

# ELEG 309 Formula Sheet

## Final Exam

May 21, 2000

$$\text{Voltage gain } (A_v) = \frac{v_o}{v_I}, \quad \text{in dB} \quad 20 \log |A_v| \quad (1)$$

$$\text{Current gain } (A_i) = \frac{i_o}{i_I}, \quad \text{in dB} \quad 20 \log |A_i| \quad (2)$$

$$\text{Power gain } (A_p) = \frac{P_L}{P_I}, \quad \text{in dB} \quad 10 \log |A_p| \quad (3)$$

$$A_v = \left. \frac{dv_o}{dv_I} \right|_{\text{at Q}} \quad (4)$$

$$A_{vo} = \left. \frac{v_o}{v_i} \right|_{i_o=0} (V/V), \quad A_{is} = \left. \frac{i_o}{i_i} \right|_{v_o=0} (A/A) \quad (5)$$

$$G_m = \left. \frac{i_o}{v_i} \right|_{v_o=0} (A/V), \quad R_m = \left. \frac{v_o}{i_i} \right|_{i_o=0} (V/A) \quad (6)$$

$$T(\omega) = \frac{V_o(\omega)}{V_i(\omega)}, \quad T(s) = \frac{V_o(s)}{V_i(s)} \quad (7)$$

$$\frac{K}{1 + (s/\omega_0)}, \quad \frac{Ks}{s + \omega_0}, \quad s = j\omega \quad (8)$$

$$y(t) = Y_\infty - (Y_\infty - Y_{0+})e^{-t/\tau} \quad (9)$$

$$\frac{v_O}{v_I} = -\frac{R_2}{R_1}, \quad \frac{v_O}{v_I} = \frac{-R_2/R_1}{1 + (1 + R_2/R_1)/A} \quad (10)$$

$$\frac{V_o(s)}{V_i(s)} = -\frac{Z_2(s)}{Z_1(s)} \quad (11)$$

$$v_O(t) = -\frac{1}{CR} \int_0^t v_I(t') dt' - V_C \quad (12)$$

$$\frac{V_o(s)}{V_i(s)} = -\frac{1}{sCR} \quad (13)$$

$$v_O(t) = -CR \frac{dv_I(t)}{dt} \quad (14)$$

$$\frac{V_o(s)}{V_i(s)} = -sCR \quad (15)$$

$$\frac{v_O}{v_I} = 1 + \frac{R_2}{R_1}, \quad \frac{v_O}{v_I} = \frac{1 + (R_2/R_1)}{1 + [1 + (R_2/R_1)]/A} \quad (16)$$

$$A(s) = \frac{A_0}{1 + s/\omega_b}, \quad \omega_t = A_0 \omega_b, \quad A(s) \simeq \frac{\omega_t}{s} \quad (17)$$

$$I_B = \frac{I_{B1} + I_{B2}}{2}, \quad I_{OS} = |I_{B1} - I_{B2}| \quad (18)$$

$$i = I_S(e^{v/nV_T} - 1) \simeq I_S e^{v/nV_T}, \quad V_T = \frac{kT}{q} \quad (19)$$

$$V_2 - V_1 = 2.3 nV_T \log \frac{I_2}{I_1} \quad (20)$$

$$n_i^2 = BT^3 e^{-E_G/kT} \quad (21)$$

$$J_p = -qD_p \frac{dp}{dx}, \quad J_n = qD_n \frac{dn}{dx} \quad (22)$$

$$v_{drift} = \mu_p E, \quad \frac{D_n}{\mu_n} = \frac{D_p}{\mu_p} = V_T \quad (23)$$

$$n_{n0} \simeq N_D, \quad p_{p0} \simeq N_A, \quad n_{n0} p_{n0} = n_i^2 = n_{p0} p_{p0} \quad (24)$$

$$V_0 = V_T \ln \left( \frac{N_A N_D}{n_i^2} \right) \quad (25)$$

$$r_d = \frac{nV_T}{I_D} \quad (26)$$

$$i_C = I_S e^{v_{BE}/V_T} \quad (27)$$

$$i_C = \beta i_B = \alpha i_E, \quad i_E = (\beta + 1)i_B \quad (28)$$

$$i_E = i_B + i_C \quad (29)$$

$$\alpha = \frac{\beta}{\beta + 1}, \quad \beta = \frac{\alpha}{1 - \alpha} \quad (30)$$

