Uncertainty. (10 points) Suppose that four different Boolean sensors (S1, S2, S3, S4) are used to predict an imminent earthquake $E$, with the following probabilities:

$$
\begin{array}{lllll}
p(E)=.02 & p(S 1 \mid E)=0.01 & p(S 2 \mid E)=0.1 & p(S 3 \mid E)=0.002 & p((S 4 \mid E)=0.0003 \\
p(S 1)=.01 & p(S 2)=.01 & p(S 3)=.01 & p(S 4)=.01
\end{array}
$$

(a) [ 5 pts$]$ Assuming the conditional independence of $\mathrm{S} 1, \mathrm{~S} 2, \mathrm{~S} 3$, and S 4 given E (often called Naive Bayes), compute the $\mathrm{p}(\mathrm{EIS} 1, \mathrm{~S} 2, \mathrm{~S} 3, \mathrm{~S} 4)$.
(b) [5 pts]Suppose that you are told that the probability of all of the sensors registering positive given an imminent earthquake is 0.000004 and you are also given the following additional information:

$$
\mathrm{p}(\mathrm{~S} 1, \mathrm{~S} 4)=.01 \quad \mathrm{p}((\mathrm{~S} 21 \mathrm{~S} 1, \mathrm{~S} 3, \mathrm{~S} 4)=.03
$$

What one other piece of information do you need in order to compute a better estimate of $p(E I S 1, S 2, S 3, S 4)$ than is provided by Naive Bayes? Give the formula that you would use to compute this better estimate, using all of these additional pieces of information.

Planning. ( 15 points) Consider the Towers of Hanoi problem as a planning problem. Here, the idea is to move all the disks from Peg 1 to Peg 3, one at a time, where no larger disk may ever be placed upon a smaller disk.


Consider the following initial state.

| At(D3, 1, P1) | Top(P1,3) | Size(D3, 3) |
| :--- | :--- | :--- |
| At(D2, 2, P1) | Top(P2,0) | Size(D2, 2) |
| At(D1, 3, P1) | $\operatorname{Top(P3,0)}$ | Size(D1, 1) |

(a) [12 pts] Write an STRIPS-style operator schema or schemas to represent the operations in this problem so that it could be solved by a planner. You may use numerical comparisons (<, >, =, etc.) and functions + and - only. Do not use conditional schemas.
(b) [3 pts] Argue that you don't really need + and -at all.

