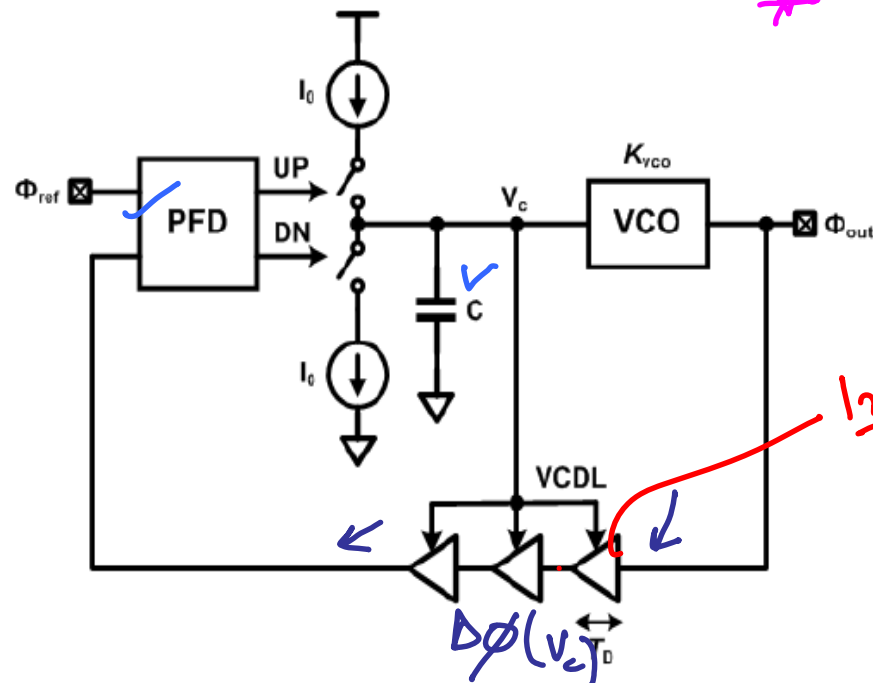


ECE 518 - Lecture 24

Note Title

4/14/2015



* phase-domain proportional path

$$T_{CK} = 2ns$$

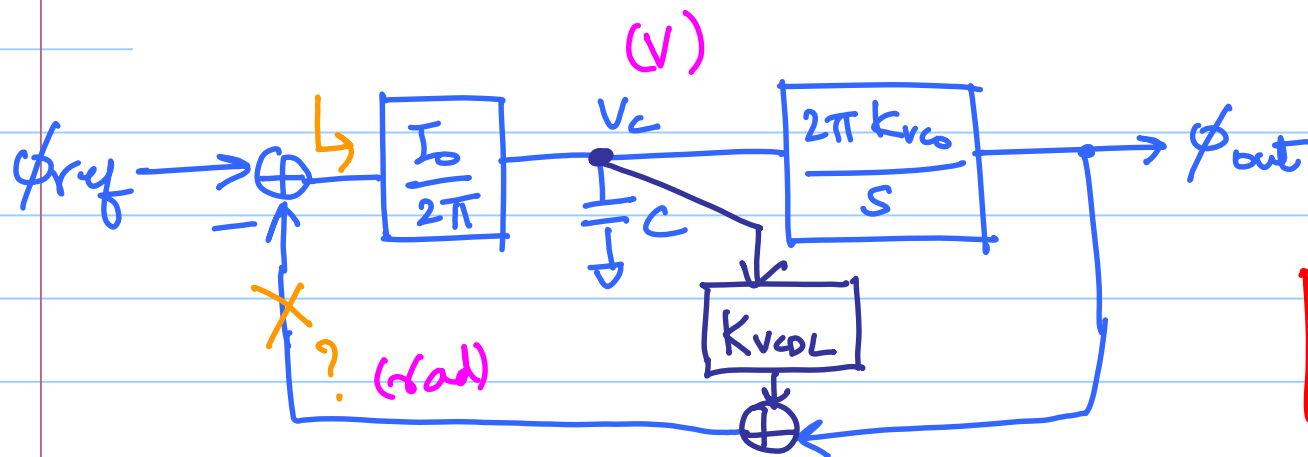
$$K_{VCO} = \frac{150 \text{ MHz}}{V}$$

$$\frac{1ns}{V}$$

(a) (10 points) Draw the phase-domain small signal block diagram in steady state.