$$i_c = g_m v_\pi, \quad V_T \simeq 25 \text{ mV} \quad (31)$$

$$g_m = \left. \frac{\partial i_C}{\partial v_{BE}} \right|_{i_C=I_C} \quad (32)$$

$$r_\pi = \frac{v_{be}}{i_b} = \frac{\beta}{g_m}, \quad r_e = \frac{v_{be}}{i_e} = \frac{\alpha}{g_m}, \quad r_\pi = (\beta + 1)r_e \quad (33)$$

$$g_m = \frac{I_C}{V_T}, \quad r_e = \frac{V_T}{I_E}, \quad r_\pi = \frac{V_T}{I_B}, \quad r_o = \frac{V_A}{I_C} \quad (34)$$

$$\frac{v_o}{v_b} = -\frac{\alpha R_C}{r_e + R_e} \quad (35)$$

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}} \quad (36)$$

$$\epsilon_{ox} = 3.97\epsilon_o = 3.5 \times 10^{-13}\text{F/cm} \quad (37)$$

$$\mu_n = 580\text{cm}^2/\text{Vs} \quad (38)$$

$$k'_n = \mu_n C_{ox} \quad (39)$$

$$i_D = k'_n \frac{W}{L} \left[ (v_{GS} - V_t) v_{DS} - \frac{1}{2} v_{DS}^2 \right] \quad (40)$$

$$i_D = \frac{1}{2} k'_n \frac{W}{L} (v_{GS} - V_t)^2 (1 + \lambda v_{DS}) \quad (41)$$

$$\frac{V_{A1}}{V_{A2}} = \frac{L_1}{L_2} \quad (42)$$

$$r_o = \frac{V_A}{I_D} \quad (43)$$

$$V_t = V_{t0} + \gamma \left[ \sqrt{2\phi_f + V_{SB}} - \sqrt{2\phi_f} \right] \quad (44)$$

$$\gamma = \frac{\sqrt{2qN_A\epsilon_s}}{C_{ox}} \quad (45)$$

$$g_m = \left. \frac{\partial i_D}{\partial v_{GS}} \right|_{v_{GS}=V_{GS}} \quad (46)$$

$$g_m = \sqrt{2k'_n \frac{W}{L} I_D} \quad (47)$$

$$\chi = \frac{\partial V_t}{\partial V_{SB}} \quad (48)$$

$$A_v = \frac{v_o}{v_i} \quad (49)$$

$$A_v = -\frac{\sqrt{2k'_n \left(\frac{W}{L}\right)_1}}{\frac{1}{|V_{A1}|} + \frac{1}{|V_{A2}|}} \frac{1}{\sqrt{I_{REF}}} \quad (50)$$

$$A_v = \left( g_{m1} + g_{mb1} + \frac{1}{r_{o1}} \right) (r_{o1} || r_{o2}) \quad (51)$$

$$i_i = (g_{m1} + g_{mb1}) v_i + \frac{v_i - v_o}{r_{o1}} \quad (52)$$

$$A_v = \frac{g_{m1}}{g_{m1} + g_{mb1} + \frac{1}{r_{o1}} + \frac{1}{r_{o2}} + \frac{1}{R_L}} \quad (53)$$

$$R_o = (1/g_{m1}) || (1/g_{mb1}) || r_{o1} || r_{o2} \quad (54)$$

$$A_v = -\sqrt{\frac{(W/L)_1}{(W/L)_2}} \quad (55)$$

$$t_{PHL} = \frac{2C}{k'_n (W/L)_n (V_{DD} - V_t)} \times \left[ \frac{V_t}{V_{DD} - V_t} + \frac{1}{2} \ln \left( \frac{3V_{DD} - 4V_t}{V_{DD}} \right) \right] \quad (56)$$

$$t_{PHL} = \frac{1.6C}{k'_n (W/L)_n V_{DD}} \quad (57)$$

$$g_{mb} = \chi g_m \quad (58)$$

$$g_m = k'(W/L)(V_{GS} - V_t) \quad (59)$$

$$g_m = \frac{2I_D}{V_{GS} - V_t} \quad (60)$$

$$\lambda = 1/V_A \quad (61)$$

$$f_{3dB} = \frac{f_t}{1 + R_2/R_1} \quad (62)$$

$$\text{SR} = \frac{dv_O}{dt} \quad (63)$$

$$\omega_M v_{omax} = \text{SR} \quad (64)$$