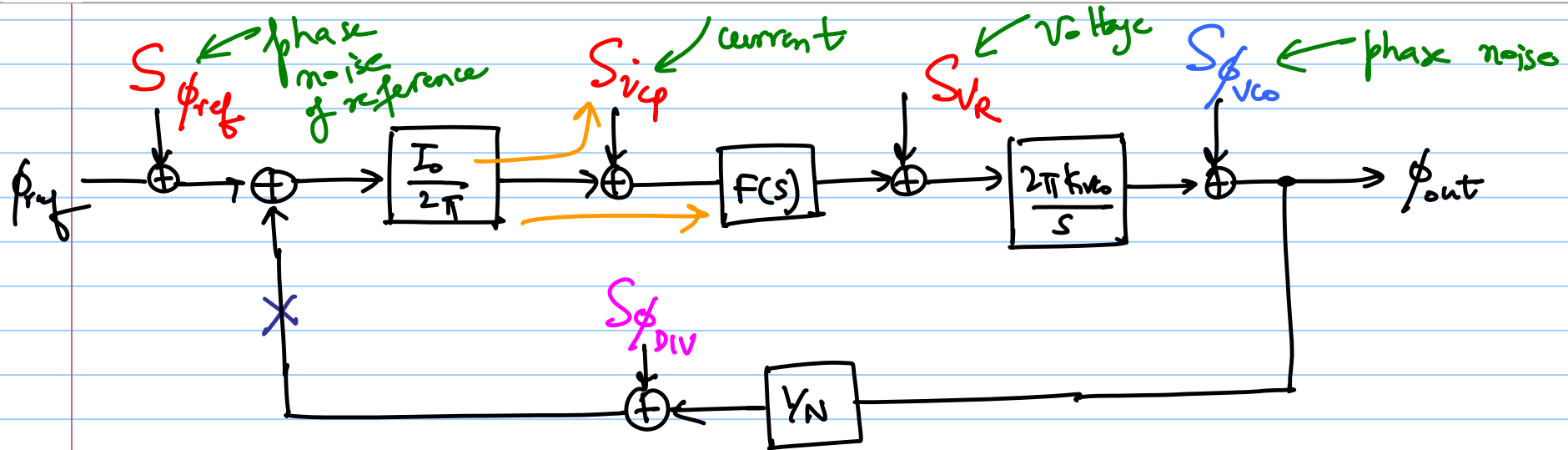


ECE 504 - Lecture 21

Note Title

11/7/2016



loop gain $L(s) = \frac{I_0 k_{vco}}{N} \cdot \frac{F(s)}{s}$

Noise Transfer Function

$$NTF_{ref}(s) = \frac{\phi_{out}(s)}{\phi_{ref}(s)} = \frac{N \cdot L(s)}{1 + L(s)}$$

low-pass response

$$NTF_{div}(s) = NTF_{ref}(s)$$

$$NTF_{cp}(s) = \frac{\phi_{out}(s)}{i_{cp}(s)} = \frac{NTF_{ref}(s)}{I_{cp}/2\pi} = \frac{2\pi}{I_{cp}} \cdot NTF_{ref}(s)$$

$$I_{cp} = I_o$$

low-pass

NTF_{ref} divided by cl gain

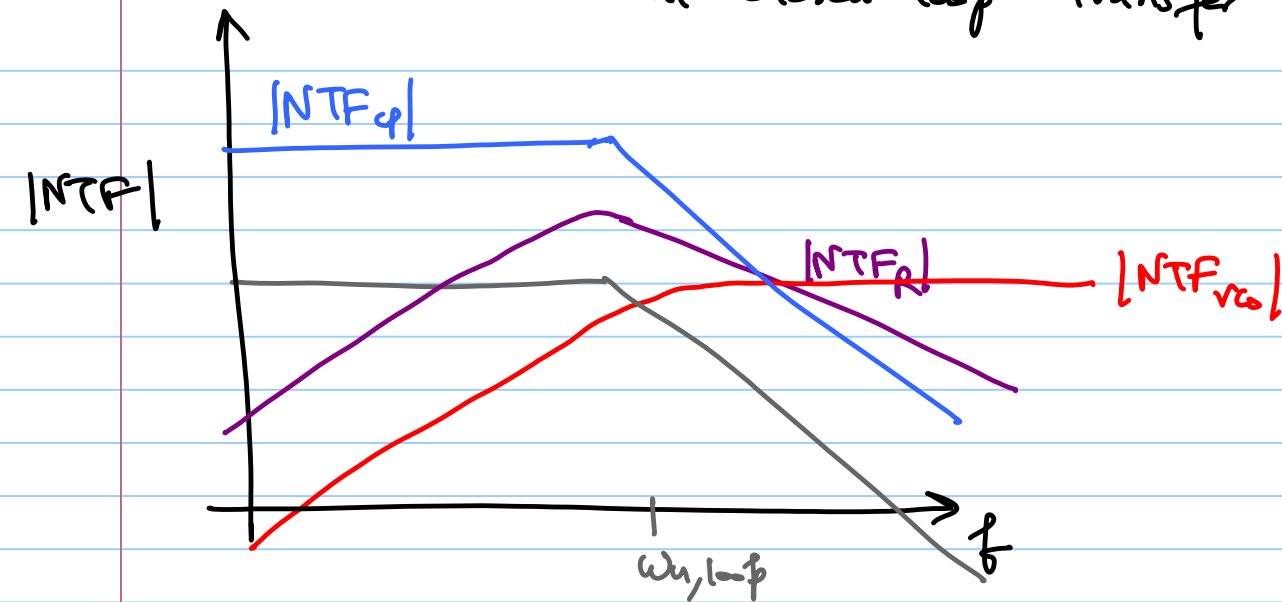
$$NTF_R(s) = \frac{\phi_{out}(s)}{v_R(s)} = \frac{\frac{2\pi K_{vco}}{s}}{1 + L(s)}$$

