

Introduction to Parsing



- Checks the stream of <u>words</u> and their <u>parts of speech</u> (produced by the scanner) for grammatical correctness
- Determines if the input is syntactically well formed
- Guides checking at deeper levels than syntax
- Builds an IR representation of the code

Think of this as the mathematics of diagramming sentences



The process of discovering a *derivation* for some sentence

- Need a mathematical model of syntax a grammar G
- Need an algorithm for testing membership in L(G)
- Need to keep in mind that our goal is building parsers, not studying the mathematics of arbitrary languages

Roadmap

- 1 Context-free grammars and derivations
- 2 Top-down parsing
 - → Hand-coded recursive descent parsers
- 3 Bottom-up parsing
 - \rightarrow Generated LR(1) parsers

Specifying Syntax with a Grammar



(words)

Context-free syntax is specified with a context-free grammar

SheepNoise → SheepNoise <u>baa</u> | <u>baa</u>

This CFG defines the set of noises sheep normally make

It is written in a variant of Backus-Naur form

Formally, a grammar is a four tuple, G = (S, N, T, P)

- S is the start symbol (set of strings in L(G))
- N is a set of non-terminal symbols (syntactic variables)
- T is a set of *terminal symbols*
- P is a set of productions or rewrite rules $(P: N \rightarrow (N \cup T)^{+})$

Deriving Syntax



We can use the *SheepNoise* grammar to create sentences

 \rightarrow use the productions as *rewriting rules*

Rule	Sentential Form	Rule	Sentential Form
	ChaonAlaida	_	SheepNoise
_	SneepiNoise	1	SheepNoise baa
2	baa	1	, SheepNoise baa baa
		2	baa baa baa
Rule	Sentential Form	_	
_	SheepNoise		
1	SheepNoise <u>baa</u>	And so on	
2	baa baa		

Т



A More Useful Grammar

To explore the uses of CFGs, we need a more complex grammar

1	Expr	\rightarrow	Expr Op Expr
2			number
3			<u>id</u>
4	Ор	1	+
5			_
6			*
7			1

need a more complex gramm					
Rule	Sentential Form				
—	Expr				
1	Expr Op Expr				
2	<id,<mark>x> <i>Op Expr</i></id,<mark>				
5	<id,<u>x> - Expr</id,<u>				
1	<id,<u>x> - Expr Op Expr</id,<u>				
2	<id,<u>x> - <num,<u>2> Op Expr</num,<u></id,<u>				
6	<id,<u>x> - <num,<u>2> * <i>Expr</i></num,<u></id,<u>				
3	<id,<u>x> - <num,<u>2> * <id,<u>y></id,<u></num,<u></id,<u>				

- Such a sequence of rewrites is called a *derivation*
- Process of discovering a derivation is called *parsing*

We denote this derivation: $Expr \Rightarrow^* \underline{id} - \underline{num} * \underline{id}$

Derivations



- At each step, we choose a non-terminal to replace
- Different choices can lead to different derivations

Two derivations are of interest

- Leftmost derivation replace leftmost NT at each step
- *Rightmost derivation* replace rightmost NT at each step

These are the two *systematic* derivations (We don't care about randomly-ordered derivations!)

The example on the preceding slide was a *leftmost* derivation

- Of course, there is also a *rightmost* derivation
- Interestingly, it turns out to be different



In both cases, $Expr \Rightarrow^* \underline{id} - \underline{num} * \underline{id}$

- The two derivations produce different parse trees
- The parse trees imply different evaluation orders!

