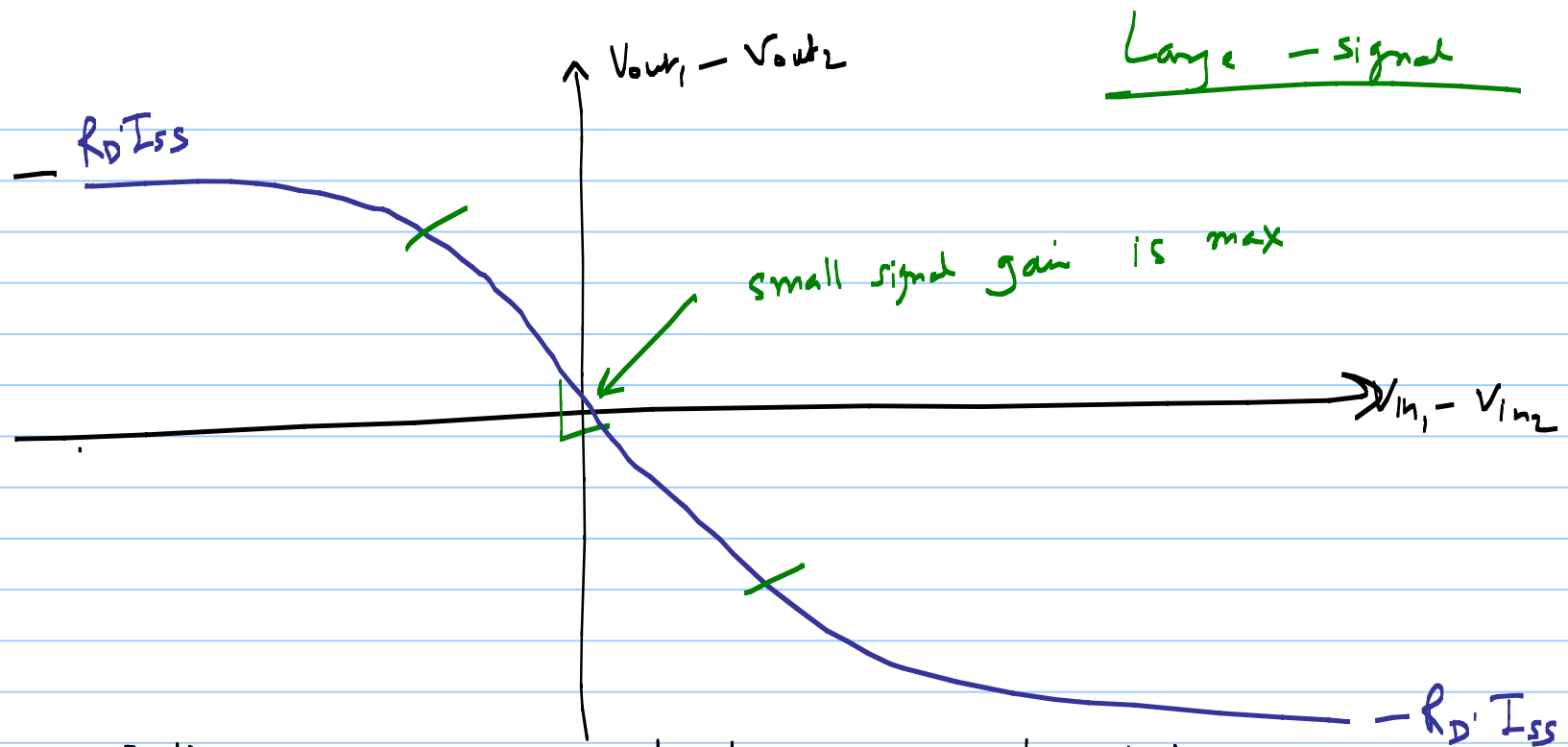
$$V_{out, cm} = V_{DD} - \frac{I_{ss}}{2} \cdot R_D \leftarrow \text{output common mode level is set}$$

Qualitative Analysis :

* Assume $(V_{in1} - V_{in2})$ varies from $-\infty$ to ∞



$$I_{D1} + I_{D2} = I_{SS}$$



* Output max & min levels are well defined.

↳ independent of input CM level

* The tail current source suppresses the effect of input cm level variations on the operation of M_1 & M_2 & the output level.

