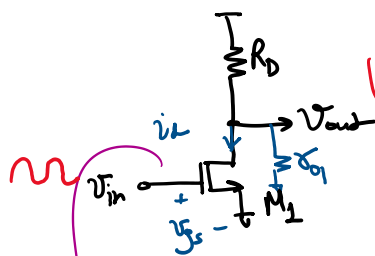


ECE 310 - Lecture 23

Friday, March 9, 2018

10:32 AM

Common Source Amplifiers



Biased is understood
(Bias networks are not shown)

$$i_d = g_m V_{gs} = g_m V_{in}$$

$$V_{out} = -i_d (R_D || r_{o1})$$

$$= -g_m V_{in} (R_D || r_{o1})$$

$$\Rightarrow A_v = \frac{V_{out}}{V_{in}} = -g_m (R_D || r_{o1})$$

$$\text{Small signal voltage gain} = -g_m R_D \quad \text{if } r_{o1} \gg R_D$$

output is inverted (180° phase shift)

CS \Rightarrow inverting amplifier

$$A_v = -g_m R_D$$

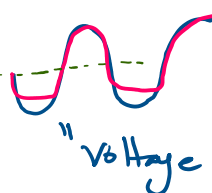
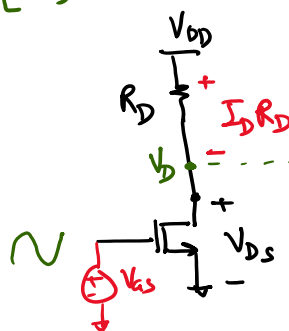
$$g_m = \sqrt{2 k_n \frac{W}{L} I_D}$$

$$A_v \uparrow \Rightarrow R_D \uparrow$$

$$I_D \uparrow$$

$$I_D R_D \uparrow \Rightarrow V_{DS} \downarrow$$

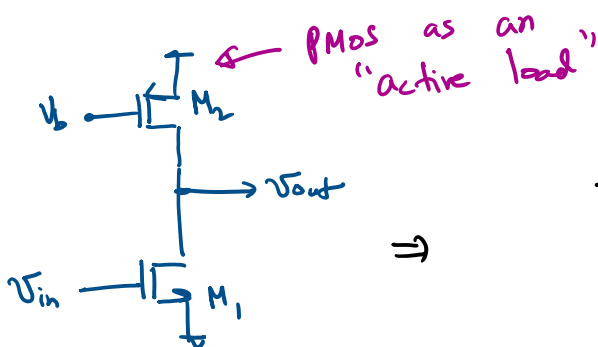
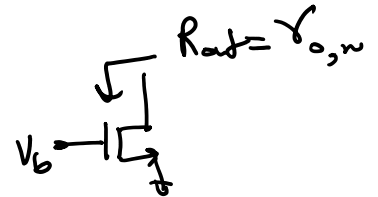
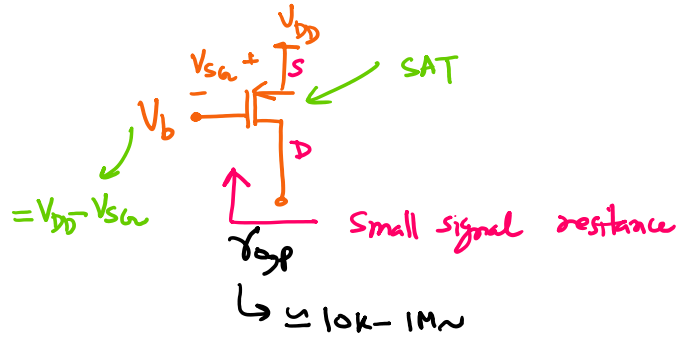
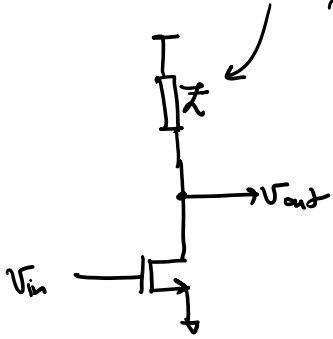
$$V_{DS} < V_{DS,sat} \leftarrow M_1 \text{ will Tnode}$$



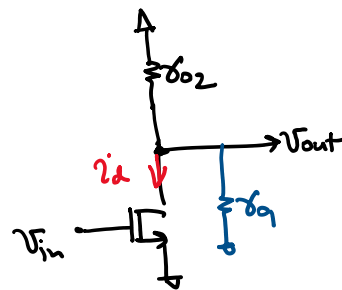
"voltage headroom"

\Rightarrow should get amplification without trioding M_1

need high- \mathcal{Z} load without dropping much voltage across it.