Rule	Sentential Form
—	Expr
1	Expr Op Expr
3	<id,<mark>x> <i>Op Expr</i></id,<mark>
5	<id,<u>x> - Expr</id,<u>
1	<id,<u>x> - Expr Op Expr</id,<u>
2	<id,<mark>x> - <num,<u>2> <i>Op Expr</i></num,<u></id,<mark>
6	<id,<u>x> - <num,<u>2> * <i>Expr</i></num,<u></id,<u>
3	<id,<u>x> - <num,<u>2> * <id,<u>y></id,<u></num,<u></id,<u>

Leftmost derivation

Rule	Sentential Form
	Expr
1	Expr Op Expr
3	<i>Expr Op<</i> id, <u>y</u> >
6	Expr * <id,<u>y></id,<u>
1	<i>Expr Op Expr</i> * <id,<u>y></id,<u>
2	<i>Expr Op<</i> num, <mark>2</mark> > * <id,<u>y></id,<u>
5	<i>Expr</i> - <num,<u>2> * <id,<u>y></id,<u></num,<u>
3	<id,<u>x> - <num,<u>2> * <id,<u>y></id,<u></num,<u></id,<u>

Rightmost derivation

Derivations and Parse Trees

Leftmost derivation

Rule	Sentential Form
	Expr
1	Expr Op Expr
3	<id,<mark>x> <i>Op Expr</i></id,<mark>
5	<id,<u>x> - Expr</id,<u>
1	<id,<u>x> - Expr Op Expr</id,<u>
2	<id,<u>x> - <num,<u>2> <i>Op Expr</i></num,<u></id,<u>
6	<id,<u>x> - <num,<u>2> * <i>Expr</i></num,<u></id,<u>
3	<id,<u>x> - <num,<u>2> * <id,<u>y></id,<u></num,<u></id,<u>

This evaluates as $\underline{x} - (\underline{2} * \underline{y})$





Derivations and Parse Trees

Rightmost derivation

Rule	Sentential Form
_	Expr
1	Expr Op Expr
3	<i>Expr Op</i> <id,<mark>y></id,<mark>
6	Expr * <id,<u>y></id,<u>
1	<i>Expr Op Expr</i> * <id,<u>y></id,<u>
2	<i>Expr Op</i> <num,<u>2> * <id,<u>y></id,<u></num,<u>
5	<i>Expr-</i> <num,<u>2> * <id,<u>y></id,<u></num,<u>
3	<id,<u>x> - <num,<u>2> * <id,<u>y></id,<u></num,<u></id,<u>

This evaluates as $(\underline{x} - \underline{2}) * \underline{y}$







These two derivations point out a problem with the grammar: It has no notion of precedence, or implied order of evaluation

To add precedence

- Create a non-terminal for each *level of precedence*
- Isolate the corresponding part of the grammar
- Force the parser to recognize high precedence subexpressions first

For algebraic expressions

- Multiplication and division, first
- Subtraction and addition, next

(level one) (level two)

Derivations and Precedence



Adding the standard algebraic precedence produces:

	1	Goal	\rightarrow	Expr
, , (2	Expr	Ŷ	Expr + Term
level	3			Expr - Term
two	4			Term
, , , ,	5	Term	1	Term * Factor
level	6			Term / Factor
one	7			Factor
	8	Factor		number
	9			id

This grammar is slightly larger

- Takes more rewriting to reach some of the terminal symbols
- Encodes expected precedence
- Produces same parse tree under leftmost & rightmost derivations

Let's see how it parses x - 2 * y



The rightmost derivation

Its parse tree

This produces $\underline{x} - (\underline{2} * \underline{y})$, along with an appropriate parse tree. Both the leftmost and rightmost derivations give the same expression, because the grammar directly encodes the desired precedence.

Ambiguous Grammars



Our original expression grammar had other problems

- This grammar allows multiple leftmost derivations for <u>x</u> $\underline{2}$ * <u>y</u>
- Hard to automate derivation if > 1 choice
- The grammar is *ambiguous*

1	Expr	\rightarrow	Expr Op Expr
2			number
3			id
4	Ор	\rightarrow	+
5			-
6			*
7			/



different choice than the first time Two Leftmost Derivations for x - 2 * y

The Difference:

- > Different productions chosen on the second step
- Both derivations succeed in producing x 2 * y

