

# ECE 513 - Lecture 20

Tuesday, October 23, 2018 1:59 PM

## Part I: Active Device Matching

optimized  $W = W_f \cdot N_f$  to obtain a noise match i.e.  $\text{Re}\{Z_{\text{opt}}\} = Z_0 = 50\Omega$

## Part II: Passive Component Matching

\* Adding resistive component for matching degrades NF

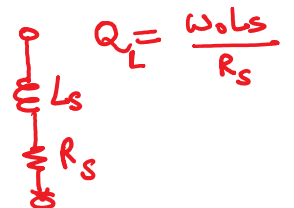
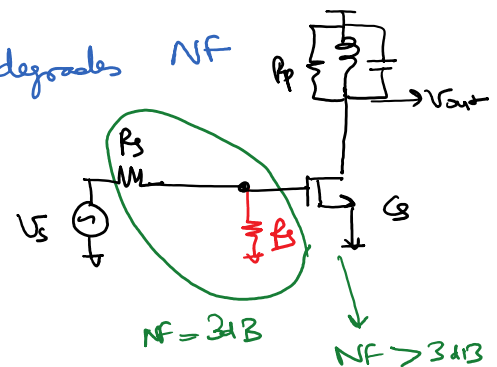
\* Purely reactive components do not add noise

↳ Ideal inductors, transformers, Transmission Lines (TL), and/or capacitors.

↳ These elements have loss resistance  $\Rightarrow$  finite Q

↳ Inductors occupy large area on chip

↳ In an LNB, inductors are more predominant.



## Design philosophy for Impedance Match:

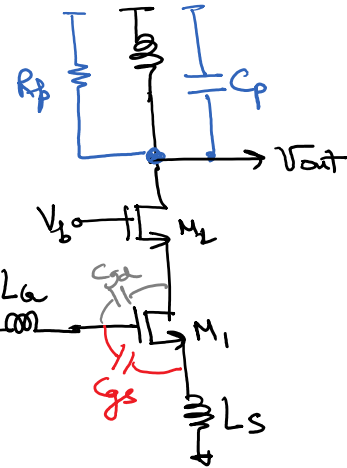
- \* Select LNA topology with the lowest number of transistors  
 ↳ avoid active loads or active inductors → degrade NF & linearity
- + Bias the transistors at  $J_{opt}$  of the topology ←  $NF = NF_{min}$   
 ↳ choose the optimal finger width  $W_f$  for least  $NF_{min}$
- \* Calculate the transistor size ( $n_f$ ) that corresponds to  $R_{s,PT} = Z_0$

### New part

- \* Add reactive (lossless) feedback to transform the real part of the input resistance ( $R_{in} = \text{Re}(Z_{in})$ ) to the desired value, i.e.  $Z_0$
- \* Add reactive matching to "tune out" the imaginary parts of the optimum noise impedance ( $Z_{opt}$ ) as well as the input impedance ( $Z_{in}$ )

# LNAs with Inductive Degeneration

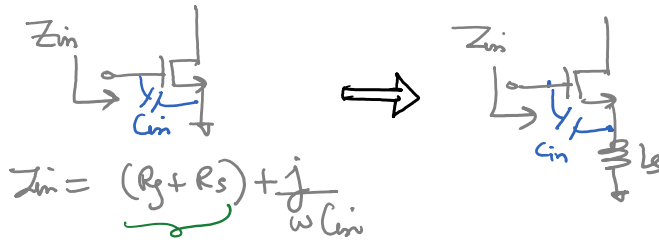
\* most widely used topology  $\rightarrow$  Cascode with inductive degeneration



\* lossless inductor  $L_s$  is a series-series feedback

$\rightarrow$  Doesn't alter the real part of transistor's  $Z_{opt}$  & overall  $N_{Fmin}$

(Analyzed in chapter 5)  
Series-series feedback



$$Z_{in} = (R_g + R_s) + j\omega C_{in}$$

$$Z_{in} = (R_g + R_s + \omega_T L_s) + j(\omega_0 L_s - \frac{1}{\omega_0 C_{in}} + \omega L_g)$$