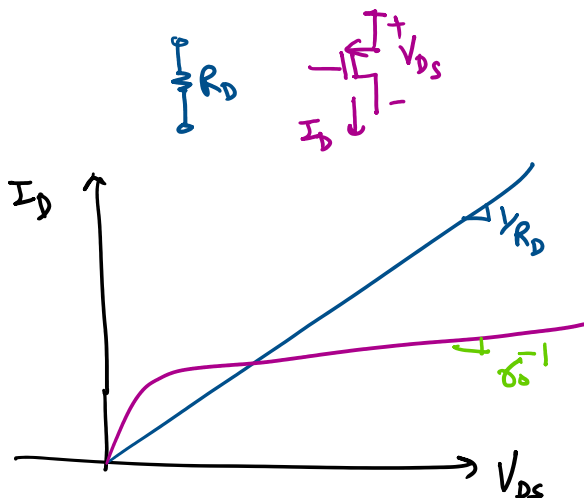
AC picture



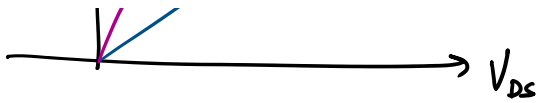
$$V_{out} = -i_d \cdot (r_{o1} \parallel r_{o2})$$

$$= -g_{m1} V_{in} (r_{o1} \parallel r_{o2})$$

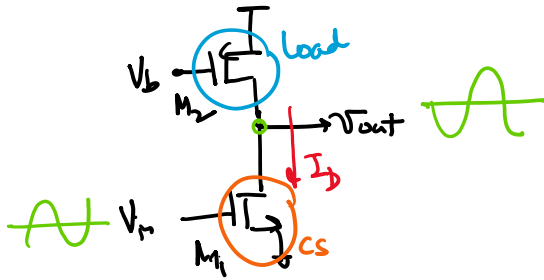
$$A_v = -g_{m1} (r_{o1} \parallel r_{o2})$$



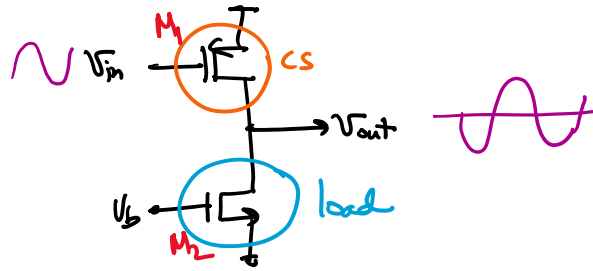
Very large gain without incurring a large V_{SD} across M_2



$$P = V_{DD} \times I_D$$

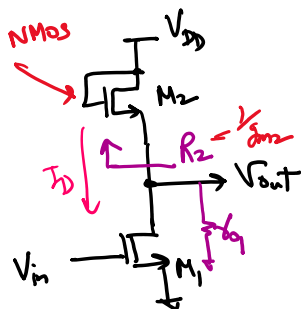


$$A_v = -g_m (r_{o1} || r_{o2})$$



$$A_v = -g_m (r_{o1} || r_{o2})$$

* Do Book Examples
17. 14, 15, 16 & 17



$$A_v = -g_{m1} \left(r_{o1} \parallel \frac{1}{g_{m2}} \right)$$

$$\hookrightarrow -\frac{g_{m1}}{g_{m2}} \Leftarrow \text{gain} = (2-5)$$

$$= -\frac{\sqrt{2\beta_1 I_{D1}}}{\sqrt{2\beta_2 I_{D2}}}$$

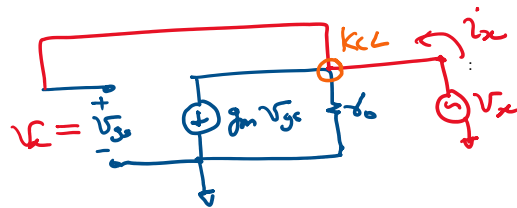
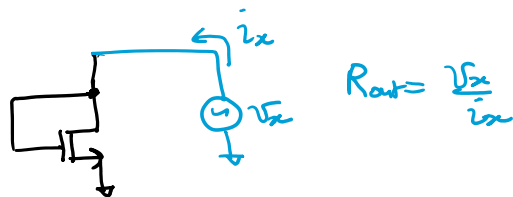
$$\beta_n = K_p n \frac{W}{L}$$