Rule	Sentential Form
_	Expr
1	Expr Op Expr
3	<id,<u>×> <i>Op Expr</i></id,<u>
5	<id,<u>x> - <i>Expr</i></id,<u>
1	<id,<u>x> - Expr Op Expr</id,<u>
2	<id,<u>x> - <num,<u>2> Op Expr</num,<u></id,<u>
6	<id,<u>x> - <num,<u>2> * <i>Expr</i></num,<u></id,<u>
3	<id,<u>x> - <num,<u>2> * <id,<u>y></id,<u></num,<u></id,<u>

Rule	Sentential Form
	Expr
1	Expr Op Expr
	Expr Op Expr Op Expr
3	<id,<u>x> <i>Op Expr Op Expr</i></id,<u>
5	<id,<u>x> - Expr Op Expr</id,<u>
2	<id,<u>x> - <num ,<u="">2> Op Expr</num></id,<u>
6	<id,<u>x> - <num ,<u="">2> * <i>Expr</i></num></id,<u>
3	<id,<u>x> - <num,<u>2> * <id,<u>y></id,<u></num,<u></id,<u>

Original choice

New choice





Definitions

- If a grammar has more than one leftmost derivation for a single sentential form, the grammar is ambiguous
- If a grammar has more than one rightmost derivation for a single sentential form, the grammar is *ambiguous*
- The leftmost and rightmost derivations for a sentential form may differ, even in an unambiguous grammar

Classic example — the *if-then-else* problem

 $\begin{array}{rcl} \textit{Stmt} \rightarrow & \underline{\text{if}} & \textit{Expr} & \underline{\text{then}} & \textit{Stmt} \\ & | & \underline{\text{if}} & \textit{Expr} & \underline{\text{then}} & \textit{Stmt} & \underline{\text{else}} & \textit{Stmt} \\ & | & ... & \textit{other stmts} & ... \end{array}$

This ambiguity is entirely grammatical in nature

Ambiguity



This sentential form has two derivations

 $\underline{if} Expr_1 \underline{then} \underline{if} Expr_2 \underline{then} Stmt_1 \underline{else} Stmt_2$



Ambiguity



Removing the ambiguity

- Must rewrite the grammar to avoid generating the problem
- Match each <u>else</u> to innermost unmatched <u>if</u> (common sense rule) With this grammar, the example has only one derivation

1	Statement	\rightarrow	<u>if</u> Expr <u>then</u> Statement
2			<u>if</u> Expr <u>then</u> WithElse <u>else</u> Statement
3			Assignment
4	WithElse	\rightarrow	<u>if</u> Expr <u>then</u> WithElse <u>else</u> WithElse
5			Assignment

Intuition: binds each else to the innermost if

Ambiguity



<u>if $Expr_1$ then if $Expr_2$ then Assignment₁ else Assignment₂</u>

Rule	Sentential Form
	Statement
1	<u>if</u> Expr <u>then</u> Statement
2	if Expr then if Expr then WithElseelse Statement
3	if Expr then if Expr then WithElseelse Assignment
5	if Expr then if Expr then Assignmentelse Assignment

This binds the <u>else</u> controlling Assignment₂ to the inner <u>if</u>

Deeper Ambiguity



Ambiguity usually refers to confusion in the CFG

Overloading can create deeper ambiguity

a = f(17)

In many Algol-like languages, <u>f</u> could be either a function or a subscripted variable

Disambiguating this one requires context

- Need values of declarations
- Really an issue of *type*, not context-free syntax
- Requires an extra-grammatical solution (not in CFG)
- Must handle these with a different mechanism
 - \rightarrow Step outside grammar rather than use a more complex grammar

Ambiguity arises from two distinct sources

- Confusion in the context-free syntax
- Confusion that requires context to resolve

Resolving ambiguity

- To remove context-free ambiguity, rewrite the grammar
- To handle context-sensitive ambiguity takes cooperation
 - → Knowledge of declarations, types, ...
 - \rightarrow Accept a superset of L(G) & check it by other means[†]
 - \rightarrow This is a language design problem

Sometimes, the compiler writer accepts an ambiguous grammar

- → Parsing techniques that "do the right thing"
- \rightarrow *i.e.*, always select the same derivation



(<u>if-then-else</u>) (overloading)