same σ^2 as NTF_{ref}
Band pass Response

$$NTF_{vco}(s) = \frac{\phi_{out}(s)}{\phi_{vco}(s)} = \frac{1}{1 + L(s)}$$

High-pass Response

All closed-loop Transfer functions

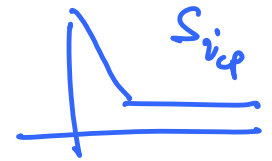
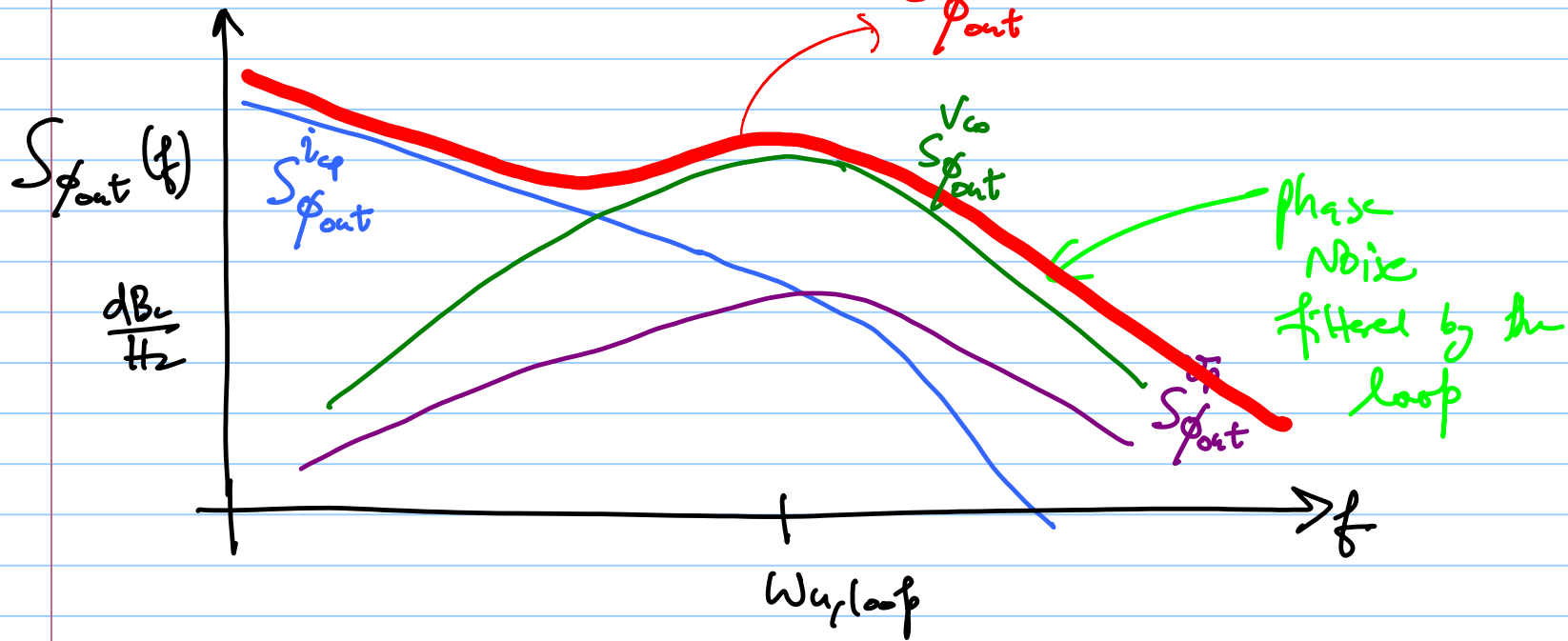