$\Rightarrow Z_0$        $\Rightarrow 0 \text{ at } \omega = \omega_0$

use Cascode  $f_T$  not CS  $f_T$

$$L_s = \frac{Z_0 - R_g - R_s}{2\pi f_T}$$

Impedance Match  $\text{Re}\{Z_{in}\} = Z_0$

$$L_g \leq \frac{\omega_T}{\omega^2 g_{meff}} - L_s$$

cancel imaginary part of  $Z_{in}$

$$\therefore \omega_T = \frac{g_{meff}}{C_{in}}$$

$$\text{Im}\{Z_{in}\} = 0$$

$$\text{Re}\{Z_{sopt}\} = Z_0$$

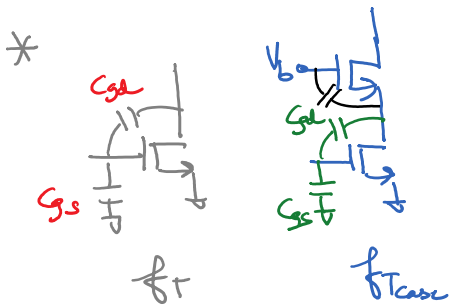
$$\text{Re}\{Z_{in}\} = Z_0$$

$$\text{Im}\{Z_{sopt}\} = 0 \quad ??$$

$$\text{Im}\{Z_{in}\} = 0$$

within 20% margin of error

Imaginary part of noise impedance  $Z_{sopt}$  is within 20% of  $\text{Im}\{Z_{in}\}$



\* Cascode device  $f_T < \text{CS device } f_T$

$$Z_o \approx \omega_T L_s \uparrow \text{Cascode } f_T$$

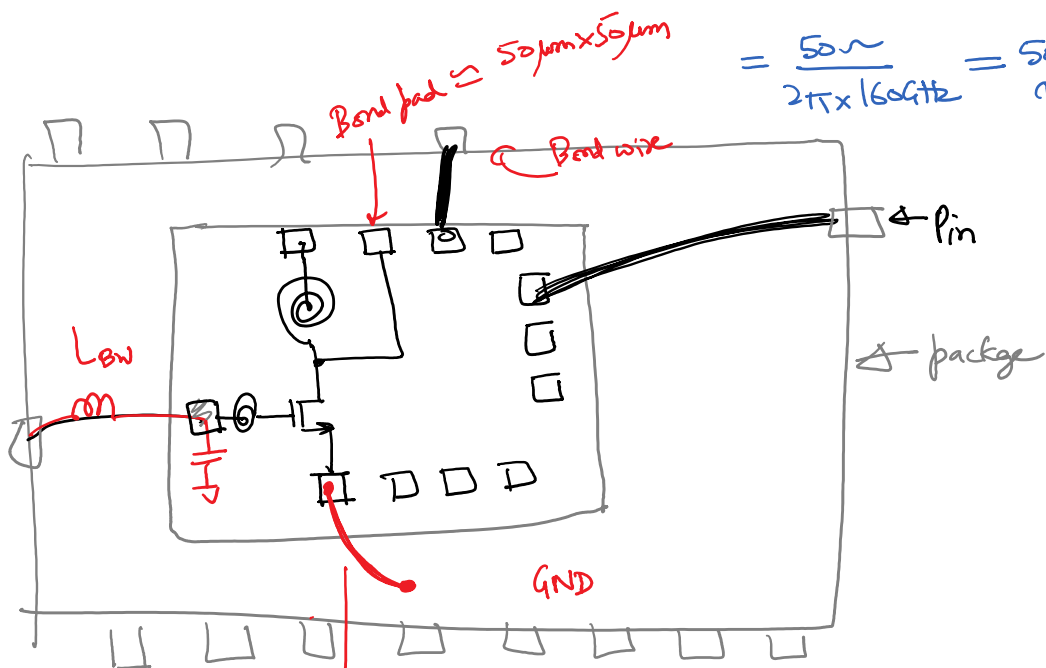
$$\omega_T \approx \frac{g_m}{C_{gs} + C_{gd}}$$

$$\omega_{T_{\text{cascode}}} = \frac{g_m}{C_{gs} + 2C_{gd}}$$

\*

$$\omega_T L_s = Z_o \Rightarrow L_s = \frac{Z_o}{\omega_T}$$

In 65nm CMOS,  $f_T = 160 \text{ GHz}$



$$= \frac{50 \text{ n}}{2\pi \times 160 \text{ GHz}} = 50 \text{ pF}$$

only depends on technology  
Not frequency of operation ( $\omega_o$ )