$$K_{VCDL} = 3 \frac{ns}{V}$$

$$\frac{D}{T_{CK}} = \frac{3 \frac{ns}{V}}{2ns} \times 2\pi \frac{rad}{V}$$



$$K_{VCDL} = 3\pi \frac{rad}{V}$$

(b)

$$L(s) = \frac{I_0}{2\pi sC} \left(\frac{2\pi K_{vco}}{s} + K_{vcol} \right)$$

proportional path
→ adds LHP zero in the loop-gain

$$= \frac{2\pi I_0 K_{vco}}{2\pi C s^2} \left(1 + \frac{s K_{vcol}}{2\pi K_{vco}} \right)$$

$$= \frac{I_0 K_{vco}}{C s^2} \left(1 + \frac{s}{\omega_z} \right)$$

$s = -\omega_z$
LHP zero

$$\omega_{p1} = \omega_{p2} = 0$$

$$\omega_z = \frac{2\pi K_{vco}}{K_{vcol}}$$

(c) (10 points) Determine the value of capacitor C to achieve loop-gain phase-margin of 45° .

$$\omega_{u,loop} \leftarrow \text{loop BW}$$

$$L(s) = \frac{I_o K_{vco}}{C s^2} \left(1 + \frac{s K_{vcdL}}{2\pi \cdot K_{vco}} \right)$$

$$\omega_c \omega_{u,loop} \gg \omega_z$$

$$\approx \frac{I_o}{C} \cdot \frac{K_{vco}}{s^2} \times \frac{s K_{vcdL}}{2\pi K_{vco}}$$

$$\boxed{\omega_{u,loop} \approx \frac{I_o K_{vcdL}}{2\pi C}}$$

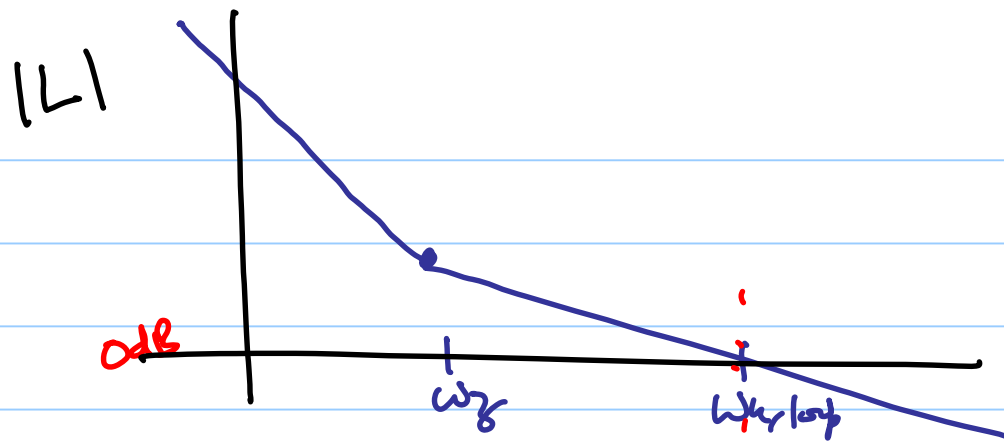
Approximated

$$\phi_M = \tan^{-1} \left(\frac{\omega_{u,loop}}{\omega_z} \right) = \tan^{-1} \left(\frac{I_o K_{vcdL}}{2\pi C} \times \frac{K_{vcdL}}{2\pi K_{vco}} \right) = 45^\circ$$

$$\frac{I_o K_{vcdL}^2}{(2\pi)^2 K_{vco} \cdot C} = \tan(45^\circ) = 1$$

$$\Rightarrow \boxed{C = ?}$$

Phase margin
for Type-II poles &
1 zero



LHP zero adds to the phase

$$+ \tan^{-1} \left(\frac{\omega}{\omega_g} \right)$$

$$\omega = \omega_{u/loop}$$



$$\phi_M = \tan^{-1} \left(\frac{\omega_{u/loop}}{\omega_g} \right)$$

(d) (10 points) Derive the expression for closed-loop transfer function $H_{cl}(s) = \frac{\Phi_{out}}{\Phi_{ref}}$.

