

ECE 517 - Lecture 28

Note Title

4/27/2017

$\Delta\Sigma$ NTF Design $\rightarrow$ Tradeoffs $\rightarrow$ inband noise (IBN) vs OBG (stability)

* Maximum stable amplitude (MSA)

$\rightarrow$ max input amplitude for which the $\Delta\Sigma$ is stable

from heuristics:

$N_0 = 1\text{-bit}$ $OBG = 1.5$

$N_0 \sim 3\text{-}4\text{ bits}$ $OBG < 3.5$
or 3

MSA vs OBG

$\rightarrow$ Quantizer resolution (N_0)

$N_0 \uparrow \Rightarrow OBG \uparrow$

Specifications :

SQNR of 100dB
BW = 1MHz , $f_s < 200\text{MHz}$

Design parameters!

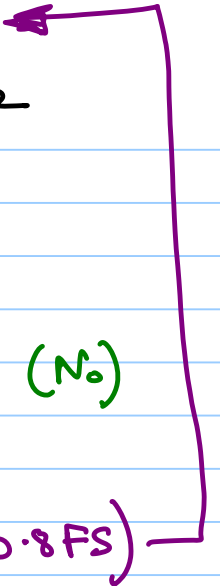


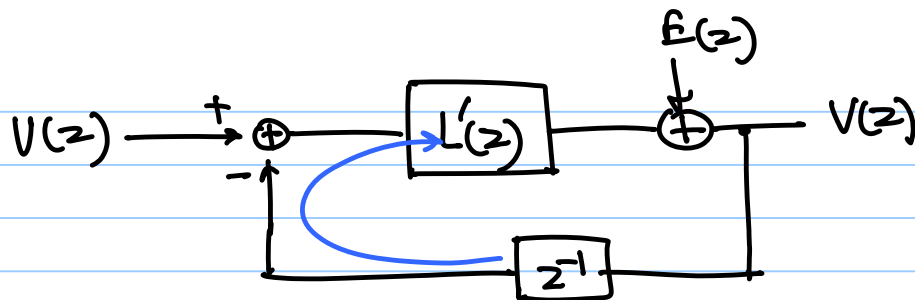
$$OSR \rightarrow f_s = 2 \cdot BW \cdot OSR$$

Order (n): 2-5 , Quantizer resolution (N_0)

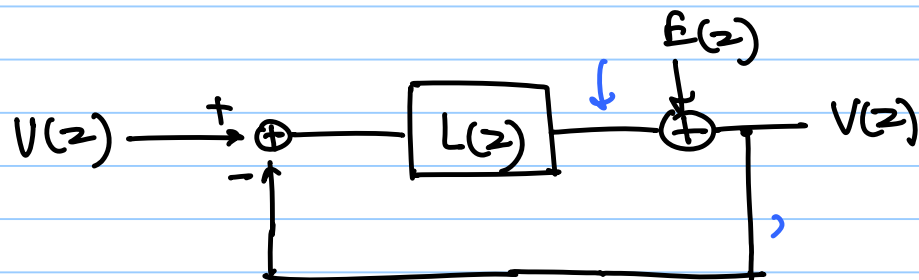
↳ $OBW < 3.5$

↳ $MSA = ?$ ($MSA > 0.8FS$)