Down bond  $\Rightarrow 50 \text{ pF} \rightarrow 50 \text{ n}$  at the input

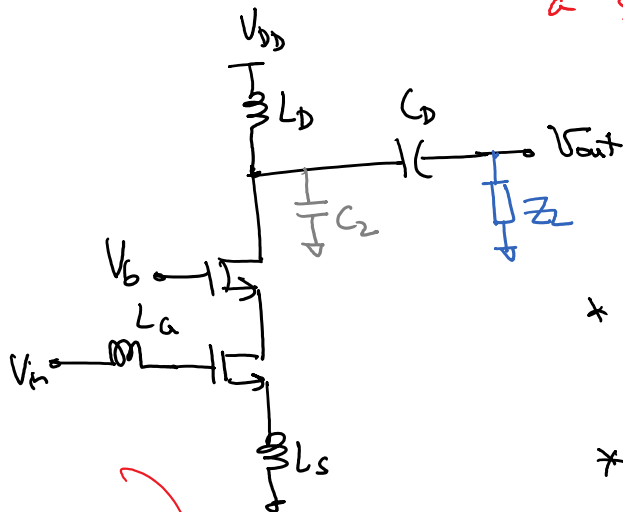
## Output Matching to Maximize Gain:

\* In an IC, the load of the LNA is provided by another gain stage, phase shifter (multiple Beamforming Receiver), or by a mixer.

\* Output of the LNA is capacitive

\* A simple narrowband matching network is realized using an L-section

→ shunt inductor  $L_D$  connected to  $V_{DD}$  followed by a series capacitor



$$Z_L = \frac{1}{j\omega C} = -jX_C \text{ or } \frac{1}{j\omega L} = jX_L$$

\*  $L_D$  forms a parallel resonant circuit with the output capacitances

\* Inductive load ( $L_D$ ) allow the output,  $V_{out}$ , to swing above the supply voltage ( $V_{DD}$ )

→ improves linearity compared to the case with resistive load.

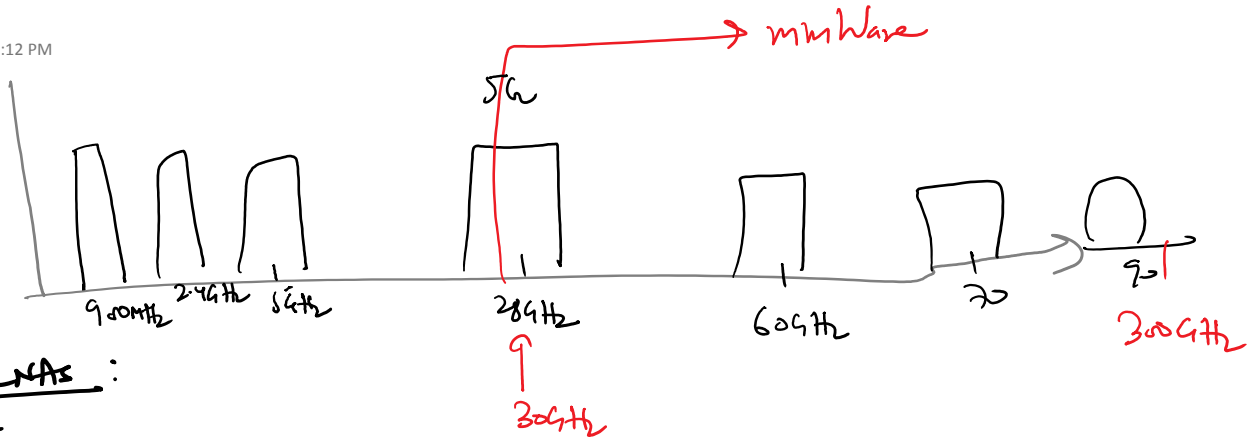
\* Broadband o/p match  $\Rightarrow$   $\pi$ -match or other matching networks

$$R_L = \frac{R_p}{Q^2 + 1}$$

$$\Rightarrow Q = \frac{R_p}{\omega L_D}$$

→ At resonance, the input and outputs are matched to  $50\Omega$  and  $Z_L$  respectively.

lower gain,  $g \leq \frac{1}{4} \left( \frac{f_1}{f_0} \right)^2 \frac{R_p}{Z_0}$



mmWave LNAs:

