# Efficient Packet Marking for Large-Scale IP Traceback

Michael T. Goodrich\* Department of Info. & Computer Science University of California Irvine, CA 92697-3425 goodrich@acm.org

# ABSTRACT

We present a new approach to IP traceback based on the probabilistic packet marking paradigm. Our approach, which we call *randomize-and-link*, uses large checksum *cords* to "link" message fragments in a way that is highly scalable, for the checksums serve both as associative addresses and data integrity verifiers. The main advantage of these checksum cords is that they spread the addresses of possible router messages across a spectrum that is too large for the attacker to easily create messages that collide with legitimate messages. Our methods therefore scale to attack trees containing hundreds of routers and do not require that a victim know the topology of the attack tree *a priori*. In addition, by utilizing authenticated dictionaries in a novel way, our methods do not require routers sign any setup messages individually.

Categories and Subject Descriptors: C.2.2 [Computer-Communication Networks]: Network Protocols. General Terms: Algorithms, Management, Security. Keywords: denial-of-service, traceback, packet marking.

## 1. INTRODUCTION

Internet denial-of-service (DOS) attacks are a serious problem. Recent analysis, by Moore *et al.* [13], shows that there are an average of at least 4,000 denial-ofservice attacks per week on the Internet. Moreover, their analysis showed that 50% of attacks have an intensity of at least 1,000 packets per second, that 25% have an intensity of at least 5,000 packets per second, and that some attacks have intensities in excess of 500,000 packets per second. Most attacks last at least 10 minutes, 10% last more than an hour, and 2% last at least 5 hours (some even last days). The volume of packets received in a DOS attack is, by its very nature, overwhelming. For example, in a 10-minute attack at 5,000 packetsper-second, a DOS victim will receive 3 million packets.

CCS'02, November 18-22, 2002, Washington, DC, USA.

Copyright 2002 ACM 1-58113-612-9/02/0011 ...\$5.00.

Moore *et al.* note that even DOS-hardened firewalls can be disabled at packet rates in excess of 14,000 packetsper-second. Simply put, there is little existing deterrent against DOS attacks and prevention of DOS attacks is not foolproof. Therefore, we desire ways of tracing DOS attacks back to their source(s), so as to employ packetblocking and law-enforcement techniques against them.

## **1.1 Modeling the Problem**

One of the insidious aspects of a denial-of-service attack is that it uses the strength of routers-to move packets quickly—against the victim. This aspect of DOS attacks is especially troubling in the case of a distributed denial-of-service (DDOS) attack, where many different hosts are compromised and used as "zombies" to fire packets at the victim. In this case, the attack packets proceed to the victim not in a single path, but through a tree. Thus, in order to model DDOS attacks, we consider the attack as propagating in a tree T, where the root of the tree T is the victim, V, each internal node in T corresponds to a router X on the Internet, and each leaf in T is a (possibly compromised) attack host. Thus, T is a subtree of the Internet, where we are modeling only the inflow of packets to V. In fact, from the perspective of V, the tree T is a subtree of a much larger universal tree U that consists of the union of all routes to V in the Internet. For any internal node X in T, other than the root, we therefore sometimes refer to the parent of X as X's downstream neighbor. Likewise, the children of a node X in T are sometimes called X's upstream neighbors. Our goal in the traceback problem is to identify the internal nodes<sup>1</sup> of the tree T. That is, we wish to identify the internal nodes in the universal tree U that correspond to routers unwittingly serving in the attack tree T to send attack packets to the victim V. In addition, we specifically want to exclude from T any routers that are not part of the attack. Moreover, so as to traceback large-scale distributed denial-of-service attacks, we desire solutions that allow for efficient traceback even if T contains hundreds of routers.

<sup>\*</sup>This work was support by DARPA grant F30602-00-2-0509 and NSF grant PHY-9980044.

Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. To copy otherwise, to republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee.

<sup>&</sup>lt;sup>1</sup>One could also consider the version where we also identify the leaves of T, but identifying internal nodes is simpler and sufficient—since ISPs control routers whereas administration of hosts is not consolidated. Therefore, we focus on the problem of identifying internal nodes in T.

We model the attacker as an adversary, A, who can compromise hundreds of hosts and use them as "zombies" in a DDOS attack. We allow that A may have knowledge about our traceback algorithms, and that he can even try to design his DDOS attack so as to confuse, break, or delay our algorithms. In so doing, A can make it difficult for us to identify some of the routers in the attack tree T. Specifically, if he succeeds in having us miss a router in T, then we say that we have made a false-negative identification. In addition, we allow that A may know the IP addresses of routers in the Internet; hence, he can try to trick us so as to implicate routers not in T. If we therefore identify a router X as belonging to the attack tree T, when X is in fact not in T, then we say that we have made a *false positive* identification. Clearly, we desire algorithms that minimize the number of false-negative and false-positive identifications.

A major challenge in the IP traceback problem is that there are approximately 200 million hosts on the Internet (e.g., see www.netsizer.com); hence, the universal tree U for a potential victim V has 200 million leaves. Conservatively assuming that there is a router for every 200 hosts on the Internet, we therefore estimate the number of routers (internal nodes) in U to be at least one million. Thus, in practical terms, solving the IP traceback problem amounts to correctly identifying a few hundred of the million internal nodes in U as belonging to the attack tree T. Ideally, we would like to do this identification without requiring any *a priori* knowledge of the universal tree U on the part of the victim V, for such information could be difficult to obtain and maintain.

Finally, we desire solutions to the IP traceback problem that are fast and efficient. We prefer solutions that minimize the amount of additional traffic on the Internet needed to solve the traceback problem or create an infrastructure for solving it. Likewise, we want to allow for incremental adoption by routers in any new infrastructure needed for traceback, and we want to minimize the amount of state that must be maintained by routers. In addition, the computations needed on the part of the victim to reconstruct the attack tree T should be fast enough so that V can quickly reconstruct T. The main objective of a DOS attack is to consume resources, so our solutions to the IP traceback problem should themselves not contribute to that goal.

## **1.2 Previous Related Work**

There are several existing approaches to the IP traceback problem (e.g., see Baba and Matsuda [3], Park and Lee [16], or Savage *et al.* [19]). We review some related approaches below.

Pattern-based Filtering and Hop-by-hop Tracing. In some cases, such as in reflector-based DDOS attacks [17], we can use patterns in the attack packets to filter out DDOS packets at a firewall. Likewise, the approach of hop-by-hop tracing, which is also known as link testing, uses a pattern-based approach to do traceback of a DOS attack while it is in progress. This is the approach of the automated Pushback mechanism [10], for example, and it is the solution currently supported manually by many router manufacturers. In this approach, a network administrator or his/her agent logs into the routers nearest the victim, and using statistics and pattern analysis, determines the next upstream routers in the attack tree T. The approach is then repeated at the upstream routers for as long as the attack continues. This scheme therefore requires immediate action during the attack, and requires considerable coordination between network administrators (to either communicate directly or setup access points for the agents of partnering administrators). This technique also requires some pattern-based way to separate legitimate packets from attack packets. A similar approach is used by Burch and Cheswick [5] to perform traceback by iteratively flooding from V portions of the Internet to see its effects on V's incoming traffic. Unfortunately, because of their iterative nature, these approaches have limited traceback capabilities in a large-scale DDOS. In addition, they have limited forensic appeal, since they can only be used while the attack is occurring.

ICMP Messaging. An alternative approach, based on ICMP messaging [4], is to have each router X decide, with some probability q (typically, q = 1/20000 is mentioned), for each packet P to send an additional ICMP packet to the destination, which identifies X and some content of P. The main idea of this approach is that during a DDOS, a sufficient amount of attack packets will trigger ICMP messages from the routers in the attack tree T so that the victim can reconstruct T from these messages. The main drawback of this approach is that it causes additional network traffic even when no DDOS is present. Even so, it is not efficient, for identifying all the n internal nodes in the attack tree T requires, according to the analysis of the coupon collectors problem (e.g., see Motwani and Raghavan [14]), an expected number of  $nH_n/dq$  packets to arrive at the victim, where  $H_n$  is the n-th Harmonic number and d is the average depth of T. For example, if d = 20 and n = 1000, then the expected number of attack packets needing to arrive at the victim V before V will have sufficient information to reconstruct T is 7.5 million.

Logging. In addition to the hop-by-hop and ICMP messaging approaches, several researchers have advocated a logging approach to the IP traceback problem. In a logging solution, we either ask routers to log the packets they process or we augment the data packets themselves to contain a full log of all the routers they have encountered on their way to their destinations [18]. Stone [22] and Baba and Matsuda [3] advocate logging of packet information at the routers, and Snoeren et al. [20] propose the logging of message digests of packets at the routers. With any of these solutions, a victim queries routers or their storage agents to see whether they sent suspect attack packets. The drawback with these approaches is that they require additional storage at the routers. They also require a way of publishing the data stored at routers in a timely manner (which itself could become a performance bottleneck or DOS vulnerability).

Probabilistic Packet Marking. An intriguing alternative solution to the IP traceback problem is probabilis*tic packet marking.* This traceback approach, which we follow in this paper, can be applied during or after an attack, and it does not require any additional network traffic, router storage, or packet size increase.

Probabilistic packet marking was originally introduced by Savage et al. [19]. In this approach to the IP traceback problem, each router X performs, for each packet it processes, an information injection event that occurs with a set probability p (e.g., p = 1/20). The information injection involves using b bits in the IP header that are typically not used or changed by routers (they identify the 16-bit IP identification field). They use 5 bits of this field for a hop count, which helps their reconstruction algorithm. The remaining bits are used for the message  $M_X$  that the router X wishes to send. If that message is too big, they break it into fragments and use the b-5 bits of usable IP header to store a fragment offset and its data fragment. By then including a hash interleaved with the message  $M_X$ , the victim can reconstruct  $M_X$  from the packets it receives during the DOS attack. Their algorithm is quite interesting, as it introduces the packet marking framework, and does not require a priori knowledge of the universal tree U. But their algorithm, unfortunately, is not practical for large distributed denial-of-service attacks. In particular, their algorithm for reconstructing a message  $M_X$ from a router at distance d from the victim requires  $n_d^l$ checksum tests, where  $n_d$  is the number of routers in Tat distance d from V and l is the number of fragments messages have been divided into (and this bound generously assumes there are no "noise" packets from the adversary). For example, if  $n_d = 30$  and l = 8, then the victim has to perform over 650 trillion checksum tests in order to reconstruct each of the 30 messages. Such a computation is, of course, not feasible for the victim, and even if it were, it would introduce many false positives. Moreover, this scheme is easily spoofed by an adversary that knows this algorithm.

Song and Perrig [21] improve the performance of probabilistic packet marking and suggest the use of hash chains [12] for authenticating routers. They also use a 5-bit distance field, but they do not fragment router messages. Instead, they assume the victim knows the universal tree U, and they include a (b-5)-bit XOR of hashed message authentication codes (HMACs) from each router X and its downstream neighbor Y. Once a time-released key is revealed, which is a computation performed out-of-band, the victim uses his/her knowledge of U and the revealed keys to determine which routers have marked the given packets. The computation proceeds breadth-first from V, so that each phase requires  $n_{d-1}N_d$  HMAC tests, where  $n_{d-1}$  denotes the number of routers in T at distance d-1 from V and  $N_d$ denotes the number of routers in the universal graph Uat distance d from V. For example, if  $n_{d-1} = 50$  and we conservatively estimate that the number of routers in U at distance d is 100,000, then their algorithm would perform 5 million HMAC tests to determine the routers at distance d in T. Summing over distances d = 5 to d = 25 (and assuming that near-by tests are faster), implies a total of at least 100 million HMAC tests, which

is several orders of magnitude better than a similar reconstruction in the Savage *et al.* approach. Such a computation is still a great effort for the victim, of course, but it is at least feasible. Unfortunately, using an 11-bit HMAC implies that over 45,000 of these tests will be validated at random. Thus, the authentication aspects of their algorithm has scalability issues in addition to the drawback of requiring knowledge of U.

Dean et al. [7] introduce an interesting algebraic approach to probabilistic packet marking. In their scheme a router X will mark the b reusable bits of a packet with probability p, as in the previous schemes, but the marking information is the value of a linear polynomial with X's identity as its leading coefficient. Any subsequent router Y not initiating a similar computation nevertheless changes the b-bits by performing an iteration of Horner's rule to create an evaluation of a new polynomial having the IP addresses of the routers on the path from X to Y as its coefficients. Thus, in order to reconstruct each path in the attack tree, the victim must perform polynomial interpolation with noise on the packets it has received. Dean et al. identify 25 bits in the IP header that can be used for marking, namely, 16 bits from the ID field used in fragmentation (which is used only 0.25% of the time), 8 type-of-service bits, and one flag bit (which is also used in fragmentation). They describe several algorithms for polynomial interpolation with noise for reconstructing paths of T. Their schemes do not require knowledge of the universal tree U. Unfortunately, their schemes do not easily lend themselves to authentication (without requiring knowledge of U). Moreover, the interpolation-with-noise algorithms are complex and slow for large distributed denial-of-service attacks (e.g., when T contains hundreds of routers), for in such cases the amount of "noise" far exceeds the interpolation data (some of which could have been forged by the adversary).

In addition to the above packet marking algorithms, Adler [1] and Park and Lee [16] study tradeoffs for various parameters in probabilistic packet marking.

#### 1.3 Our Results

In this paper we introduce a novel approach to probabilistic packet marking, which we call the randomizeand-link approach, that greatly improves the practicality and security of probabilistic packet marking. The main idea of our approach is to have each router Xfragment its message  $M_X$  into several words and include in the b reusable bits such a word fragment at random together with a large checksum cord on the entire message  $M_X$ . For example, if b = 25, we may wish to include 14 bits of a checksum cord in every marked packet. Such an approach to packet marking may at first seem counter-intuitive, for we are apparently wasting a large amount of "real estate" in the precious b bits. But the checksum cords make the reconstruction algorithm much more efficient. The checksum cords serve both as associative addresses for the router messages and also as partial integrity validators. They also spread the spectrum of possible messages across a large domain, which significantly reduces the ability of the adversary to interject false messages that collide with legitimate ones. As we will show, such an approach can easily reconstruct 8-fragment messages or higher, from hundreds of routers, even when the adversary is injecting packets meant to confuse or slow-down our algorithm. In addition, by including reasonably-large HMAC information in the message  $M_X$ , we can achieve unpredictability for these checksum cords, which makes the adversary's job harder, while also providing moderate-to-strong authentication of the routers in the attack tree T. Moreover, our algorithms do not require any knowledge of the universal tree U, and we avoid the requirement of having routers sign individual setup messages by employing authenticated dictionaries [2, 6, 8, 9, 15] for the out-ofband validations. We describe our methods in the sections that follow.

## 2. EFFICIENT PACKET MARKING

Let b denote the number of bits in the IP header that we can safely use to encode information from a router. For example, we may wish to use b = 25, as advocated by Dean *et al.* [7]. Indeed, we will use b = 25 as a running example throughout most of this paper. Still, even if one does not use the 8 type-of-service bits (which are being advocated for differentiated services), we would still have b = 17 (and we give some examples using this value for b as well). In either case, we may sometimes upset packet fragmentation<sup>2</sup>, but the frequency of use of fragmentation is arguably below typical packet loss rates [7].

# 2.1 High-Level View

Our scheme for sending to V the message  $M_X$  from each router X in the attack tree is based on using a technique that we call *randomize-and-link*. The main idea of this technique is to perform the following transformation to  $M_X$ :

- 1. Pad  $M_X$  as needed to make  $|M_X|$  a multiple of l, which is a parameter in our algorithm.
- 2. Compute a reasonably large (and statistically random) checksum  $C = C(M_X)$  on the sequence  $M_X$ . The checksum  $C(M_X)$  should utilize randomness in itself or  $M_X$ , so that  $C(M_X)$  is statistically random (like a random hash function) and unpredictable to the adversary (but not necessarily confidential).
- 3. Break  $M_X$  into a sequence W of non-overlapping word fragments  $w_0, w_1, w_2, \ldots, w_{l-1}$ .
- 4. Create a collection of blocks, which are used to over-write the b bits, so  $b_i = [i, C, w_i]$ .

We use these  $b_i$  blocks to transmit the message  $M_X$  to the victim V. These pieces are not sent in any particular order, however. We call  $C = C(M_X)$  the cord for  $M_X$ , as it will be used as both an associative address for  $M_X$  and a checksum to "link" all the pieces of  $M_X$  back together. Moreover, since the cord C is statistically random and unpredictable to the attacker, he cannot easily create false cords that would confuse the reconstruction algorithm. This reconstruction algorithm is therefore quite simple—given a collection of  $b_i$ 's with the same cord C, a victim simply tries all possible ways of putting the  $b_i$ 's back together in the right order, using the checksum property of the cord C to eliminate unintended sequences. Once the victim V has a valid sequence of  $b_i$ 's correctly constructed in order, V will have built the message  $M_X$ . We give the details below.

# 2.2 Randomize-and-Link Transmission

As mentioned above, we assume that the IP header allows the reuse of some of its bits for the purpose of information marking by routers. We partition the b reusable bits in the IP header as follows:

- $\lceil \log l \rceil$  bits for the fragment index i
- c bits for the cord, which serves both as an associative address and as a checksum
- $h = b c \lceil \log l \rceil$  bits for the data word  $w_i$ .

For example, if b = 25 and l = 8, then we could use  $\lceil \log l \rceil = 3$  bits for the index *i*, c = 15 bits for the checksum *C*, and h = 7 bits for each data word  $w_i$ . As we will show in our analysis, the choices of these parameters relate to the security and efficiency of our approach.

We assume that either the function C() or  $M_X$  itself contain a sufficient number of bits that are essentially random, so that the checksum value  $C(M_X)$  is statistically random and unpredictable to the adversary. That is, it is as unlikely as a random hash function with similar output size for  $C(M_X) = C(M_Y)$  for two different router messages  $M_X$  and  $M_Y$ . In addition, C should be unpredictable, so that it is difficult for the adversary to compute  $C(M_X)$  prior to its transmission to V. In particular, we want  $C(M_X)$  to be unpredictable to an adversary who knows only the value of X (we assume the adversary does not know all of  $M_X$ ). For example, if  $M_X$  does not contain sufficient randomness in itself, we could pad  $M_X$  with a random nonce, so that its cord  $C = C(M_X)$  has the desired randomness and unpredictability properties.

Given the message  $M_X$ , we pad to have size that is a multiple of l. We then compute the *c*-bit checksum (cord)  $C = C(M_X)$  on  $M_X$ , and we break  $M_X$  into a sequence W of l words  $w_0, w_1, w_2, \ldots, w_{l-1}$  of length hbits each. We define a set of l blocks  $b_0, b_1, \ldots, b_{l-1}$  so that  $b_i = [i, C, w_i]$ . Note that the cord C is included in every block  $b_i$ . Indeed, it is the inclusion of the cord C that links the blocks  $b_i$  together, as it makes C an associative address for the blocks.

# 2.3 Packet Marking

Once we have the blocks  $b_0, b_1, \ldots, b_{l-1}$  defined for a message  $M_X$ , we proceed with probabilistic packet

<sup>&</sup>lt;sup>2</sup>We will not completely destroy fragmentation, however, for our scheme will only overwrite the *b* seldom used bits in the IP header with probability p.

marking in the natural way. Namely, we define a probability parameter p (e.g., p = 1/20). With each packet that X receives, we "flip a coin" with probability p. If this coin comes up "tails" (an event that occurs with probability 1 - p), then X simply forwards the packet on to its destination as usual. Otherwise, if the coin comes up "heads," then X chooses one of its blocks  $b_i$ at random, inserts  $b_i$  into the reusable bits of this packet (updating the header checksum as needed), and forwards this revised packet on to its destination.

This packet marking process continues until we choose, for timeliness reasons, to change the message  $M_X$ . At such a time that we wish to change to a new  $M_X$ , the router X repeats that above computation for the  $b_i$  blocks for the new message. The router then repeats the probabilistic packet marking for this new set of blocks, until we decide yet another change is needed. Thus, we keep very little state at a router in order to implement the randomize-and-link packet marking scheme. A router doesn't even need to store the blocks  $b_0, b_1, \ldots, b_{l-1}$ , so long as it has a fast way of generating a  $b_i$  at random. Moreover, note that the computational overhead per packet is very small. In the default case, when the "coin flip" is tails, the router's work is the same as when we were doing no packet marking at all; hence, this scheme can be deployed incrementally. This property contrasts with most previous packet marking schemes [7, 19, 21], which require specialized additional work even when routers are not marking packets.

#### 2.4 Message Reconstruction

The message reconstruction algorithm is based on a simple combinatorial process. Given a set of packets received at the victim, we sort their b-bit blocks lexicographically by their  $(C, i, w_i)$  values, and remove duplicates (interpreting values according to the same format we used to store blocks in the IP header). This sorting can be done, for example by a radix sort. Thus, we have, for each distinct cord C, all the distinct blocks for this cord ordered by their *i*-index. We let  $P_{C,i}$  denote the set of distinct packets that have cord C and fragment index *i*. We then try all combinatorial combinations of the blocks in  $P_{C,0} \cdot P_{C,1} \cdots P_{C,l-1}$ , computing a checksum for each. We keep only those combinations that have a checksum equal to the cord C. That is, we accept these strings as being strong candidates as having been sent from the routers (although we must recognize that some of these may have been sent by the attacker). The total running time, then, for this reconstruction algorithm at the victim is proportional to the following quantity:

$$N + \sum_{C} \prod_{i=0}^{l} N_{C,i},$$

where N is the total number of packets and  $N_{C,i}$  is the number of distinct packets from this set with cord C and fragment index *i*. As we show in Section 3, the expected values of these quantities can be made quite reasonable, even if there are a large number of routers in the attack tree. For example, it is easy to observe that the expected value of  $N_{C,i}$  is  $(N'+nl)/l2^c$ , where N' is the number of distinct packets received and n is the number of routers in T.

#### 2.5 **Two-Phase Fragmentation**

In the above discussion, we argued how fragmenting a message into small blocks indexed (that is, linked) by a large statistically-random checksum cord can be an effective means for sending a message to the victim that is longer than b bits. In particular, fragmenting a message into two, four, or eight word fragments can be an efficient way to send a moderate-sized message to the victim (say, on the order of 48 to 96 bits). Unfortunately, if we have a larger-sized message (say, on the order of 128 or 192 bits), eight fragments may not be sufficient to send the message and still utilize a large checksum cord (which is needed for both security and message reconstruction). We can iterate our randomizeand-link approach, however, to send larger messages. In this subsection, we describe how to design a two-phase fragmentation scheme for sending larger messages.

We begin as in our previous method. We take the message M and subdivide it into l words,  $w_0, w_1, \ldots, w_l$ . This subdivision should be done in such as way as to preserve in each word  $w_i$  the same degree of randomness as is present globally in the message M. Still, in many cases where we want M to be reasonably large, we may observe that each word  $w_i$  is too big to be transported with high confidence in a single data block. So we further subdivide each word  $w_i$  into m subwords  $s_{i,0}, s_{i,1}, \ldots, s_{i,m}$ . Given the value *m* and the size of the subwords, we determine the number,  $c_1$ , of checksum bits that we can devote to sending the subwords in the first round (given our fixed size of b bits per block). We devote  $b - c_1 - \lceil \log m \rceil$  bits to the data in each subword  $s_{i,j}$ . Thus, we can compose subwords to form bigger blocks of  $m(b-c_1 - \lceil \log m \rceil)$  bits. In order for these big blocks to have the same security as the smaller blocks, we should devote  $c_2 = c_1 - \lfloor \log m \rfloor$  bits to a random checksum cord for each of them, just as we did in our single-phase approach. This factor is due to the fact that the probability of collision between two distinct packets in the first round is  $1/m2^{c_1}$  and this probability in the second round is  $1/lm2^{c_2}$ , since every round-two word was comprised of m round-one subwords. In addition, we must also devote  $\lceil \log l \rceil$  bits to a fragment number of each index i. So, for each word  $w_i$  we compute a  $c_2$ -bit checksum cord we wish to use in order to achieve high confidence of message transmission for each word.

Data transmission in the two-level scheme is as in the one-level scheme, except that now when a router decides to interject a message into a packet it chooses one of its many subwords,  $s_{i,j}$  at random and interjects this. Reconstruction of the message, of course, proceeds in two phases. In the first phase we reconstruct all the candidate words  $w_i$  and in the second phase we reconstruct all the candidate messages. Thus, the running time for message reconstruction in the two-phase scheme is proportional to the following:

$$N + \sum_{C} \prod_{i=0}^{m} M_{C,i} + \sum_{C} \prod_{i=0}^{l} N_{C,i},$$

where N is the total number of packets the victim is using for reconstruction,  $M_{C,i}$  is the number of distinct phase-one blocks from this set with cord C and fragment index *i*, and  $N_{C,i}$  is the number of distinct phase-two blocks with cord C and fragment index *i*. In the analysis section that follows, we show that these quantities can be quite reasonable, provided that there are a sufficient number of bits devoted to the checksum cords.

# 3. ANALYSIS

In this subsection, we analyze the randomize-and-link approach to probabilistic packet marking. We give this analysis parameterized by the various values, such as N, l, and c, and we also give specific analyses for various values assuming we have b = 25 or b = 17 bits that can be used in an IP header for message transmission.

#### 3.1 Number of Packets Needed

We begin our analysis by estimating the number of packets that are needed for traceback in our single-phase method. Let n denote the number of routers in the attack tree T, and recall that l is the number of words in the message  $M_X$  each router X wishes to transmit to the victim V. Thus, the victim wishes to receive nl distinct packets if we are to reconstruct the messages from all the routers in T.

Let p denote the probability that a router injects its information in a packet. So,  $p(1-p)^{d-1}$  is the probability that a packet is marked and arrives unchanged from a router that is d hops away from V. If we conservatively assume that all routers have their packets successfully delivered with probability at least that of the farthest routers, then we can safely estimate that the information from some router in the attack tree will be contained in a packet received by the victim with probability at least  $dp(1-p)^{d-1}$ , where d is the maximum hop-distance for any such router.

Since every router must successfully send l different blocks for all of its information to arrive at the victim, the expected number of packets that must be received before all fragments have been received is an instance of the coupon collectors problem [14], where the number of "coupons" is nl and the probability of receiving a marked packet is  $dp(1-p)^{d-1}$ . This observation implies that the expected number of packets that must arrive at the victim before it can perform a complete traceback of all n routers is  $n l H_{nl} / dp (1-p)^{d-1}$ , where  $H_n$ denotes the *n*-th Harmonic number. Using an inequality for  $H_n$  from Knuth [11],  $H_n < \ln n + \gamma + 1/2n$ , where  $\gamma$  = 0.5772156649... is Euler's constant. Thus, the expected number of packets that must arrive at V before it can perform a complete traceback of n routers using our scheme is at most  $(nl\ln(nl) + \gamma nl + 1)/dp(1-p)^{d-1}$ . For example, if p = 1/20, d = 20, n = 1000, and l = 8, then the expected number of needed packets to do reconstruction of all the router messages is 76516, not considering the packet marking probability  $dp(1-p)^{d-1}$ . Dividing this expectation by the packet marking probability in this case implies that the expected total number of packets needed by the victim to do complete reconstruction of all messages is 202770. Moreover, we can assume that

the attacker's packets arrive at the victim with probability  $(1-p)^d$ , which is approximately 36% of the time in this example. Thus, in this example, we could expect that victim received unchanged from the attacker 72690 the 202770 expected packets the victim needs for attack tree reconstruction. Note that there are only nl distinct packets that come from the routers in the attack tree. Thus, in this example, we should not expect to have to consider more than 80690 distinct packets during the message reconstruction phase of the randomize-andlink algorithm (72690 "noise" packets and 8000 message packets). Note that this is roughly equal to the expected number of packets needed without consideration of the packet marking probability. Contrast this, for example, with an ICMP messaging solution, which would require that the victim receive at least 7.5 million attack packets before it could expect to identify all the participating routers (assuming d = 20 and the ICMP injection probability is 1/20000).

The analysis of the two-phase version of the randomizeand-link algorithm is similar to that given above for the single-phase version. The main difference is that in the two-phase algorithm we wish to receive, from each router, l words subdivided into m subwords. That is, we wish to receive lm packets from each router. Thus, the expected number of packets we have to receive in order to do complete traceback is  $nlmH_{nlm}/dp(1-p)^{d-1}$ .

## 3.2 Analysis of Message Reconstruction

Let us address next the expected running time needed to reconstruct all the messages received by the victim. We give the analysis first for our single-phase algorithm, and we then explain the slight differences for our twophase algorithm.

The important observation in analyzing the expected running time of the message reconstruction algorithm is that, since the checksum cords are statistically random, we can view the mapping of messages to checksum indices as a random hash function. Thus, the number of collisions among legitimate messages should be small. Of course, the adversary might construct lots of fake messages and then construct lots of collisions with these messages, but let us ignore this possibility for the time being (we will revisit this possibility shortly).

We begin with the reconstruction algorithm for our single-phase scheme. Let N denote the number of distinct packets the victim has received and let n denote the number of routers in the attack tree. Since there are l pieces to each message and each one has a c-bit checksum cord that is statistically random, the probability that two random packets have the same fragment index i and cord C is  $1/(l2^c)$ . In addition, the probability that two router-sent packets have the same fragment index i and cord C is at most  $1/2^c$ , since any router wishing to send a message will send a packet with each *i*-index for the checksum cord C it is using. Thus, the expected number of packets with the same fragment index i and cord C is at most  $\lfloor N/(l2^c) + n/2^c \rfloor$ . For any given cord C, then, the running time for computing all combinatorial combinations of blocks with this cord is proportional to  $Z = Z_0 Z_1 \cdots Z_{l-1}$ , where  $Z_i$  is a random variable corresponding to the number of packets with fragment index i (for this checksum cord C). Since these  $Z_i$ 's refer to different fragment indices, they are independent; hence, the expected value of their product is equal to the product of their expected values. That is, the expected running time for checking all the combinations for a given checksum cord C is  $\lceil (N + ln)/(l2^c) \rceil^l$ . Summing this expectation over the at most N possible cord values, we see that the expected number of checksum tests in the message reconstruction phase is

$$\left(\frac{N}{l}\right) \left[\frac{N+ln}{l2^c}\right]^l,$$

where the N/l bound comes from the fact that we have to have at least l different fragments for a given checksum cord before we will have to perform an actual checksum test. So, for example, if N = 80000, l = 8, n =1000, and c = 14, then the expected number of checksum tests the victim must make is only 10,000. Thus, if the adversary acts in a completely random fashion, there is little additional work that he can create for us in our single-phase algorithm.

The adversary has little advantage in our two-phase algorithm, as well, although the total number of packets needed in this case is somewhat greater than in the single-phase approach. Specifically, in the two-phase algorithm, each router sends a total of lm fragments. The victim first assembles these as m-length subwords, and then assembles the l words produced from this reconstruction. If the first phase uses  $c_1$ -bit checksum cords and the second phase uses  $c_2$ -bit checksum cords, then the expected number of checksum tests for the two-phase algorithm is

$$\left(\frac{N}{m}\right) \left\lceil \frac{N+nlm}{m2^{c_1}} \right\rceil^m + \left(\frac{N}{lm}\right) \left\lceil \frac{N+nlm}{lm2^{c_2}} \right\rceil^l$$

The arguments justifying this bound are similar to those above, but applied twice. So, for example, if N = 80000, l = 8, m = 4, n = 250,  $c_1 = 14$ , and  $c_2 = 12$ , then the expected number of checksum tests the victim must make is 10,000.

Of course, the adversary may deliberately send false messages to us that have valid checksum cords according to our scheme. But the number of such messages is limited, for the adversary must be limited to the same coupon collector bounds as the legitimate routers in T. To estimate the number of such false messages, let us conservatively assume that the probability that a packet arrives unchanged from the adversary is equal to the probability that the victim receives a packet marked by a router. Thus, the maximum number of false messages the adversary can send is bounded by n, the number of legitimate routers in the attack tree. Still, the adversary may not only try to send us false message with valid checksum cords. He may also send lots of extra packets that have checksum cords that deliberately collide with each other, so as to make us do extra wasteful work trying in vain to find a combination of these word fragments that have a checksum equal to this cord. Fortunately, as we show in the next subsection, we can apply a probabilistic packet filtering strategy to our algorithm that

significantly limits the amount of extra work the adversary can force us to do in combining colliding word fragments.

# 3.3 High Probability Packet Filtering

In this subsection, we derive a high-probability upper bound on the running time of the message reconstruction algorithm, which is useful for identifying improbably large numbers of collisions that are most likely deliberately sent by the adversary in an attempt to slow down our traceback algorithm. Armed with this highprobability bound, we can safely discard packets that define an improbably large number of collisions in reconstructing the blocks for a specific cord C. We derive this upper bound somewhat indirectly, as it is easier to derive bounds on summations of random variables than it is on their products. Let us fix a checksum cord C, and let  $Y = Z_0 + Z_1 + \cdots + Z_{l-1}$ , where  $Z_i$  denotes the number of distinct blocks with fragment index i and cord C. We will bound Y and thereby derive a bound on  $Z = Z_0 Z_1 \cdots Z_{l-1}$ . We will utilize the following Chernoff bound (e.g., see Motwani and Raghavan [14]):

**Theorem 1 (Chernoff Bound Theorem):** Let Y be the sum of independent indicator (0/1) random variables, and let  $\mu$  denote the expected value of Y. Then,

$$\Pr(Y > (1+\delta)\mu) < \left(\frac{e^{\delta}}{(1+\delta)^{1+\delta}}\right)^{\mu}$$

**Corollary 2:** Let Y be the sum of independent indicator (0/1) random variables, and let  $\mu$  denote the expected value of Y. For any  $k > \mu$ ,

$$\Pr(Y > k) < \frac{e^{k-\mu}\mu^k}{k^k}$$

Returning to our analysis, then, note that Y can be defined as the sum of independent indicator random variables and that the expected value of Y is  $\mathbf{E}(Z_0) + \mathbf{E}(Z_1) + \cdots + \mathbf{E}(Z_{l-1})$ . Thus, in the single-phase algorithm,  $\mathbf{E}(Y)$  is  $lN/(l2^c) + ln/2^c = (N + ln)/2^c$ . Thus, we have the following fact:

**Lemma 3:** Suppose  $N \leq l2^c$ . Then, for any integer  $x \geq 2$ ,

$$\Pr(Y > lx) < \frac{e^{xl - (N+ln)/2^c}}{x^{xl}l^{l(x-1)}};$$

hence,

$$\Pr(Z > x^{l}) < \frac{e^{xl - (N+ln)/2^{c}}}{x^{xl}l^{l(x-1)}}.$$

Thus, we can bound with this same probability that Y > lx the odds that  $Z > x^l$ . So, for example, if l = 8, c = 15, x = 3,  $n = 2^{10}$ , and  $N = 2^{18}$ , then the probability that Y > 24 is less than  $1/2^{48}$ , which is a very small number. Thus, in this example, we may safely discard the packets for any index C that have more than 24 packets. That is, we may safely discard any subproblems that would cause us to perform more than  $3^8 = 6561$  checksum tests. With high probability, such a subproblem will not occur at random, so it most

Frag.	Number, $c$ , of Checksum Bits						
scheme	9	10	11	12	13	14	15
2	56	52	48	44	40	36	32
3	104	96	88	80	72	64	56
2 + 2	188	168	148	128	108	88	68
3 + 2	380	344	308	272	236	200	164
3 + 3	760	688	616	544	472	400	328

**Table 1:** Message sizes for the given fragmentation schemes and checksum lengths, assuming b = 25 is the bit length of individual blocks. A fragment scheme identified by "x" indicates a scheme with x number of bits used to index fragments. A fragment scheme identified by "x + y" indicates a two-phase fragmentation scheme where the first round uses x bits for the fragment index and the second round uses y bits for the fragment index. We index the checksum needs in the two-phase schemes by  $c_1$ , since we can set  $c_2 = c_1 - \lceil \log l \rceil$  and get the same confidence bound.

Frag.	Number, $c$ , of Checksum Bits						
scheme	8	9	10	11			
3	48	40	32	24			
2 + 2	80	60	40	20			
3 + 2	160	124	88	52			
3 + 3	320	248	176	104			

**Table 2:** Message sizes for the given fragmentation schemes and checksum lengths, assuming b = 17 is the bit length of individual blocks.

likely was sent to us by the adversary in an attempt to make us do extra unnecessary work in our single-phase traceback algorithm. A similar analysis can be done for the two-phase algorithm, which we omit here.

## 3.4 Trading-Off Message and Cord Size

As we observed above, increasing the checksum size leads to higher security. A large checksum makes the space of possible messages addresses large, which in turn makes it that much more difficult for the adversary to interject false messages that collide with legitimate ones. Of course, this increased security has a cost. Namely, as the checksum becomes larger, the bits left over for the message must go down. Even so, there are still several strong choices for checksum lengths and fragmentation schemes that allow for message sizes long enough to do authenticated IP traceback. We show in Table 1 the maximum message size for various randomize-and-link fragmentation schemes, assuming b = 25, and we show similar information for b = 17 in Table 2.

## 3.5 Sufficient Packet Volume

We have described the randomize-and-link strategy in a general way, so as to allow for several possible message sizes. But we should also recognize that reconstructing large messages requires more packets. Moreover, the number of needed packets also increases with the number of routers in the attack tree. In order to keep the reconstruction algorithm fast, we prefer that expected number of collisions between a given packet and any other packet be less than 2. The randomize-and-link algorithm will still work for higher expectations, but it

Frag.	Numbe	r, n, of I	Routers in	Attack Tree	
scheme	50	100	250	500	1000
2	1176	2628	7486	16357	35486
3	2628	5810	16357	35486	76516
2 + 2	5810	12729	35486	76516	164122
3 + 1	5810	12729	35486	76516	164122
2 + 3	12729	27675	76516	164122	350424
3 + 2	12729	27675	76516	164122	350424
3 + 3	27675	59785	164122	350424	745208

**Table 3:** Expected upper bounds on N, the number of packets that need to be received for various fragmentation schemes and number of routers, n, in the attack tree. The volumes given are the expected number needed to cover all the routers. If we conservatively assume that the probability a packet arrives marked by a router is equal to the probability that a packet arrives unmarked, the same numbers bound the expected number of packets from the adversary. The upper bounds are on the number of required packets, without regard to the marking probability. To convert the presented numbers to an expectation that factors in the marking probability, the above values should be divided by  $pd(1-p)^{d-1}$ .

Frag.	Number, $n$ ,	of	Routers	$_{\mathrm{in}}$	Attack	Tree
-------	---------------	----	---------	------------------	--------	------

scheme	50	100	250	500	1000	2000
2	8	9	10	11	13	14
3	8	9	10	12	13	14
2 + 2	10	11	13	14	15	16
3 + 1	9	10	12	13	14	15
2 + 3	11	12	14	15	16	17
3 + 2	10	11	13	14	15	16
3 + 3	11	12	14	15	16	17

**Table 4:** The checksum sizes needed for the different randomize-and-link fragmentation schemes, assuming various values of the number of routers, n, in the attack tree. The checksum sizes given are the number needed to force the expected collision size to be less than 2. For the two-phase schemes, the checksum size is given for the first round, since its checksum needs are higher.

is most efficient when the expected collision size is less than 2. Thus, we have worked out the needed packet volume and checksum bit-length for various randomizeand-link fragmentation schemes under various numbers of routers in the attack tree. We provide this information in Tables 3 and 4.

# 4. ROUTER AUTHENTICATION

In this section, we discuss several possible IP traceback schemes that are based on the randomize-and-link approach. This discussion is not meant to be exhaustive, however, as the randomize-and-link approach only specifies the length of the information that is sent from routers in the attack tree to the victim. The main points we want to make in the following discussion, then, is to show how the randomize-and-link strategy can be used to create traceback methods that scale to hundreds of routers, that do not require the victim know the universal tree U, and that can authenticate routers without requiring them individually to sign setup messages.

All of our traceback mechanisms create the message  $M_X$  that a router X will transmit so that it includes X's identity. That is,  $M_X$  includes X's 32-bit IP address. Additionally, if we want to learn the topology of the attack tree T, as opposed to simply learning the names of all the routers in T, we can optionally have each router X also include in  $M_X$  the name of its downstream router in T, which would add another 32 bits to  $M_X$ . This identity and optional topology information, of course, does not provide any additional randomness or authentication information to  $M_X$ , as is needed by the security needs of a good randomize-and-link traceback scheme. Fortunately, there are several ways that we can simultaneously add randomness and authentication to  $M_X$ . Before we describe some of these ways, however, let us briefly review the main cryptographic tool that these methods are based on.

#### 4.1 Authenticated Dictionaries

Our different authentication schemes all utilize an authenticated dictionary for some portions of the task of authenticating routers. An authenticated dictionary [2, 6, 8, 9, 15] consists of a trusted source and many untrusted directories. The trusted source produces and maintains a dictionary database, D, of objects, stored as key-value pairs, (k, o), while the directories answer key-value queries for D on behalf of client users. In requesting a key-value query, a client provides a key k and asks the directory to return the object o in D that has k as its key. If there is such an object, then the directory returns it. If, on the other hand, there is no object with key k in D, then the directory returns a special "no-such-object" value. In either case, in addition to the answer a directory gives, a directory also provides a cryptographic proof of that answer, which validates (subject to standard cryptographic assumptions) that the answer is current and is as accurate as if it had come directly from the source. There is a small (usually logarithmic) overhead incurred for this cryptographic proof, but it allows the source to be offline during the request. In addition, by deploying many directories widely dispersed in the network, using an authenticated dictionary allows us to reduce response latency and the effectiveness of a denial-of-service attack on the authenticated dictionary itself (for such an attack would have to target all of the directories simultaneously). We describe below how authenticated dictionaries can be used in various traceback schemes to allow for strong authentication of routers without requiring them to sign any setup messages individually.

## 4.2 Authentication Methods

In this subsection, we describe several methods for authenticating routers in a randomize-and-link traceback scheme.

HMAC with Individual Key Exposure. One way to do router authentication is to determine, for each router X, a sequence of secret keys  $K_{X,0}, K_{X,1}, \dots$  Then, with a message  $M_X$  intended for a victim V, the router X includes a hashed message authentication code (HMAC) of  $h(V||K_{X,t})$ , where h is a one-way cryptographic hash function and t is a time-quantum counter that is of sufficient granularity that we can assume rough synchronization between routers and the victim. We include V in the HMAC so as to reduce the possibility of a replay attack. We reveal the key  $K_{X,t}$  for each router X in time quantum t + 2. The revelation is done using an authenticated dictionary for each autonomous system (AS), whose source is the administrator of the AS. Indeed, we assume this administrator distributed the secret keys to his or her routers in the first place. To determine the amount of extra space this scheme adds to the message  $M_X$ , note that we did not include the packet's source address in the HMAC, as is done, for example, in a previous scheme [21], for this value is set by the adversary. Thus, there is no risk of a birthday attack for our hash function h, as its data is fixed for Vand the current time quantum t. This scheme will therefore add 32, 48, or 64 bits to  $M_X$  depending on whether we want fair, moderate, or strong authentication of X.

HMAC with Messaged Key Exposure. An alternate scheme to the previous authentication method is to utilize a sequence of secret keys,  $K_{X,0}, K_{X,1}, ...,$  as before, but include  $K_{X,t-2}$  in  $M_X$  during time quantum t. In this way, the router X itself reveals the secret key used in the HMAC. In this case, we should create the sequence of keys themselves as a hash chain [12]using a one-way cryptographic hash function, g, so that  $K_{X,i} = g(K_{X,i+1})$ . Then we need only store  $K_{X,0}$  in the authenticated dictionary for X's autonomous system. For given any revealed  $K_{X,t}$ , the victim can determine the authenticity of this key by performing t applications of the function q. Thus, this approach reduces the work required of the AS administrator, so that rather than revealing keys with each time quantum, the administrator now just needs to reveal the base of each router's hash chain. The trade-off is that we now are including more information in  $M_X$ . Namely, we are adding 64, 96, or 128 bits to  $M_X$ , depending on whether we want fair, moderate, or strong authentication of X. In addition, since the keys are determined through a hash chain, we now require the victim to perform t hash computations for every router in the attack tree. This effort can be significant if the number of routers in T is over 1000.