Ⓐ

$$V_{in,cm} = 0$$

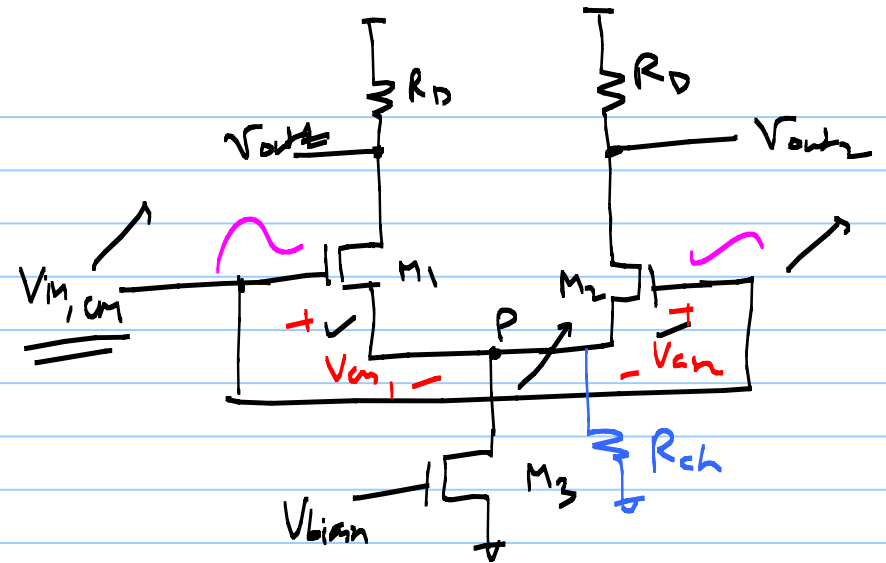
$M_1, M_2 \leftarrow$ cut-off

$$I_{D3} = 0$$

$M_3 \Rightarrow$ deep triode

$$V_{out1} = V_{out2} = V_{DD}$$

$\Rightarrow$ no amplification



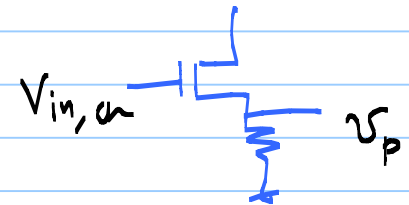
Ⓑ

$$V_{in,cm} > V_{THN}$$

$\Rightarrow M_3$ still in triode

$\Rightarrow V_p$ increases and tracks $V_{in,cm}$

$\Rightarrow V_{out1,2}$ start decreasing



③

$$\underline{V_{in,cm} \geq V_{as,1} + V_{ds,sat,3}}$$

↳ M_3 enters saturation

↳ total current $\frac{I_{ss}}{2}$ each $\rightarrow I_{ss}$ ($r_{o3} = \infty$)

④

$$\underline{V_{in,cm} > V_{out,1,2} + V_{thn} = \left(V_{DD} - \frac{R_D I_{ss}}{2} \right) + V_{thn}}$$

