

ECE 310 - Lecture 4

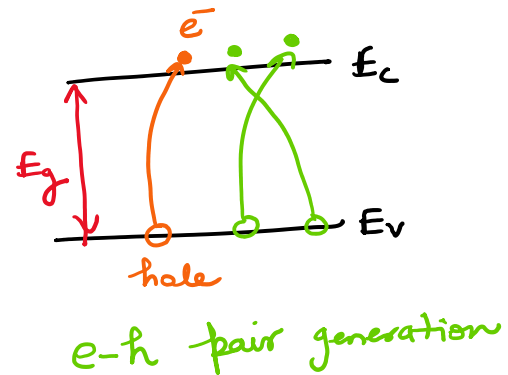
Tuesday, January 16, 2018 11:26 PM

- intrinsic \rightarrow pristine semiconductor
- extrinsic \rightarrow with impurities (dopants)

In equilibrium in intrinsic SC

$$n = p = n_i \leftarrow \text{intrinsic carrier density}$$

\uparrow # of free electrons cm^{-3} \uparrow # of holes cm^{-3}



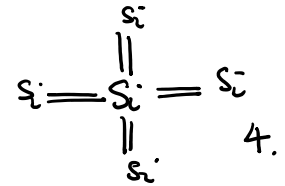
In "Equilibrium"

- \hookrightarrow no external potential (voltage)
- \hookrightarrow no external light on the sample
- \hookrightarrow no thermal gradient

$$np = n_i^2$$

Derived from device physics
Important!

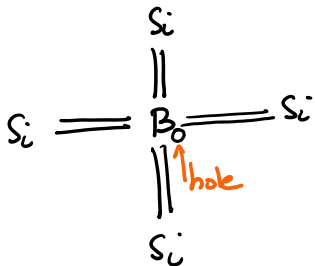
Modification of Carrier densities :



III

B → Boron ⇒ 3 e⁻ in outer shell

Acceptor type dopant
(or impurity)



N_A ← doping concentration
atoms/cm³

$$N_A \gg n_i$$

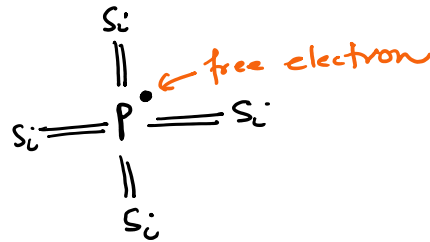
$$\Rightarrow p = N_A$$

$$n = \frac{n_i^2}{p} = \frac{n_i^2}{N_A}$$

V

P ← Phosphorus ⇒ 5 electrons in the outer shell

Donor type Dopant



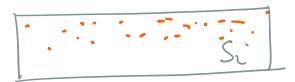
N_D ← atoms/cm³

$$N_D \gg n_i$$

$$n \approx N_D$$

$$p = \frac{n_i^2}{n} = \frac{n_i^2}{N_D}$$

p Dopants



× ion implantation
× annealing
dopants are activated
↳ they form part
of the Si lattice

$$np = n_i^2$$

Extrinsic Semiconductor in Equilibrium

Acceptor

$$\begin{aligned} p &\approx N_A \\ n &\approx \frac{n_i^2}{N_A} \end{aligned}$$

$n, p = n_i$ $\xRightarrow{\text{Doping}}$ $p = N_A$
 $n = \frac{n_i^2}{N_A}$

more holes \Rightarrow p-type semiconductor
 p-Si

hole is the majority carrier
 electron is the minority carrier

Donor

$$\begin{aligned} n &\approx N_D \\ p &\approx \frac{n_i^2}{N_D} \end{aligned}$$

$$np = n_i^2$$

$n, p = n_i$ $\xRightarrow{\text{Doping}}$ $n = N_D$
 $p = \frac{n_i^2}{N_D}$

more electrons \Rightarrow n-type s/c
 n-Si

e^- is the majority carrier
 hole is the minority carrier

Q. How can $n_p = n_i^2$ be maintained if we introduce dopants?

$n \cdot p = n_i^2$
 $N_D \gg n_i^2$ (indicated by a red arrow from 'n')

'p' must fall below n_i (indicated by a green arrow from 'p')
 ↳ this occurs because many of the new dopants "recombine" with the holes