$$H_{cl}(s) = \frac{L(s)}{1 + L(s)}$$

$$L(s) = \frac{I_0 K_{vco}}{C s^2} \left(1 + \frac{s K_{vco} L}{2\pi \cdot K_{vco}} \right)$$

$$= \frac{\frac{I_0 K_{vco}}{C s^2} \left(1 + \frac{s K_{vco} L}{2\pi K_{vco}} \right)}{1 + \frac{I_0 K_{vco}}{C s^2} \left(1 + \frac{s K_{vco} L}{2\pi K_{vco}} \right)}$$

$$H_{cl} = N \cdot \frac{L(s)}{1 + L(s)}$$

$$= \frac{\frac{I_0 K_{vco}}{C} \left(1 + \frac{s K_{vco} L}{2\pi K_{vco}} \right)}{s^2 + \frac{I_0 K_{vco} L}{2\pi C} s + \frac{I_0 K_{vco}}{C}}$$

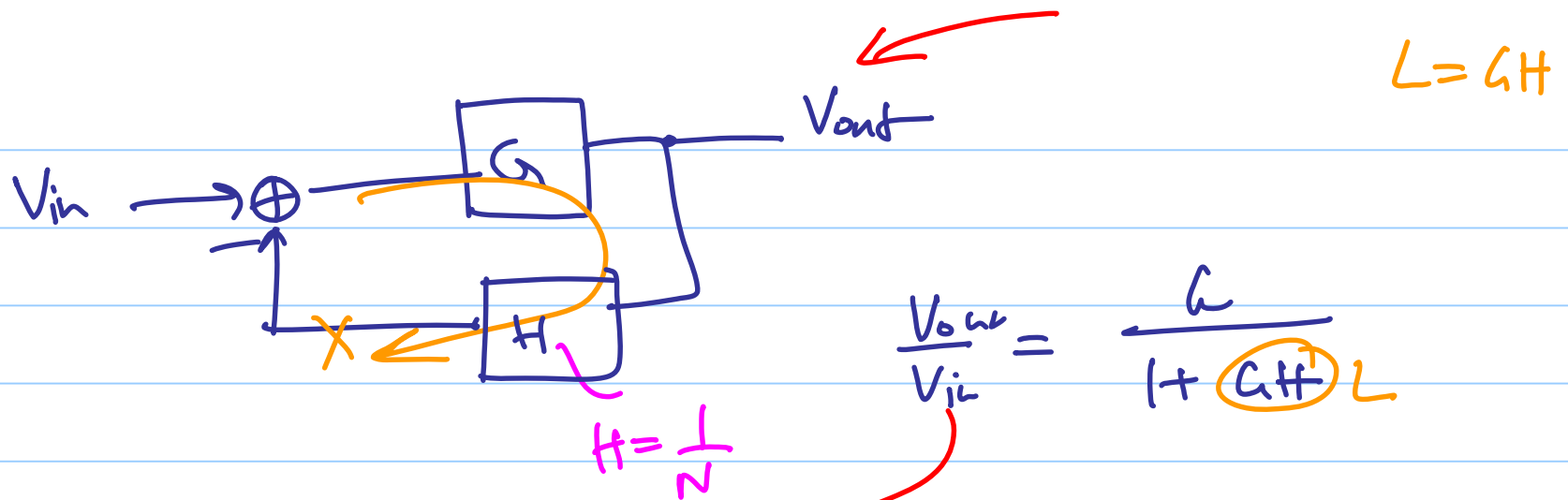
$$= \frac{k \cdot (1 + s/\omega_z)}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

$$\omega_n = \sqrt{\frac{I_0 K_{VCO}}{C}}, \quad \zeta = \frac{I_0 K_{VCO}}{2\pi C} \cdot \frac{1}{2\omega_n}$$

(e) (5 points) Sketch open- and closed-loop Bode magnitude and phase plots for the PLL.

* Look into lecture notes



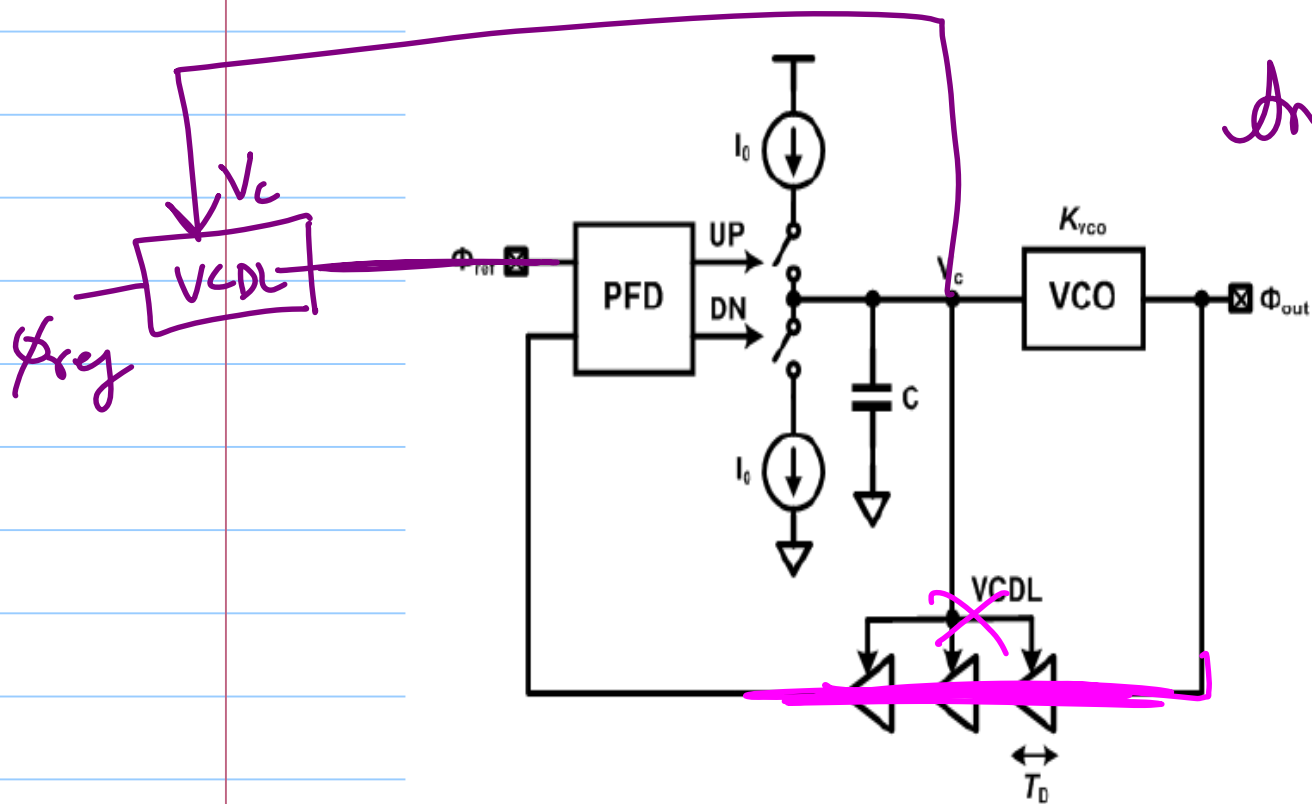


$$\frac{V_{out}}{V_{in}} = N \cdot \left(\frac{L}{1 + L} \right)$$

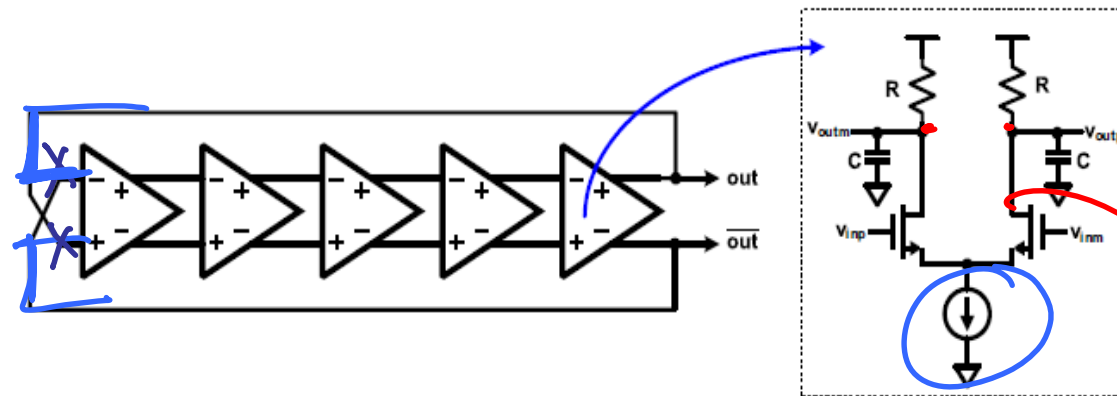
$$L = G_c \cdot H = \frac{G_c}{N}$$

$$G_c = N \cdot L$$

(f) (Bonus 5 points) What is the main difference between the above proportional control and the conventional proportional path using a resistor.



operating in saturation.



CM Logic
Ring
Oscillator

(a) (10 points) Find the frequency of oscillation ω_{osc} if $R = 1 \text{ k}\Omega$ and $C = 100 \text{ fF}$.

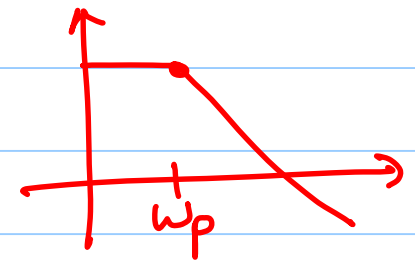
A_0

$$\frac{g_m R}{(1 + sRC)}$$

$$\omega_p = \frac{1}{RC}$$

loop gain

$$L(s) = \left(\frac{A_0}{1 + \frac{s}{\omega_p}} \right)^5, \quad \angle L(j\omega) = -5 \tan^{-1} \left(\frac{\omega}{\omega_p} \right)$$