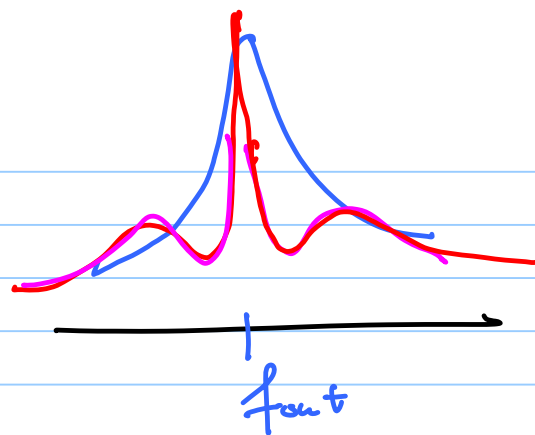
Output Phase Noise Contribution

$$S_{\phi_{out}}^{\phi_{ref}} = S_{\phi_{ref}} |NTF_{ref}(j\omega)|^2$$

$$S_{\phi_{out}}^{Total} = S_{\phi_{out}}^{\phi_{ref}} + S_{\phi_{out}}^{i_{eq}} + S_{\phi_{out}}^{V_R} + S_{\phi_{out}}^{\phi_{vco}} + S_{\phi_{out}}^{DIV}$$

S-shaped curve $S_{\phi_{out}}^{Total}$





Calculating Jitter from Phase Noise

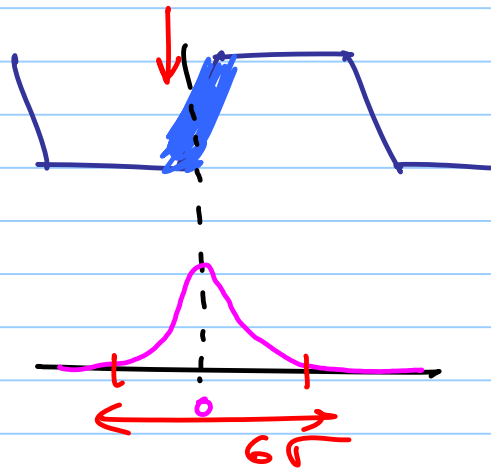
$$\text{Total phase Noise} = \sigma_{\Delta\phi}^2 = \int_0^{\infty} S_{\phi_{\text{out}}}^{\text{Total}}(f) \cdot df$$

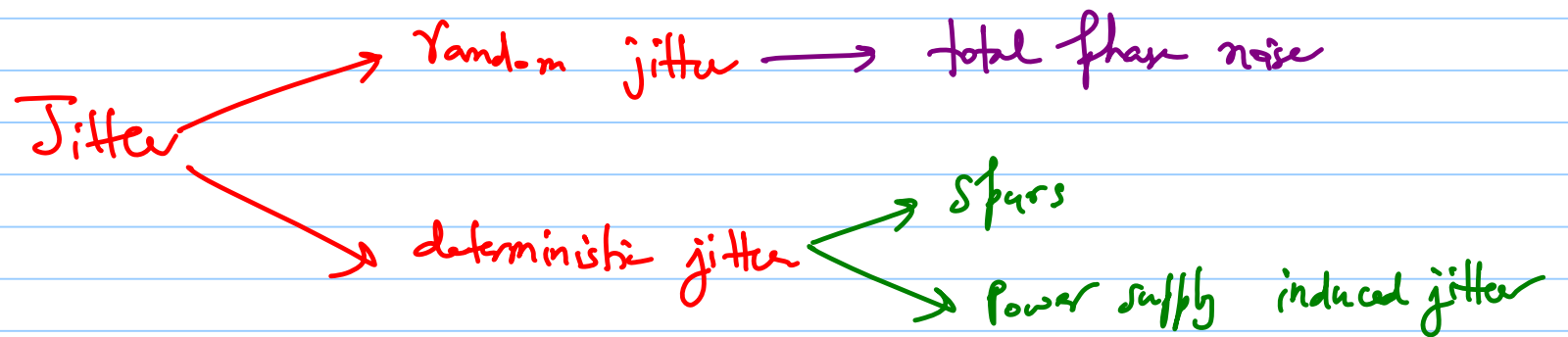
Variance of phase Noise (also the phase noise power)
↳ (in radians)

Jitter : $\sigma_{\Delta T} = \sqrt{\int_0^{\infty} S_{\phi_{\text{out}}}^{\text{Total}}(f) df} \times \frac{T_{VCO}}{2\pi}, \text{ (sec)}$
Standard deviation

* In MATLAB trapz function for discrete integration

Jitter is usually represented as δt or $\delta \tau$





PLL Noise Optimization

- ① Start with $\omega_{y,loop} < \frac{\omega_{ref}}{10}$
- ② Find loop parameters (K_{vco} , I_{cp} , R , C_1 & C_2)
- ③ Estimate the PSD of all noise sources ($\hat{S}_{\phi_{out}}^i$)
- ④ Find total output phase noise $\hat{S}_{\phi_{out}}^{Total} \rightarrow \sigma_{jitter}$
- ⑤ If total phase noise doesn't meet the spec
↳ adjust BW and/or lower noise
- ⑥ If the spec is met, reduce power

$$S_{VR} \propto K_{VO} \cdot R^2$$