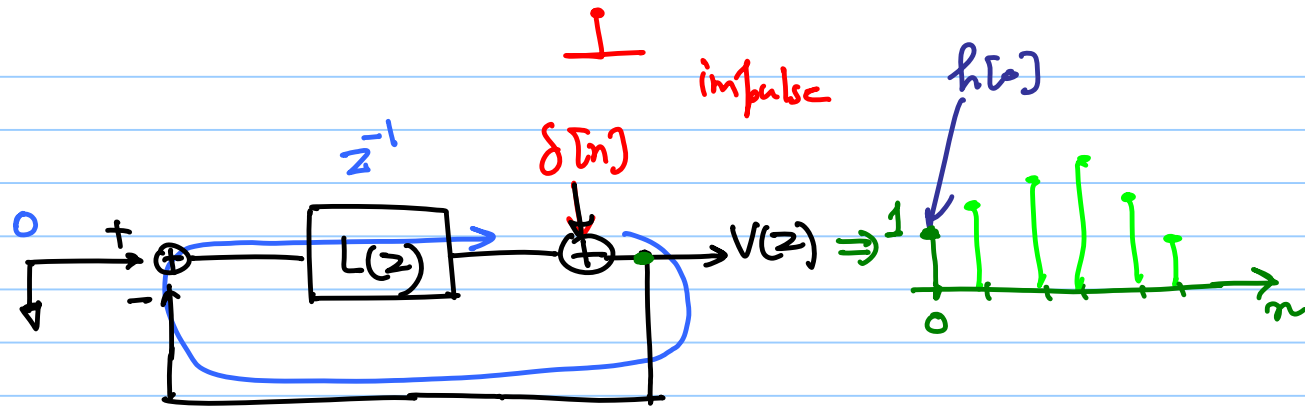


$$L(z) = \frac{z^1}{1-z^{-1}} \leftarrow \text{Delaying integrator}$$



$$L(z) = \frac{1}{1-z^{-1}}$$

* No delay free loops!



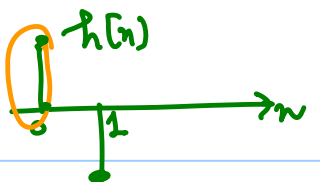
The first sample of the impulse response of the loop

$$h[0] \geq 1$$

"NTF realizability condition"

$$h(n) \xrightarrow{\neq} \text{NTF}(z)$$

$$NTF(z) = 1 - z^{-1}$$

$$h[n] = \{1, -1\}$$


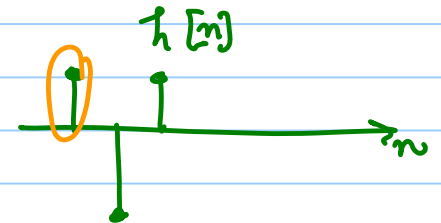
$$NTF(z) = \sum_{n=0}^{\infty} h[n] z^{-n} = 1 - z^{-1}$$

$$NTF(z) = (1 - z^{-1})^2$$

$$= 1 - 2z^{-1} + z^{-2}$$

$$h[n] = \{1, -2, 1\}$$

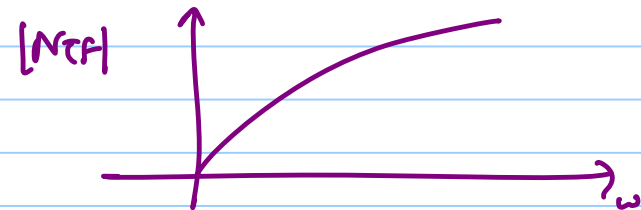
$$h[0] = \lim_{z \rightarrow \infty} NTF(z) = \lim_{z^{-1} \rightarrow 0} NTF(z) = 1$$



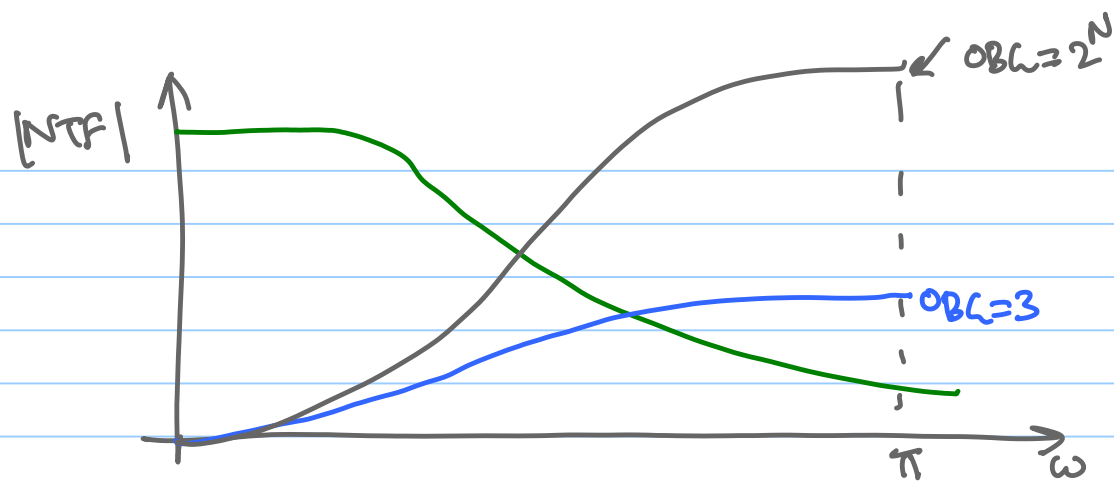
$$\sum_{n=0}^{\infty} h[n] \rightarrow \text{gain at DC}$$