$$= -\sqrt{\frac{(W/L)_1}{(W/L)_2}}$$

$$= -\sqrt{\frac{W_1}{W_2}}$$

(+) max precise (linear) gain
than $g_{m1} r_{o1}$

(-) gain is much lower



$$KCL \Rightarrow i_x - \frac{v_x}{r_o} - g_m v_x = 0$$

$$i_x = v_x \left(\frac{1}{r_o} + g_m \right)$$

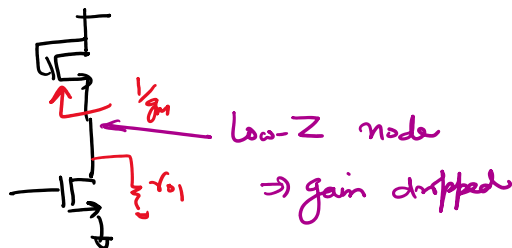
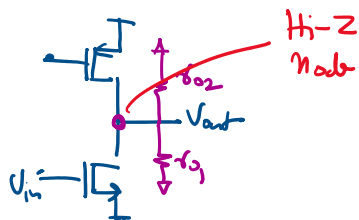
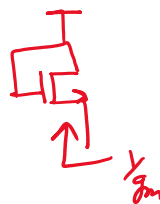
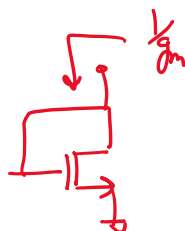
$$\Rightarrow R_{out} = \frac{v_x}{i_x} = \frac{1}{g_m + \frac{1}{r_o}} = \frac{r_o}{1 + g_m r_o}$$

$$= \frac{r_o \cdot \frac{1}{g_m}}{\frac{1}{g_m} + r_o}$$

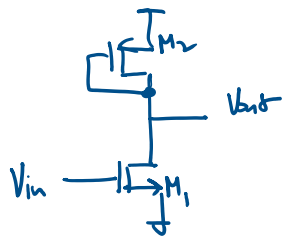
$$= \frac{1}{g_m} \parallel r_o$$

if $r_o \gg \frac{1}{g_m}$
or $g_m r_o \gg 1$

$$R_{out} \approx \frac{1}{g_m}$$



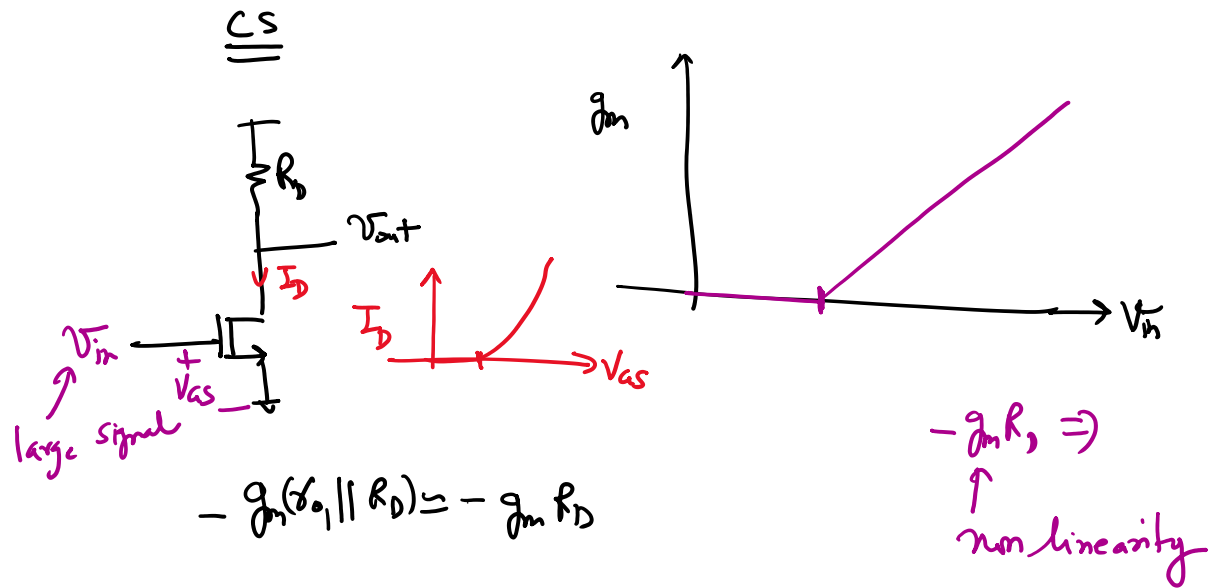
for higher gain \Rightarrow high output impedance.