Ex. $n_i = 1.08 \times 10^{10} \text{ cm}^{-3}$
 Donor-type dopants $N_D = 10^{16} \text{ cm}^{-3}$

$$n \approx N_D = \underline{10^{16}} \text{ cm}^{-3} \gg n_i$$

$$p = \frac{n_i^2}{N_D} = \frac{(1.08 \times 10^{10})^2}{10^{16}} = 1.17 \times 10^4 \text{ cm}^{-3} \ll n_i$$

electrons → 'majority carrier'
 holes → 'minority carrier'

$$N_D, N_A \approx \underline{10^5 - 10^{18}} \text{ cm}^{-3}$$

$10^{20} \text{ cm}^{-3} \ll$ degenerate doping

Transport of Carriers

↓

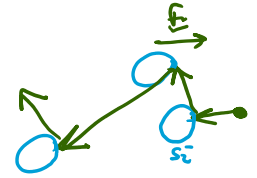
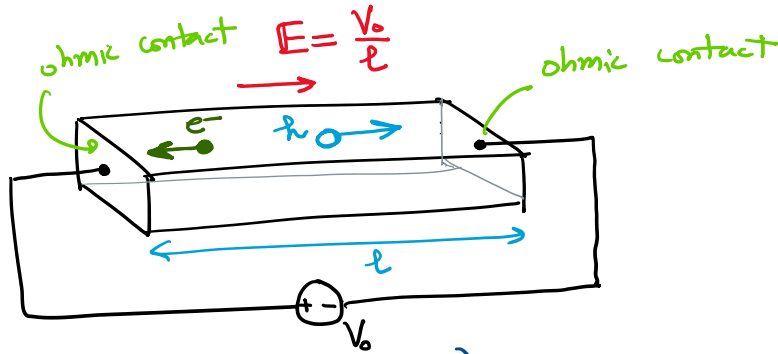
mechanism of movement of carriers in the semiconductor

{ electron
hole

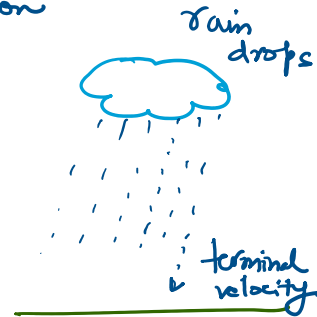
Two type of transport mechanisms

- ① Drift
- ② Diffusion

Drift



electrons accelerate due to field 'E' in opposite direction
 ↳ collide with Si atoms
 ↳ attain drift velocity (terminal velocity)



Drift velocity

$$v \propto E$$

$$v = \mu E$$

mobility of carriers $\Rightarrow \frac{\text{cm}^2}{\text{V.s}}$

$$\mu = \frac{v}{E} \text{ in the semiconductor}$$

Ex.

electron $\Rightarrow \mu_n = 1350 \cdot \frac{\text{cm}^2}{\text{V.s}}$ $\leftarrow \text{e mobility}$

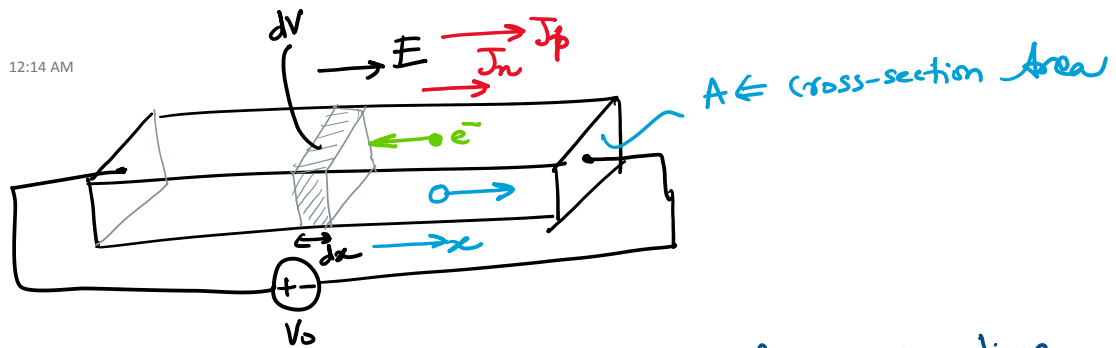
hole $\Rightarrow \mu_p = 480 \cdot \frac{\text{cm}^2}{\text{V.s}}$ $\leftarrow \text{hole mobility}$

\leftarrow hole mobility is lower than the e^- mobility!

\Rightarrow from semiconductor physics
 \Rightarrow holes have "higher effective mass"

↳ are in the valence band
 \Rightarrow held tighter by the atom

We can see that for Si:
 $\mu_n \approx 3\mu_p$



Electron current $\Rightarrow I_n = \text{charge flow per unit time}$
 $= (n \cdot q) \cdot (dV \text{ in unit time})$
 $= qn \cdot A \cdot \left(\frac{dx}{dt}\right)$
 \swarrow drift velocity

$$dV = A \cdot dx$$

$$\frac{dV}{dt} = A \cdot \frac{dx}{dt}$$

$$I_n = qnA v_n$$

\swarrow electron
 \swarrow drift velocity

$$q = 1.6 \times 10^{-19} \text{ C}$$

n

Current density \Rightarrow

$$J_n = \frac{I_n}{A} = qn v_n$$

$$\rightarrow J_n = qn \mu_n E$$

$$v_n = \mu_n E$$

Similarly for holes

$$J_p = qp \mu_p E$$

Total current density \Rightarrow

$$J_{\text{tot}} = J_n + J_p = q(\eta \mu_n + p \mu_p) E$$

\swarrow total current density
 \swarrow e^- current density
 \swarrow hole current density

'Read chapter 2'