$$e^{-j\pi} \Rightarrow -1$$

$$\sum_{n=0}^{\infty} |h[n]| \approx \text{gain at } \omega=\pi$$



High pass filter



$$NTF = \frac{(1-z^{-1})^N}{D(z)}$$

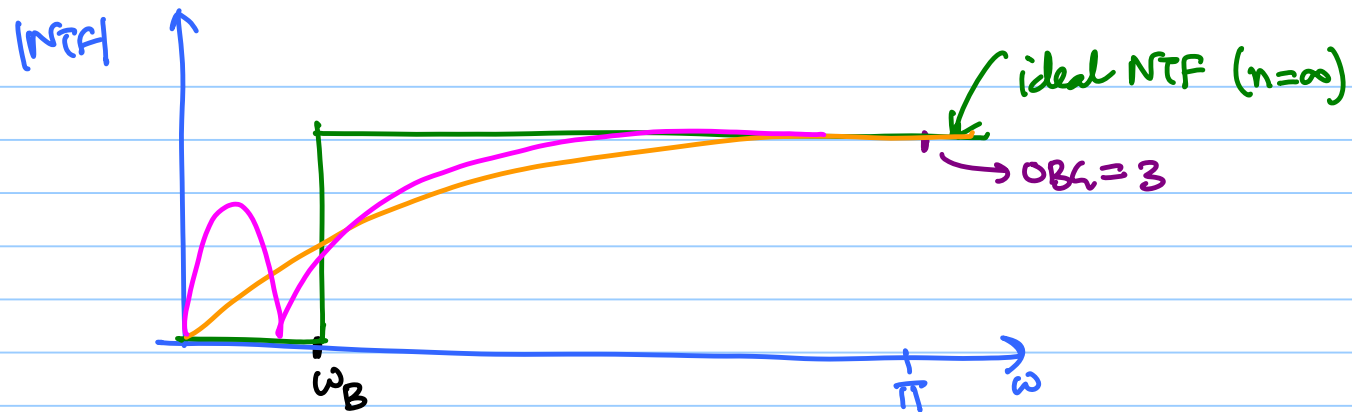
$$NTF(z) = \frac{(1-z^{-1})^4}{a_0 + a_1 z^{-1} + \dots + a_4 z^{-4}} = \frac{N(z)}{D(z)}$$