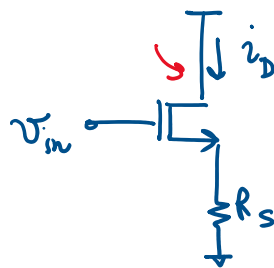
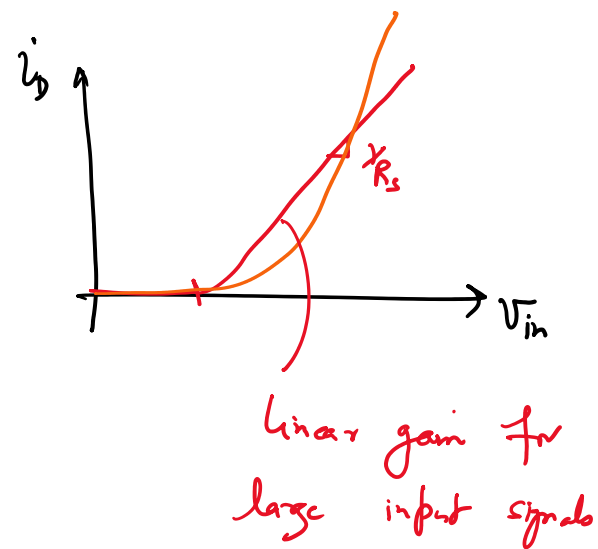
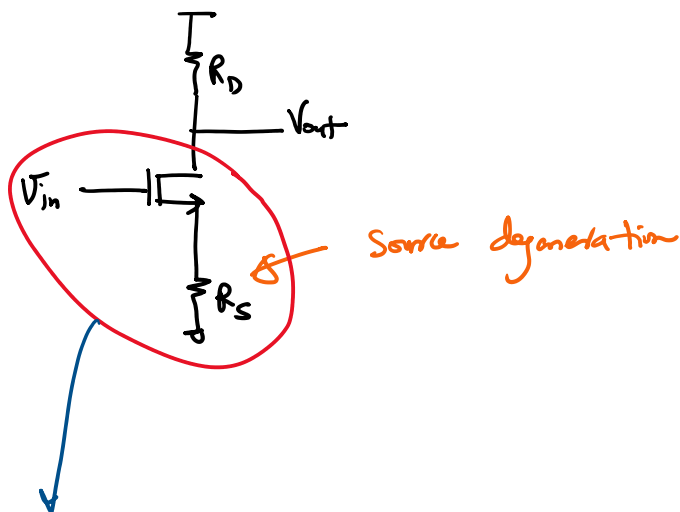
$$A_v \approx - \frac{g_{m1}}{g_{m2}} \quad \leftarrow \text{for } \omega \gg \frac{1}{g_m}$$

$$A_v = - g_{m1} \cdot \left(r_{o1} \parallel \frac{1}{g_{m2}} \right) \parallel r_{o2}$$

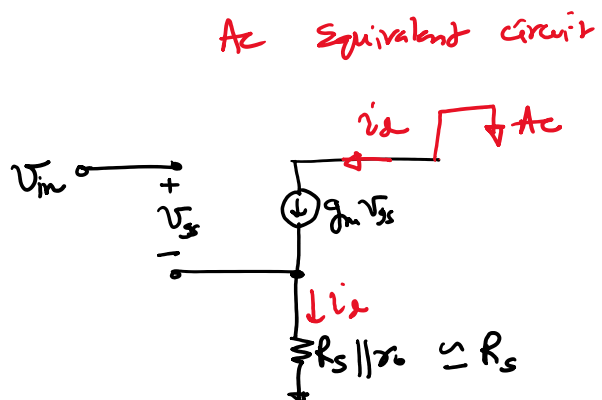
↑ precise



Add R_S to the source



\Rightarrow

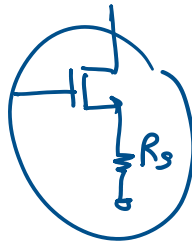


$$V_{in} = V_{gs} + v_a R_s$$

$$= \frac{i_a}{g_m} + v_a R_s$$

$$\Rightarrow v_a \left(\frac{1}{g_m} + R_s \right) = V_{in}$$

$$\Rightarrow v_a = \underbrace{\frac{g_m}{1 + g_m R_s}}_{g_m} V_{in}$$



$$g_m = \frac{g_m}{1 + g_m R_s}$$