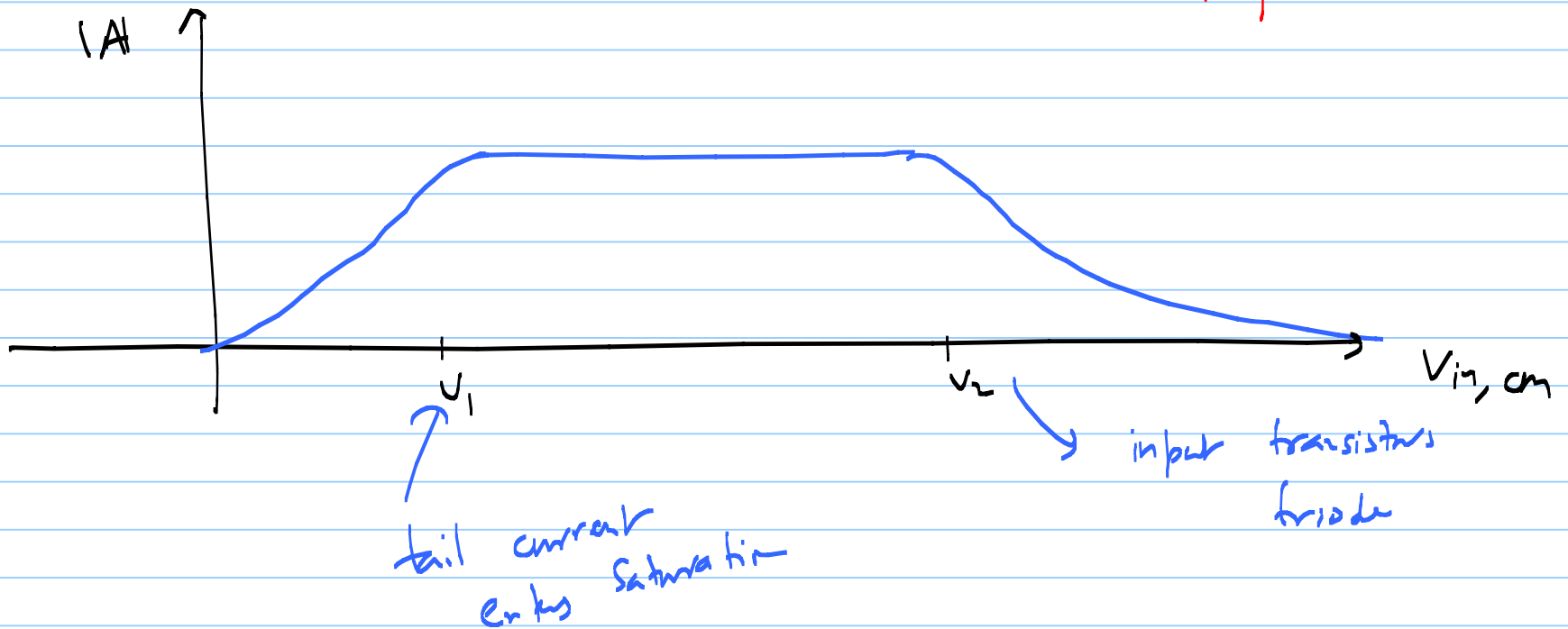
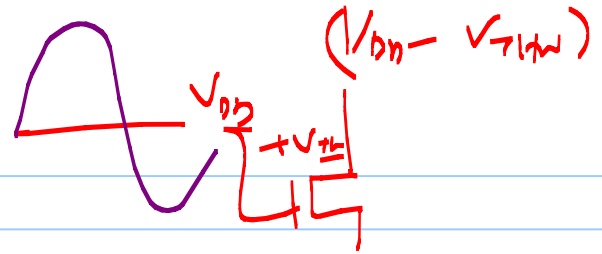
$\Rightarrow M_1$ & M_2 start trioding

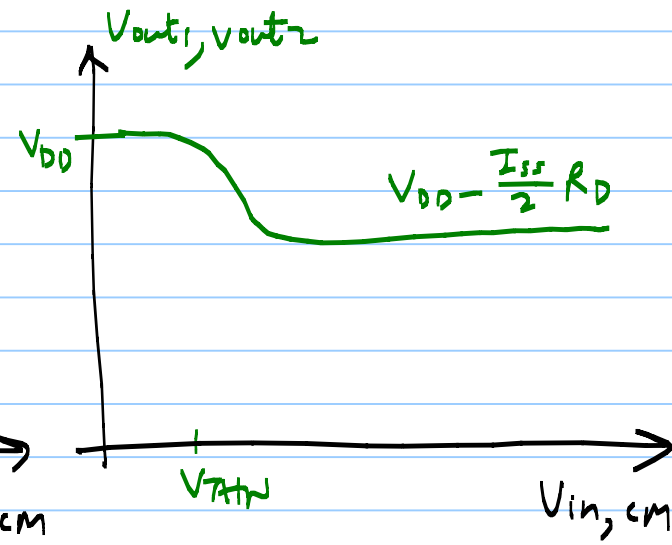
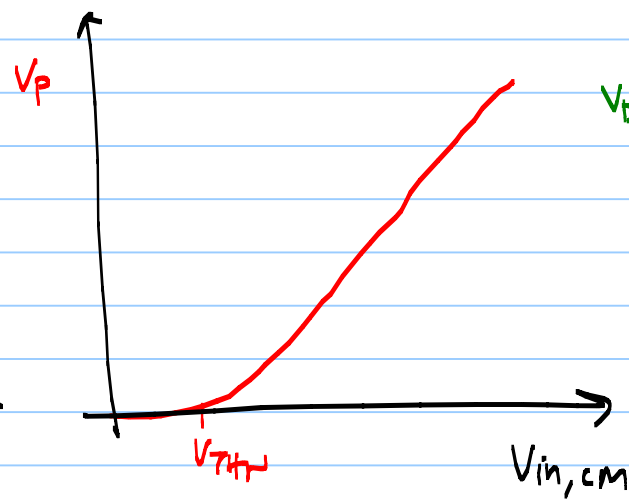
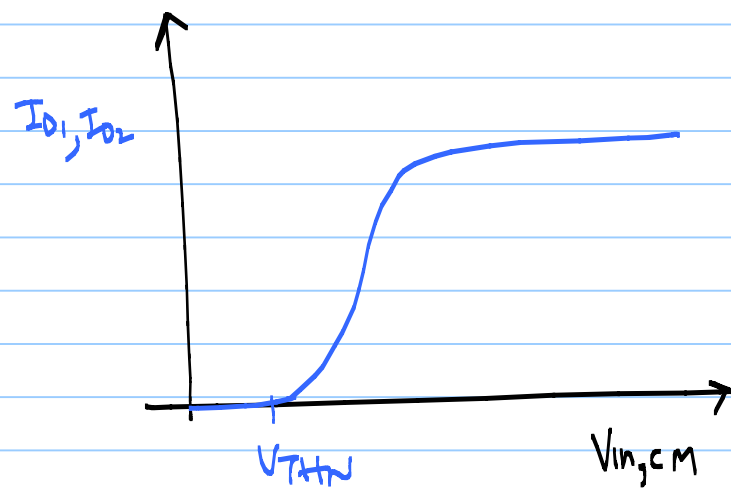
↳ sets upper limit on $V_{in,cm}$

