## CISC320 Algorithms, Homework set 1 Due Tuesday, Sept 14, 2010

- 1. Find a counterexample consisting of 4 points in the plane to the proposition that the closest pair algorithm (pg 6) produces a solution to the robot tour optimization problem (pg 5). Explain how the algorithm fails on your counterexample.
- 2. Exercise 1-5.
- 3. Exercise 1-12.
- 4. Exercise 1-18. This is the rather surprising identity that the square of the sum of the first n positive integers is the sum of their cubes. You can establish this identity directly by induction or you can do exercise 1.10 using induction and follow up by using 1-10 and 1-12 to establish this identity. The second approach may be simpler.
- 5. 2-2.
- 6. 2-7. Explain your reasoning.
- 7. 2-11.
- 8. a) Show that  $n\log(n)$  is  $\Theta(\sum_{i=1}^{n}\log(i))$ .
  - b) Show that  $n\log(n)$  is  $\Theta(\log(n!))$ .

Hint: for the lower bound, you can use the largest half strategy. You may also use the transitivity of  $\Theta$ : if  $f(n) = \Theta(g(n))$  and  $g(n) = \Theta(h(n))$ , then  $f(n) = \Theta(h(n))$ .