To oscillate, $\angle L(j\omega_{osc}) = -180^\circ$ $\Rightarrow$ even phase-shift

$$5 \tan^{-1} \left(\frac{\omega_{osc}}{\omega_p} \right) = 180^\circ$$

$$\Rightarrow \frac{\omega_{osc}}{\omega_p} = \tan \left(\frac{180^\circ}{5} \right) = \tan(36^\circ) = 0.726$$

~~Small-signal
Analysis~~

$$\omega_{osc} = 0.726 \omega_p$$

$$= \frac{0.726}{RC} = 7.265 \text{ Grad/s}$$

$$\text{or } 1.156 \text{ GHz}$$

(b) (10 points) What is the minimum delay-cell transistor transconductance (g_{m1}) required for oscillation?

$$|L(\omega_{osc})| \geq 1$$

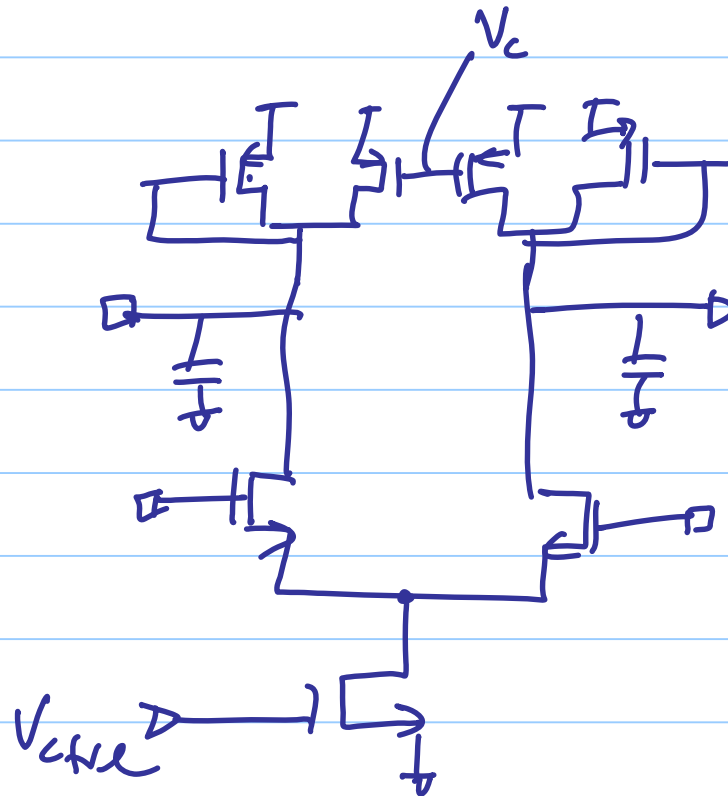
$$\left[\frac{g_{mR}}{\sqrt{1 + \left(\frac{\omega_{osc}}{\omega_p}\right)^2}} \right]^5 \geq 1$$