HMAC with Key Collection Exposure. There is another alternative that we can make to router authentication, which reduces the work needed for both the victim and the AS administrators when the number of routers is large. Rather than issue a different sequence of keys for every router in an AS, the administrator instead issues just 64 key sequences, divided into two sets of 32 key sequences:  $\kappa_0, \kappa_1, \ldots, \kappa_{31}$  and  $\lambda_0, \lambda_1, \ldots, \lambda_{31}$ . So  $\kappa_i = (K_{i,0}, K_{i,1}, \dots)$  and  $\lambda_i = (L_{i,0}, L_{i,1}, \dots)$ . These key sequences (possibly as hash chains) are then distributed to routers according to their IP addresses—so that if  $X = (x_0, x_1, \dots, x_{31})$  is the binary expansion of X's address, then X is assigned the key sequence  $(\omega_0, \omega_1, \ldots, \omega_{31})$ , where  $\omega_i = \kappa_i$  if  $x_i = 0$  and  $\omega_i = \lambda_i$ otherwise. To determine the key  $K_{X,t}$  to use in an HMAC, the router X simply computes the XOR of all the *t*-th keys in the sequences it was assigned. Thus, after a delay of two time quantums, a victim need only retrieve from the authenticated dictionary the 64 t-th keys in the sequences  $\kappa_0, \kappa_1, \ldots, \kappa_{31}$  and  $\lambda_0, \lambda_1, \ldots, \lambda_{31}$ . From these 64 keys it can compute any key  $K_{X,t}$ , just by knowing the value of X. Thus, this scheme has the benefits of keeping the amount of additional authentication information in  $M_X$  to 32, 48, or 64 bits, depending on whether we desire fair, moderate, or strong authentication. Even so, it requires only a modest amount of work on the part of the administrator for the AS: namely, the revelation of 64 keys in each time quantum. Of course, this revelation could be carried out by a trusted agent for the administrator if we use hash chains to determine the  $\kappa_i$  and  $\lambda_i$  sequences.

# 5. DISCUSSION AND CONCLUSION

We have presented a new approach to IP traceback based on the probabilistic packet marking paradigm. Our approach, which we call randomize-and-link, uses large checksum cords to link message fragments in a way that is highly scalable, for the cords serve both as associative addresses and data integrity verifiers. For example, with a 12-bit checksum cord we can use a singlephase randomize-and-link scheme to produce an 80-bit message that contains a router's 32-bit IP address and a 48-bit combination HMAC. Such a scheme would allow for fast and efficient message reconstruction for up to 500 routers in the attack tree T. If we wish to traceback efficiently attacks that are targeting a victim through a larger attack tree, we could use a 16-bit initial checksum cord in a two-phase randomize-and-link strategy (using 8 subwords in phase one and 4 words in phase two) that produces a 128-bit message. Such a message could contain a router X's IP address, the IP address of the downstream neighbor of X, and a 64-bit HMAC (collective or individual). Or such a message could contain X's IP address, a 48-bit HMAC, and a 48-bit key revelation. In either case, using a 16-bit checksum cord with a two-phase scheme producing a 128-bit message would allow for fast and efficient traceback for attack trees of size up to 2000 routers. In general, our methods do not require that a victim know the topology of the universal tree U, we do not require that routers sign any setup messages individually, and we allow for incremental adoption (for the default router action is to process packets in the same way as a non-participating router).

#### Acknowledgments

We thank Maithili Narasimha, Dawn Song, and Gene Tsudik for helpful discussions related to this paper.

# 6. **REFERENCES**

- M. Adler. Tradeoffs in probabilistic packet marking for IP traceback. In 34th ACM Symposium Theory of Computing (STOC), 2002.
- [2] A. Anagnostopoulos, M. T. Goodrich, and R. Tamassia. Persistent authenticated dictionaries and their applications. In *Information Security Conference (ISC 2001)*, LNCS 2200, 379–393, 2001.
- [3] T. Baba and S. Matsuda. Tracing network attacks to their sources. *IEEE Internet Computing*, 6(2):20–26, 2002.

- [4] S. M. Bellovin. ICMP traceback messages. In Work in Progress, Internet Draft draft-bellovin-itrace-00.txt, March 2000.
- [5] H. Burch and B. Cheswick. Tracing anonymous packets to their approximate source. In Usenix LISA (New Orleans) Conference, 313–322, 2000.
- [6] R. Cohen, M. T. Goodrich, R. Tamassia, and N. Triandopoulos. Authenticated data structures for graph and geometric searching. Technical report, Brown University, 2001.
- [7] D. Dean, M. Franklin, and A. Stubblefield. An algebraic approach to IP traceback. In *Network and Distributed* System Security Symposium (NDSS), 3–12, 2001.
- [8] P. Devanbu, M. Gertz, C. Martel, and S. Stubblebine. Authentic third-party data publication. In *Fourteenth IFIP 11.3 Conference on Database Security*, 2000.
- [9] M. T. Goodrich, R. Tamassia, and A. Schwerin. Implementation of an authenticated dictionary with skip lists and commutative hashing. In 2001 DARPA Information Survivability Conference and Exposition, vol. 2, 68–82, 2001.
- [10] J. Ioannidis and S. M. Bellovin. Implementing pushback: Router-based defense against DDoS attacks. In Network and Distributed System Security Symposium. The Internet Society, 2002.
- [11] D. E. Knuth. Fundamental Algorithms, vol. 1 of The Art of Computer Programming. Addison-Wesley, Reading, MA, 2nd edition, 1973.
- [12] L. Lamport. Password authentication with insecure communication. Communications of the ACM, 24(11):770–772, 1981.
- [13] D. Moore, G. Voelker, and S. Savage. Inferring internet denial-of-service activity. In Usenix Security Symposium, 2001.
- [14] R. Motwani and P. Raghavan. Randomized Algorithms. Cambridge University Press, New York, NY, 1995.
- [15] M. Naor and K. Nissim. Certificate revocation and certificate update. In 7th USENIX Security Symposium (SECURITY-98), 217–228, Berkeley, 1998.
- [16] K. Park and H. Lee. The effectiveness of probabilistic packet marking for IP traceback under denial of service attack, 2000.
- [17] V. Paxson. An analysis of using reflectors for distributed denial-of-service attacks. ACM Computer Communications Review (CCR), 31(3), July 2001.
- [18] J. Postel. Internet protocol, 1981.
- [19] S. Savage, D. Wetherall, A. R. Karlin, and T. Anderson. Practical network support for IP traceback. In *SIGCOMM*, 295–306, 2000.
- [20] A. C. Snoeren, C. Partridge, L. A. Sanchez, C. E. Jones, F. Tchakountio, S. T. Kent, and W. T. Strayer. Hash-based IP traceback. In ACM SIGCOMM 2001 Conference on Applications, Technologies, Architectures, and Protocols for Computer Communication, 2001.
- [21] D. Song and A. Perrig. Advanced and authenticated marking schemes for IP traceback. In *IEEE Infocomm*, 2001.
- [22] R. Stone. Centertrack: An IP overlay network for tracking DoS floods. In 9th USENIX Security Symposium, August 2000.