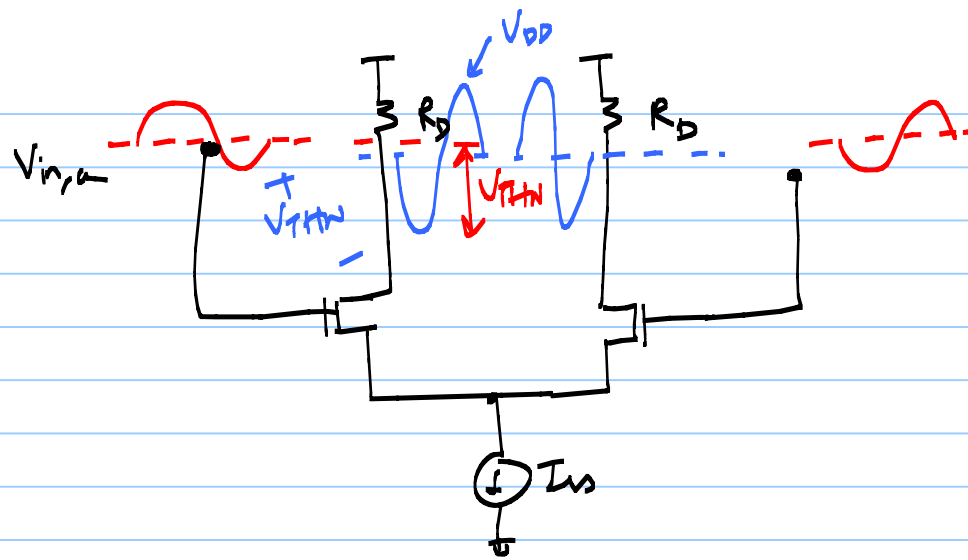
* Input common-mode range (CMR)

$$V_{as,1} + V_{ds,sat,3} \leq V_{in,cm} \leq \boxed{\left(V_{DD} - \frac{R_D I_{ss}}{2} \right) + V_{thn}}$$

$$V_{in,cm} = V_{oh}$$





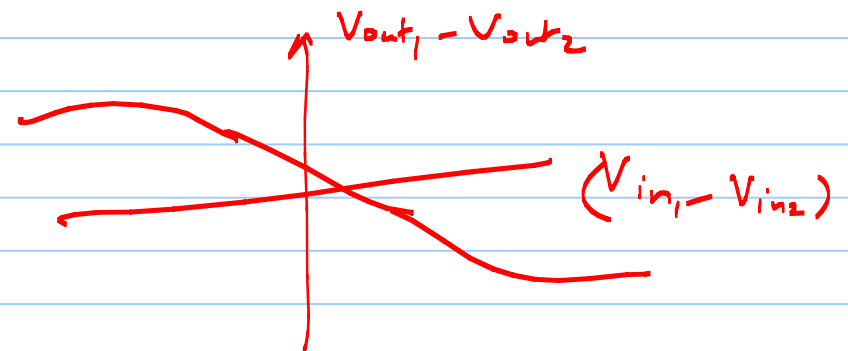


v/p can swing from $(V_{in,cm} - V_{THN})$ to V_{DD} .

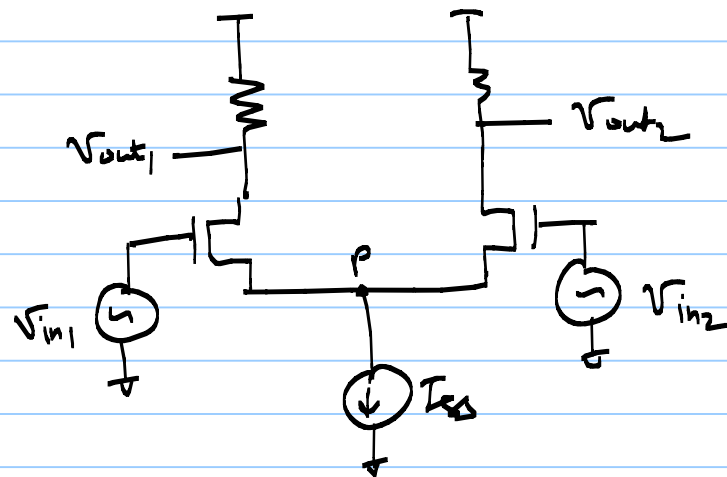
→ The higher the input cm level
↳ lower the output swing.

Large Signal Analysis :

$$I_{D1} - I_{D2} = \frac{\beta}{2} (V_{in1} - V_{in2}) \sqrt{\frac{4I_{SS}}{\beta} - (V_{in1} - V_{in2})^2}$$



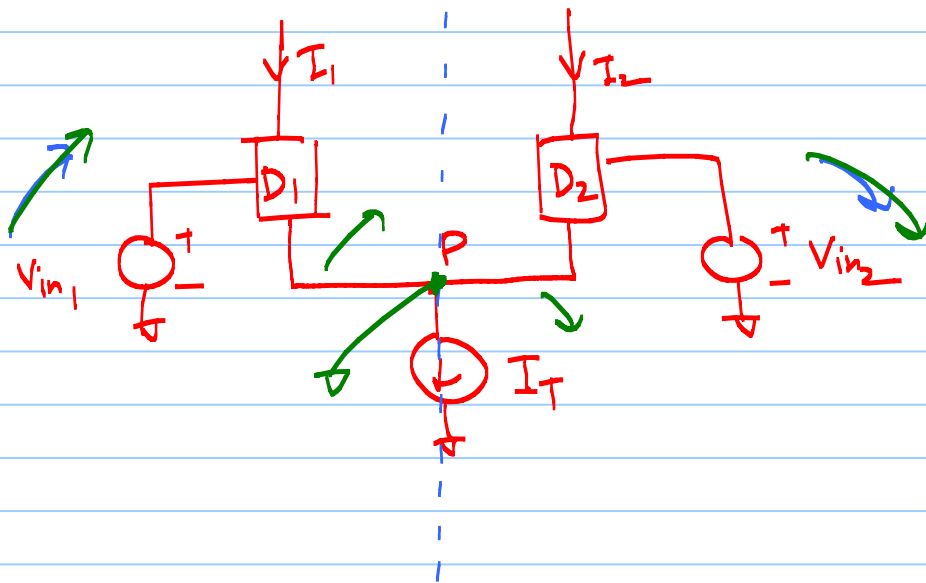
Small-Signal Analysis :



$$A_v = \frac{(V_{out1} - V_{out2})}{(V_{in1} - V_{in2})}$$

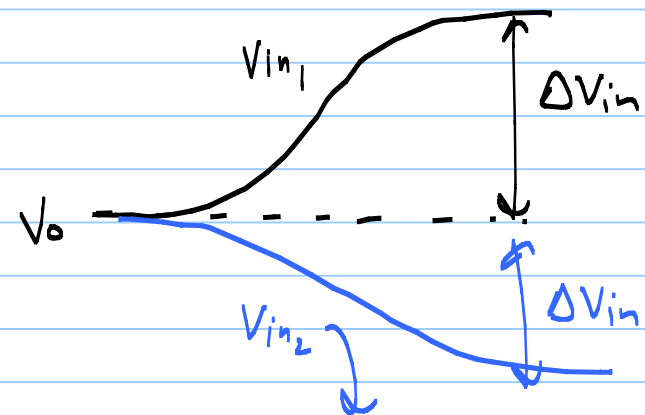
'Half-Circuit Analysis'