1 ←

$$h[0] = NTF(\infty) = 1$$

$$a_0 = 1$$

Approximation Problem

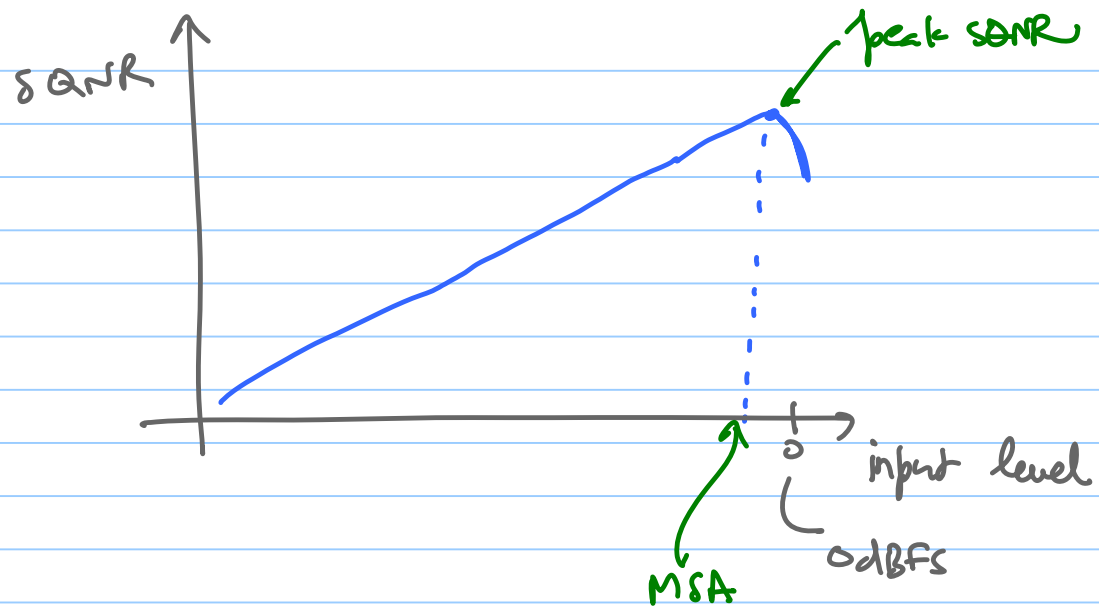


① Butterworth

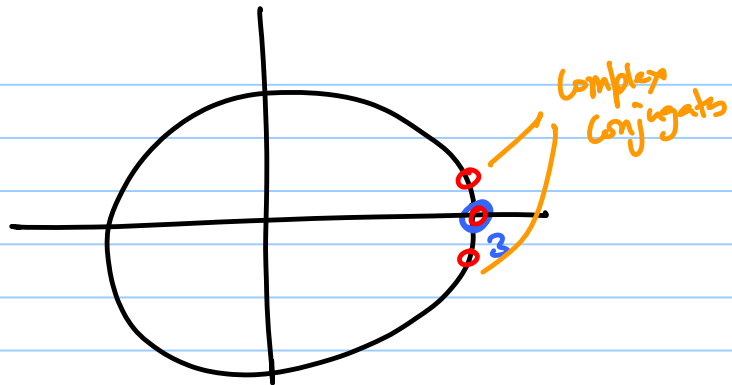
② Inverse Chebyshev

③ Maximally flat all poles

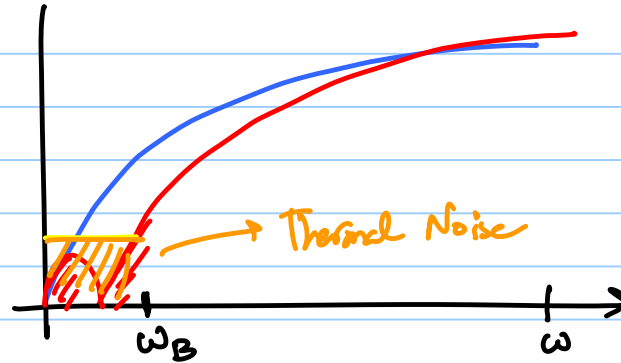
④ Elliptical



NTF-3rd optimization



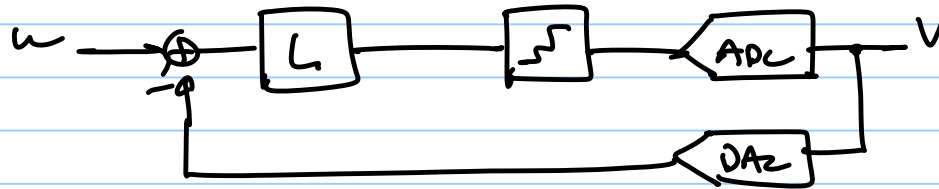
NTF



$$NTF(z) = \underline{\underline{(1-z^{-1})^3}}$$

spread the zeros around in the BW.

