

Review of material covered before midterm exam

Book lectures covered: 1-16, A, 17, 18

- 1: not much here
- 2: review of strings and sets, concatenation, set operations: union, intersection, complement, set concatenation, powers, asterate
- 3: formal definition of deterministic finite automaton (DFA), language of a DFA, regular sets
- 4: closure properties of regular sets: union, intersection, complement, concatenation, asterate; product of two DFAs
- 5: nondeterministic finite automata (NFA), subset construction of an equivalent DFA from an NFA, do it without constructing unreachable states
- 6: Formal definition of NFAs, the subset construction, Thm: an NFA and the DFA constructed from it accept the same set of strings, ϵ -transitions, proof that concatenation preserves regularity
- 7: patterns; atomic: letters in Σ , ϵ , \emptyset , $\#$, $@$; compound patterns: $+$, \cap , \cdot (concatenation), \sim , $*$, $(,)$, the languages of patterns, pattern matching
- 8: regular expressions: patterns restricted to letters in Σ , ϵ , \emptyset , $+$, \cdot , $*$, $(,)$, Thm: the languages of DFAs, patterns and regular expressions are all the same
- 9: simplification of regular expressions (pp. 49,50,57), construction of regular expression for the language of a DFA or NFA using $\alpha_{u,v}^X$ (pg. 52)
- A: Kleene algebra: pages 55-top three lines of 58; skip from matrices onward
- 10: homomorphisms, use to show other sets are regular, use to reduce NFAs with ϵ -transitions to NFAs without ϵ -transitions; skip Hamming distance
- 11: not all sets are regular, Pumping lemma, especially the contrapositive version
- 12: using the pumping lemma to show a set is not regular, ultimate periodicity
- 13: minimization of DFAs, quotient construction of M/\approx from M and \approx , Thm: $L(M'/\approx) = L(M)$
- 14: a minimization algorithm; computing \approx relation, M/\approx
- 15: Isomorphism, Myhill-Nerode relations for a set R ; right congruence, refinement of R , finite index, \equiv_M , M_{\equiv}
- 16: Myhill-Nerode theorem, use to show whether a set is regular or not
- 17: Two-way deterministic A, finite automata(2DFA), formal definition, configurations, the next relation $(\frac{1}{x})$, other binary relations, \xrightarrow{n} , $\xrightarrow{*}$
- 18: Tables T_x for showing the state of a 2DFA as it moves its head left and right across the right boundary of string x , the equivalence relation I called \equiv_T , construction of a DFA from the tables (two ways), showing that 2DFAs accept only regular sets