CISC320 Algorithms, Homework set 1 Due Tuesday, Sept 14, 2010

1. Find a counterexample consisting of 4 points in the plane to the proposition that the closest pair algorithm ( $\operatorname{pg} 6$ ) produces a solution to the robot tour optimization problem (pg 5). Explain how the algorithm fails on your counterexample.
2. Exercise 1-5.
3. Exercise 1-12.
4. Exercise 1-18. This is the rather surprising identity that the square of the sum of the first $n$ positive integers is the sum of their cubes. You can establish this identity directly by induction or you can do exercise 1.10 using induction and follow up by using 1-10 and 1-12 to establish this identity. The second approach may be simpler.
5. 2-2.
6. 2-7. Explain your reasoning.
7. 2-11.
8. a) Show that $n \log (n)$ is $\Theta\left(\sum_{i=1}^{n} \log (i)\right)$.
b) Show that $n \log (n)$ is $\Theta(\log (n!))$.

Hint: for the lower bound, you can use the largest half strategy. You may also use the transitivity of $\Theta$ : if $f(n)=\Theta(g(n))$ and $g(n)=\Theta(h(n))$, then $f(n)=\Theta(h(n))$.