How to find MSA?

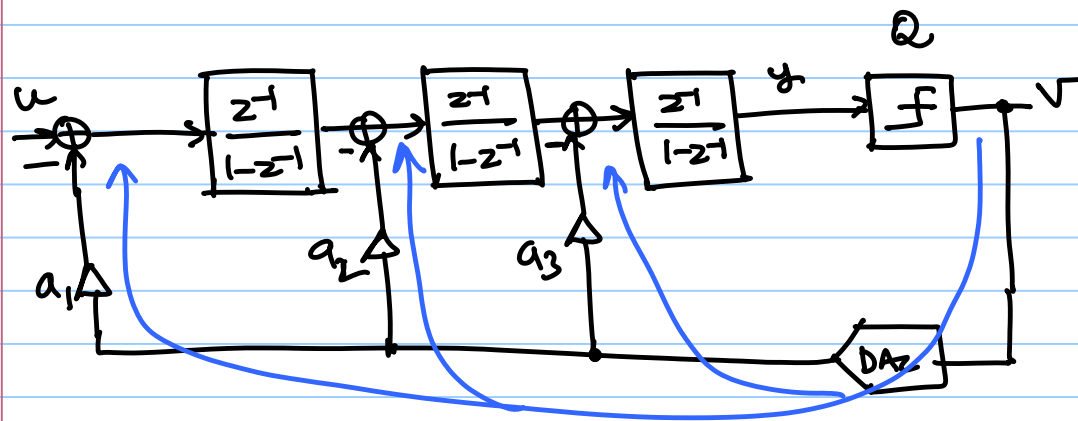


$\Delta\Sigma$ Loop Filter Architectures

- * feedback type
- * feedforward type

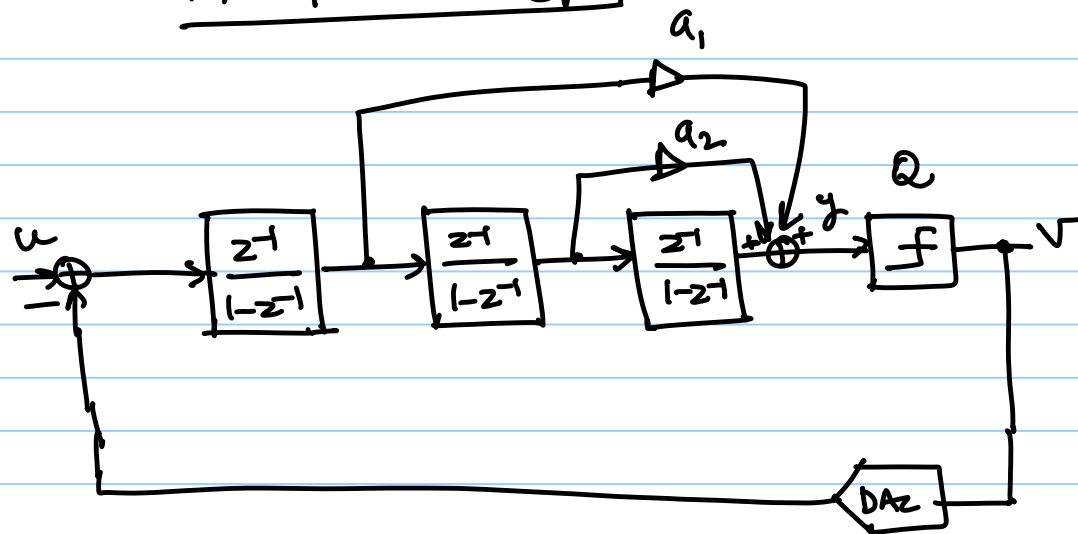
feedback.