Lemma:



D_1 & $D_2 \rightarrow$ any 3-terminal devices

"Inputs are differential"

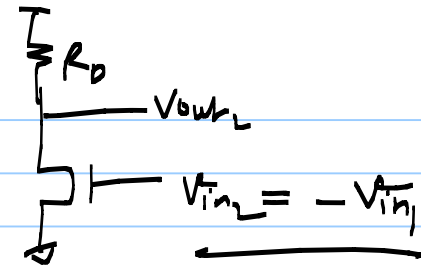
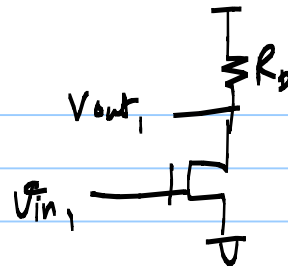
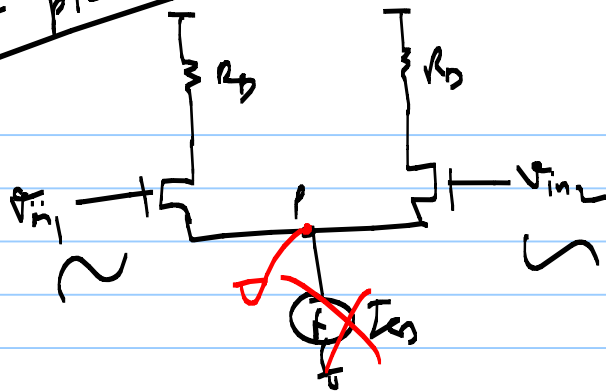


If the circuit is linear

$\Rightarrow V_p$ doesn't change at all. ($\lambda=0$)

$\Rightarrow P$ is ac ground.

Az picture



$$\frac{V_{out1}}{V_{in1}} = -g_{m1}(R_D || r_{o1})$$

$$g_{m1} = g_{m2}$$

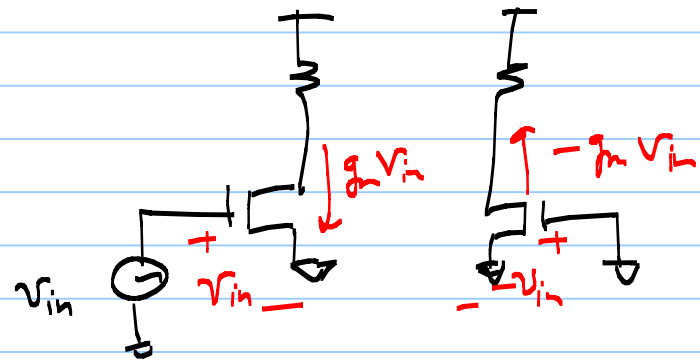
$$r_{o1} = r_{o2}$$

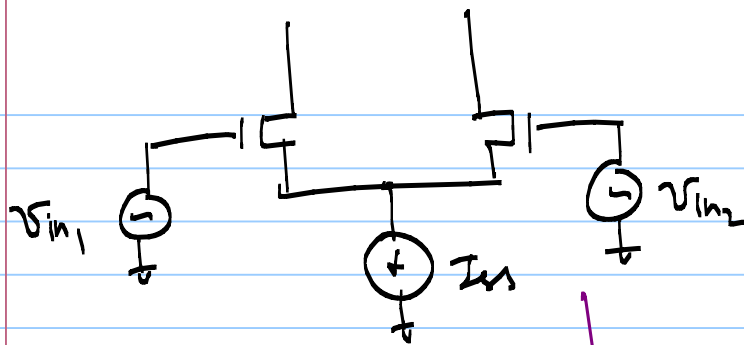
$$\frac{V_{out2}}{V_{in2}} = g_{m2}(R_D || r_{o2})$$