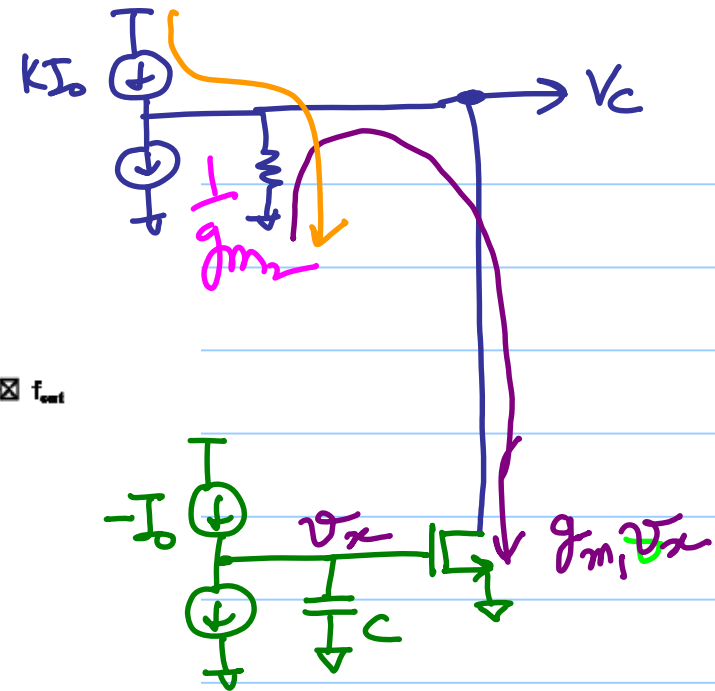
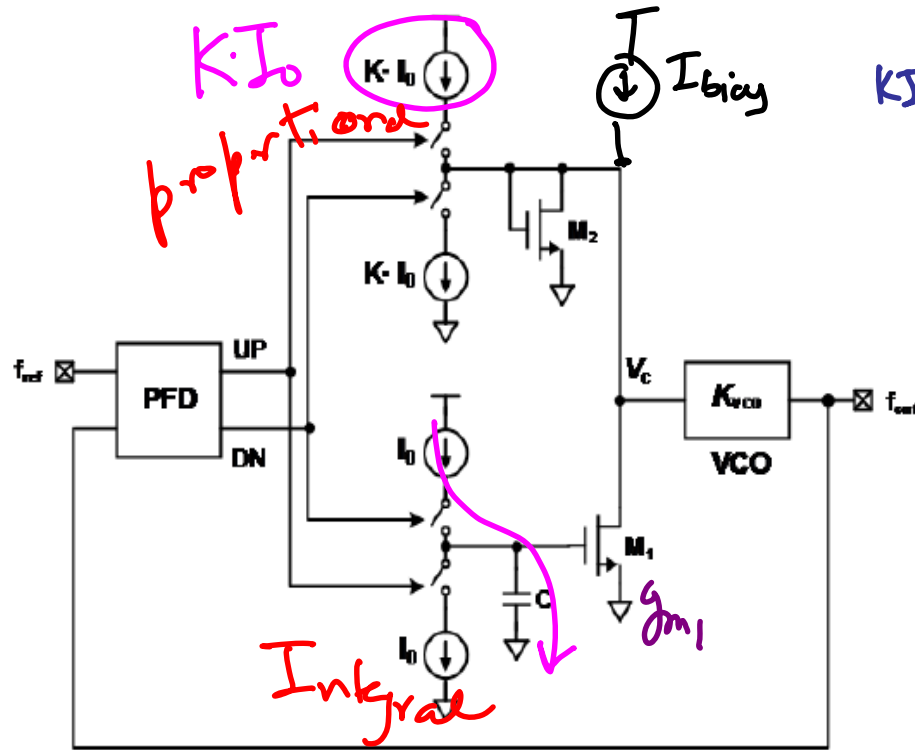
$$\Rightarrow \frac{g_{mR}}{\sqrt{1 + \tan^2(36^\circ)}} \geq 1$$