CIFB in $\Delta\Sigma$ Toolbox



Cascade of Integrator with
distributed feedback

Feedforward Type



$\Delta\Sigma$ Toolbox $\rightarrow$ Clff

* Hybrid of FB & FF

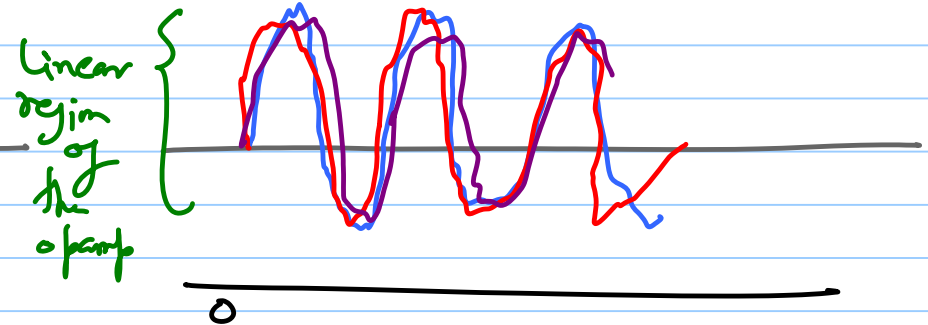
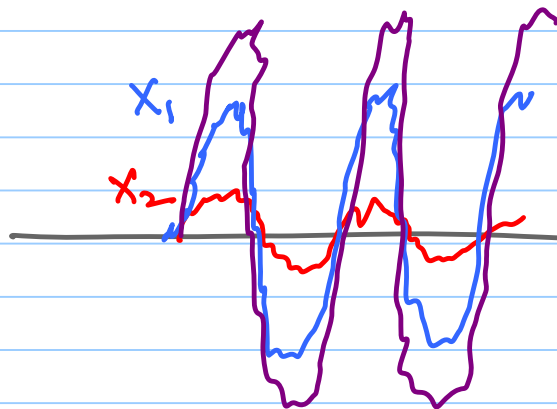
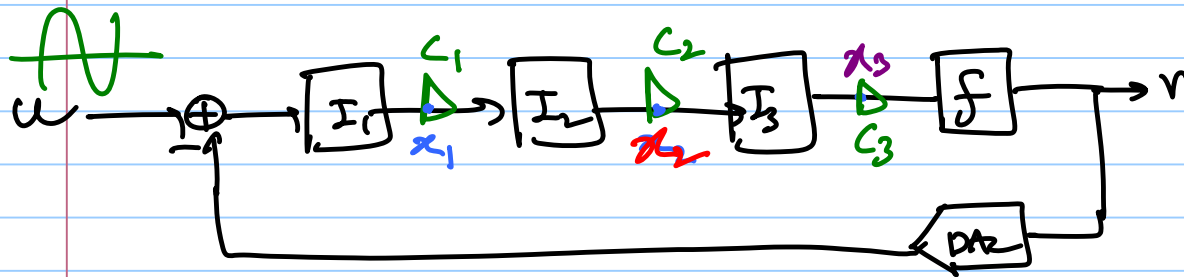
FF

vs

FB

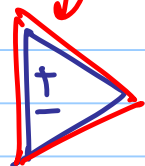
Dynamic Range Scaling

* All integrator output (states) should have similar swings

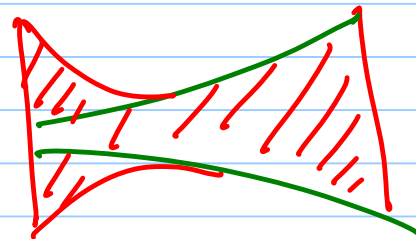
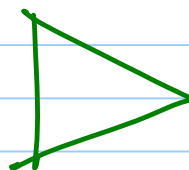
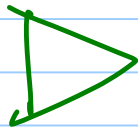
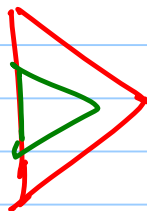


golden opamp for low noise & Distortion

1/f



1/f



↳ feedforward is better for Power Consumption

FR $\Rightarrow$ gain peaking $\downarrow$