$$\frac{V_{out1} - V_{out2}}{V_{in1} - V_{in2}} = -g_m(R_D || r_o)$$

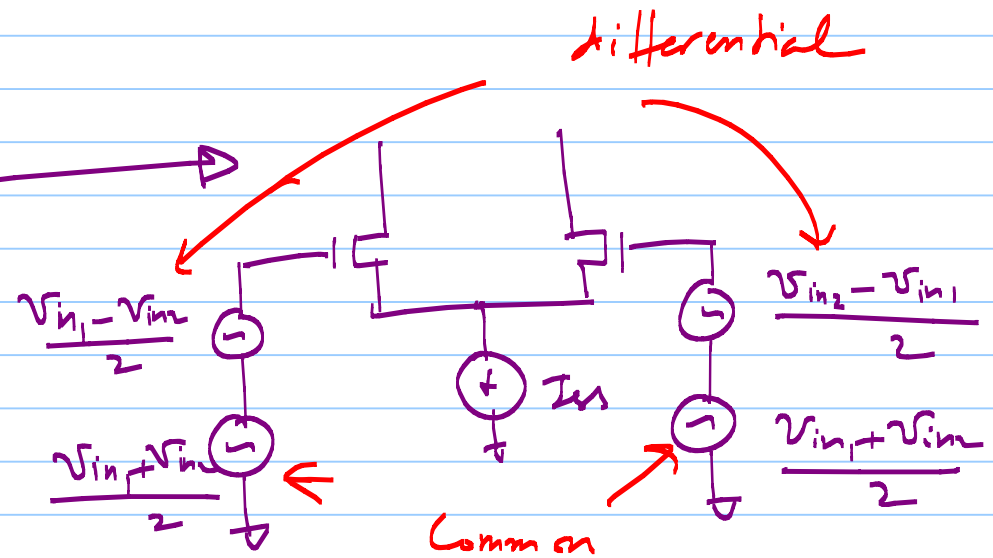
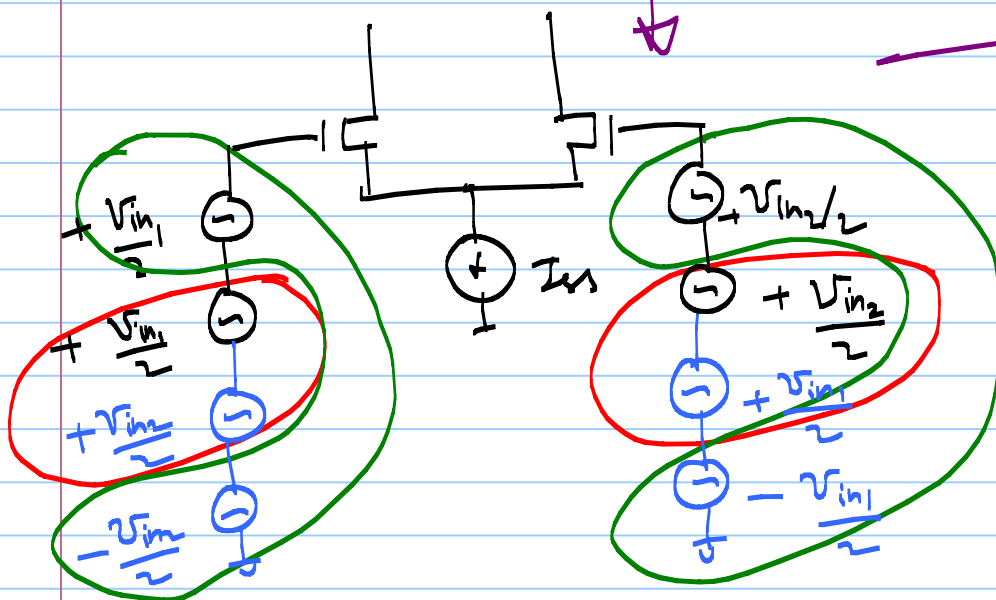
$+ V_{in1}$