$$\Rightarrow g_{mR} \geq 1.236$$

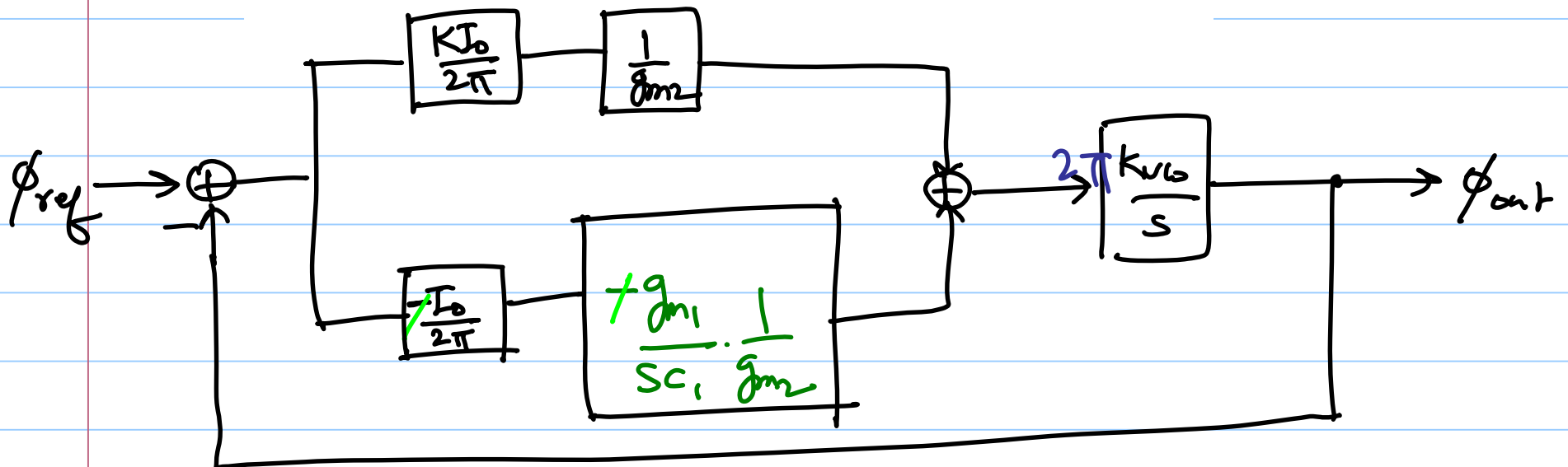
$$\Rightarrow \boxed{g_m \geq 1.236 \frac{\text{mA}}{\text{V}}}$$

- (c) (10 points) A 5-stage VCO needs to be designed based upon the above schematic.
Draw schematic of a delay cell to achieve this with best possible PSRR.





(a) (5 points) Draw the phase-domain *small-signal* block diagram in steady state.



(b) (5 points) What is the effective loop-filter transfer function, $F(s) = \frac{V_c(s)}{I_o}$?

$$\frac{V_c(s)}{I_o} = \frac{K}{g_{m2}} + \left(\frac{g_{m1}}{g_{m2}} \right) \cdot \frac{1}{sC}$$

(c) (5 points) Find the expression for loop gain $L(s)$ and determine the pole and zero locations.

$$L(s) = \frac{I_o K_{vco} K}{s^2 g_{m2}} \left(s + \frac{g_{m1}}{Kc} \right)$$

$$\omega_{p1} = \omega_{p2} = 0$$

$$\omega_z = - \frac{g_{m1}}{Kc}$$

LHP zero.

$$H_L(s) = \frac{L(s)}{1 + L(s)}$$

(e) (5 points) In order to minimize the loop filter area, should K be minimized or maximized? Why?

maximize $K \rightarrow$ minimize area

