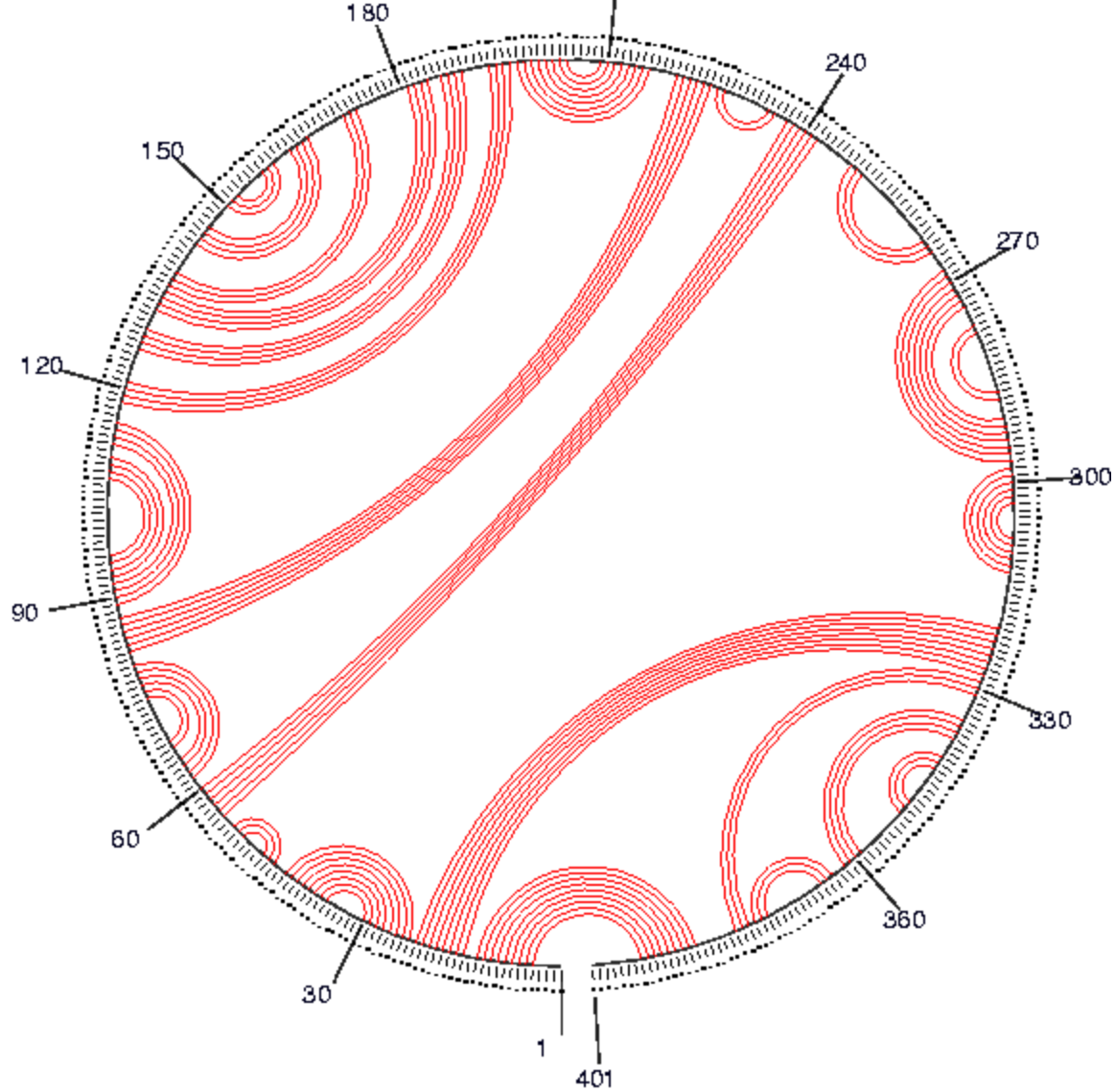


GLOBEX Bioinformatics (Summer 2015)

RNA secondary structure

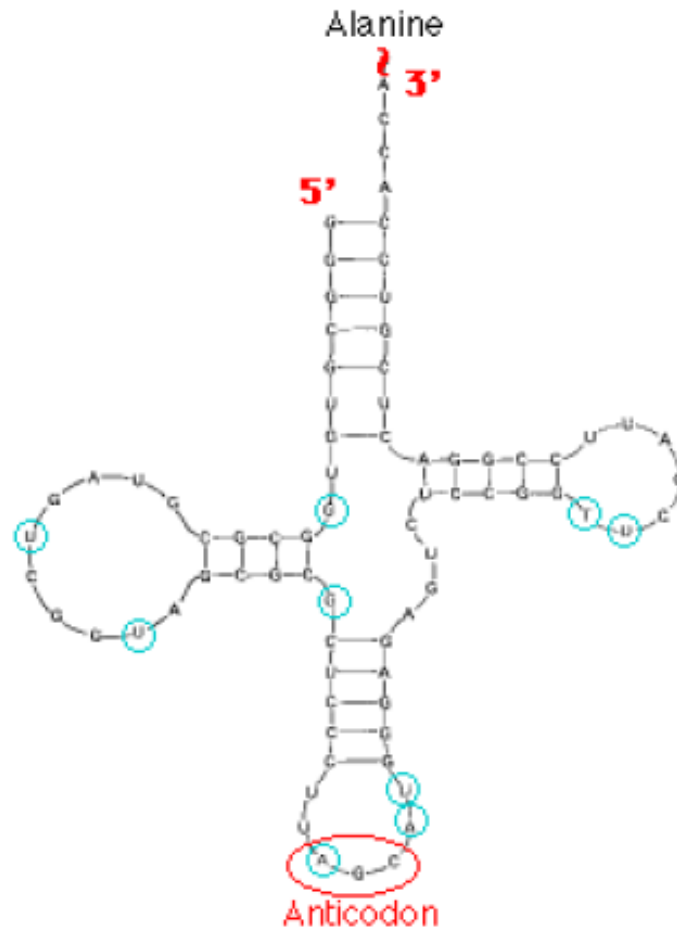
Facts about RNAs

- Mainly as “information carrier” in protein synthesis
 - mRNA
 - tRNA
- Also as catalysts
 - Ribozymes
- Also as regulator
 - RNAi
- Single strand
 - Intra-molecular pairing
 - Secondary structure
 - Essential for sequence stability and function
- Similarity in secondary structure plays a more important role than primary sequence in determining homology for RNAs

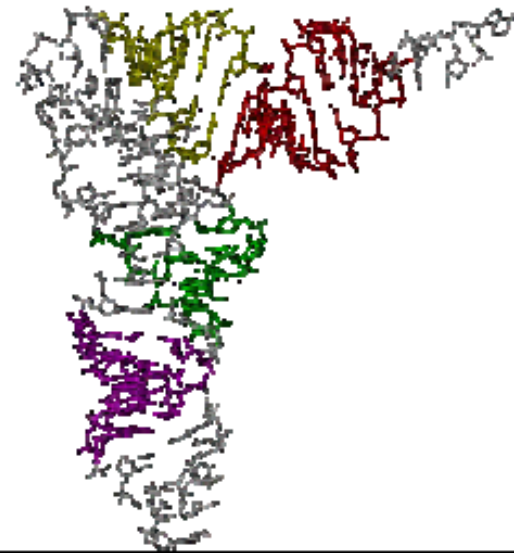


ENERGY = -85.7 Bacillus subtilis RNase P RNA

tRNA Secondary Structure



tertiary structure



Secondary structure prediction

Base pair maximization algorithm [Nussinov]

$m_{i,j}$: maximal # of base pairs that can be formed for sequence $s_i \dots s_j$.

$d_{i,j} = 1$, if s_i and s_j are paired
 $= 0$, otherwise

Initialization

$m_{i,i-1} = 0$ for $i = [2, L]$

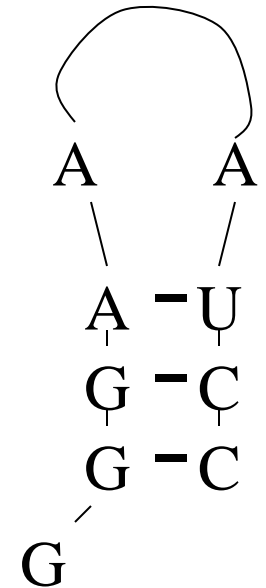
$m_{i,i} = 0$ for $i = [1, L]$

Recursion

$m_{i,j} = \max \{ m_{i+1,j},$
 $m_{i,j-1},$
 $m_{i+1,j-1} + d_{i,j},$
 $\max_{i < k < j} \{ m_{i,k} + m_{k+1,j} \}$
 $\}$ // bifurcation

Dynamic programming table

		1	2	3	4	5	6	7	8	9
		G	G	G	A	A	A	U	C	C
1	G	0 →						1	2	3
2	G		0 ↗					1	2	3
3	G			0				1	2	2
4	A				0			1	1	1
5	A					0	0	1	1	1
6	A						0	1	1	1
7	U							0		
8	C								0	
9	C									0



Time Complexity: $O(L^3)$, where L is sequence length

Space complexity: $O(L^2)$

Secondary structure prediction

Minimum energy algorithm [Zuker]

$E_{i,j}$: minimum energy for an optimal fold formed by sequence $s_i \dots s_j$.

$$\begin{aligned} e_{i,j} &= -5, \text{ if } s_i, s_j \text{ is CG or GC} \\ &= -4, \text{ if } s_i, s_j \text{ is AU or UA} \\ &= -1, \text{ if } s_i, s_j \text{ is GU or UG} \end{aligned}$$

Initialization

$$\begin{aligned} E_{i,i-1} &= 0 && \text{for } i = [2, L] \\ E_{i,i} &= 0 && \text{for } i = [1, L] \end{aligned}$$

Recursion

$$\begin{aligned} E_{i,j} = \min \{ & E_{i+1,j}, \\ & E_{i,j-1}, \\ & E_{i+1,j-1} + e_{i,j}, \\ & \min_{i < k < j} \{ E_{i,k} + E_{k+1,j} \} && // \text{ bifurcation} \\ & \} \end{aligned}$$

Resources

Lecture notes:

<http://www.bioinfo.rpi.edu/~zukerm/lectures/RNAfold-html/>

RNA informatics:

http://www-lbit.iro.umontreal.ca/RNA_Links/RNA.shtml

Software:

- Vienna RNA fold

- Mfold (<http://www.bioinfo.rpi.edu/zukerm/export/>)