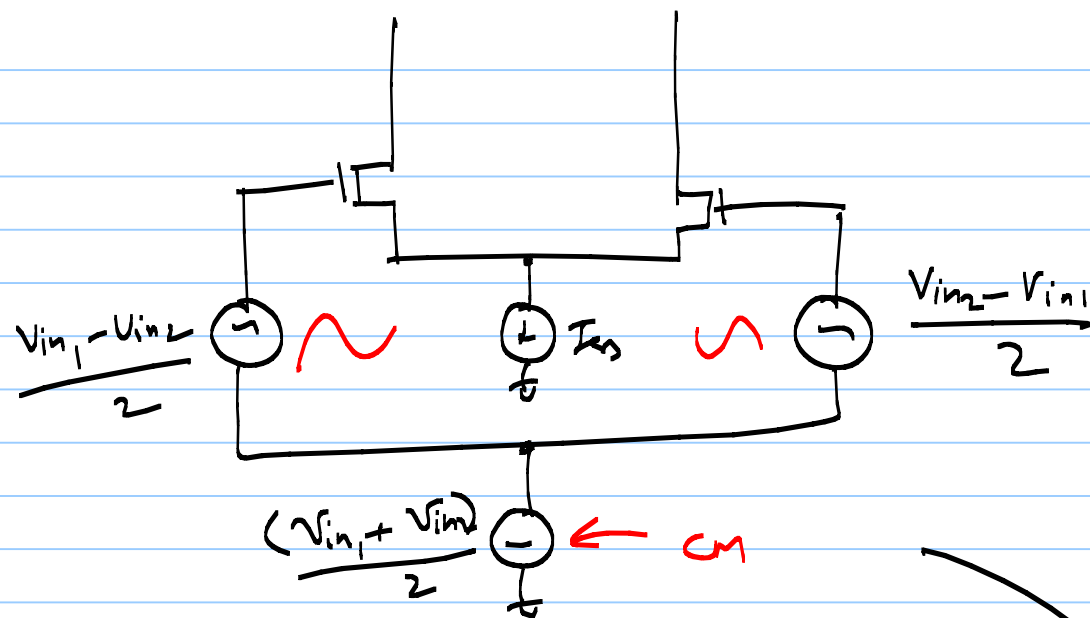
$$\frac{v_{out1}}{v_{in1} - v_{in2}} = - \frac{g_m (R_o || r_o)}{2}$$



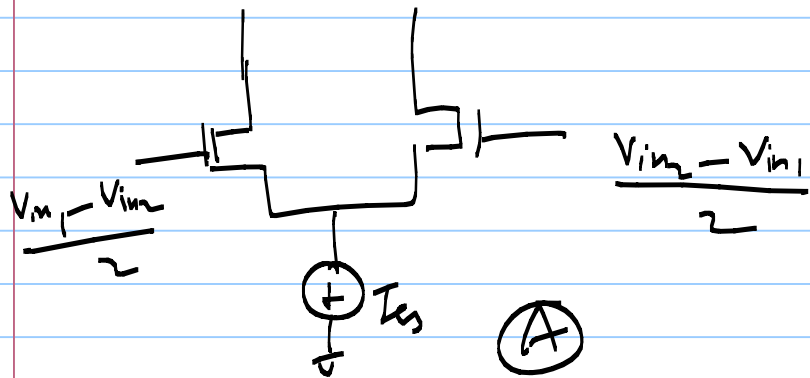


$\Rightarrow v_{in1}, v_{in2}$ are not differential

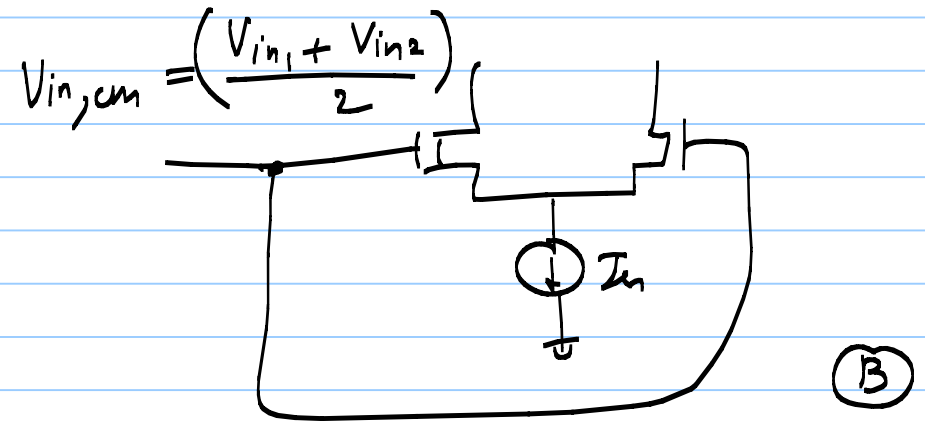




"Linear Superposition"



Differential Mode



Common Mode

$$\begin{aligned}
 V_{in1} &= \left(\frac{V_{in1} - V_{in2}}{2} \right) + \left(\frac{V_{in1} + V_{in2}}{2} \right) \\
 V_{in2} &= \left(\frac{V_{in2} - V_{in1}}{2} \right) + \left(\frac{V_{in1} + V_{in2}}{2} \right)
 \end{aligned}$$

DM

CM



