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# TEST GENERATION IN THE PRESENCE OF CONFLICTING TIMERS

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Abstract The UD's and CCNY's ongoing research to generate conformance tests for the Army network protocol MIL-STD 188-220 addressed test generation when multiple timers are running simultaneously. A test sequence may become unrealizable if there are conflicting conditions based on a protocol's timers. This problem is handled in the hitherto generated tests by manually expanding a protocol's extended FSM based on the set of conflicting timers, resulting in test sequences that are far from minimum-length. Similar inconsistencies, but based on arbitrary linear variables, are present in the extended FSMs modeling VHDL specifications. This paper presents an efficient solution to the conflicting timers problem that eliminates the redundancies of manual state expansion. CCNY's inconsistency removal algorithms are applied to a new model for testing protocols with multiple timers, in which complex timing dependencies are captured by simple linear expressions. This test generation technique is expected to significantly shorten the test sequences without compromising their fault coverage.

Keywords: conformance testing; test case generation; timing constraints; timer testing

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### 1. INTRODUCTION

The on-going collaboration between the City College of the City University of New York (CCNY) and the University of Delaware (UD) [7] focuses on the generation of test cases automatically from Estelle specifications. Tests are being generated for the US Department of Defense (DoD)/Joint protocol military standard developed in the US Army, Navy and Marine Corps systems for mobile combat network radios [7]. Within this effort, several theoretical problems have been investigated, including generation of test sequences uninterrupted by active timers [21], and the improvement of test coverage by using the semicontrollable interfaces [8].

This paper studies the problem of test case generation for network protocols with timers, where a test sequence may become unrealizable due to conflicting conditions based on a protocol's timers. This problem is termed the *conflicting timers problem*.

The research has been motivated by the ongoing effort to generate tests for MIL-STD 188-220. The protocol's Datalink Layer defines several timers that can run concurrently and affect the protocol's behavior. For example, *BUSY* and *ACK* timers may be running independently in *FRAME\_BUFFERED* state. If either timer is running, a buffered frame cannot be transmitted. If *ACK* timer expires while *BUSY* timer is <u>not</u> running, a buffered frame is retransmitted. If, however, *ACK* timer expires while *BUSY* timer is running, no output is generated.

In the test cases delivered to the US Army Communications-Electronics Command (CECOM), such conflicts are handled by manually expanding EF-SMs based on the set of conflicting timers. This procedure results in test sequences that are far from minimum-length [7]. Similar conflicts, but based on arbitrary linear variables, are present in EFSM models of VHDL specifications [19]. Uyar and Duale present algorithms for detecting [19] and removing [5, 20] such inconsistencies in VHDL specifications. Current research at UD and CCNY focuses on adapting these algorithms to eliminate inconsistencies caused by a protocol's conflicting timers, with a view to applying the methodology to conformance test generation for MIL-STD 188-220.

This paper presents a new model for testing real-time protocols with multiple timers, which captures complex timing dependencies by using simple linear expressions. This modeling technique, combined with the CCNY's inconsistency removal algorithms, is expected to significantly shorten test sequences without compromising their fault coverage.

The proposed solution is expected to have a broader application due to a recent proliferation of protocols with real-time requirements [12, 15]. The functional errors in such protocols are usually caused by the unsatisfiability of time constraints and (possibly conflicting) conditions involving timers; therefore, significant research is required to develop efficient algorithms for test generation for such protocols. The results presented here are expected to contribute towards achieving this goal.

## 2. **PROBLEM DEFINITION**

Suppose that a protocol specification defines a set of timers  $K = \{tm_1, \ldots, tm_{|K|}\}$ , such that a timer  $tm_j$  may be started and stopped by arbitrary transitions defined in the specification. Each timer  $tm_j$  can be associated with a boolean variable  $T_j$  whose value is true if  $tm_j$  is running, and false if  $tm_j$  is not running. Let  $\phi$  be a time formula obtained from variables  $T_1, \ldots, T_k$  by using logical operands  $\land, \lor$ , and  $\neg$ . Suppose that a specification contains transitions with time conditions of a form "if  $\phi$ " for some time formula  $\phi$ . It is clear that there may exist infeasible paths in an FSM modeling a protocol, if two or more edges in a path have inconsistent conditions. For example, for transitions  $e_1$ : if  $(T_j)$  then  $\{\varphi_1\}$  and  $e_2$ : if  $(\neg T_j)$  then  $\{\varphi_2\}$ , a path  $(e_1, e_2)$  is inconsistent unless the action of  $\varphi_1$  in  $e_1$  sets  $T_j$  to false (which happens when timer  $tm_j$  expires in transition  $e_1$ ). The solution to the above problem is expected to allow generating low-cost tests free of such conflicts.

The conflicting timers problem is a special case of the feasibility problem of test sequences, which is an open research problem for the general case [9, 18]. However, there are two simplifying features of the conflicting timers problem: (1) time variables are linear, and (2) time-keeping variable values implicitly increase with time. By considering these features, we expect to find an efficient solution to this special case.

## 2.1 GENERAL APPROACH

The goal of the presented technique is to achieve at least the following fault coverage: *cover every state transition at least once*. During the testing of a system with multiple timers, when a node  $v_p$  is visited, an efficient test sequence should either (1) traverse as many self-loops as possible before a timeout or (2) leave  $v_p$  immediately through a non-timeout transition. Once the maximum allowable number of self-loops are traversed, a test sequence may leave  $v_p$  through any outgoing transition. Such an approach does not let perform full reachability analysis; however, it can be easily proven that considering only the above two cases is sufficient to include at least one feasible path for each transition (if such a feasible path is not prohibited by the original specification).

In general, the goal of an optimization is to generate a low-cost test sequence that follows the above guidelines, satisfies time conditions of all composite edges and is not disrupted by timeout events during traversal (i.e., contains only feasible transitions). In Section 3., a model will be introduced that allows the generation of test sequences satisfying the above criteria.

## 2.2 RELATED WORK

Conformance test generation is an active research area [1, 3, 9, 11, 14, 17, 18]. The related work on testing systems with timing dependencies focuses on testing the so-called Timed Automata (TA) [2, 16], which are a formalism primarily used in system verification. However, there is relatively little work reported in the literature on successful application of timed automata to conformance testing. (Other FDTs, such as ET-LOTOS [13], can also be used to describe timed systems.)

Springintveld et al. [16] present the first published theoretical framework for testing timed automata. En-Nouaary et al. [6] introduce a method based on the state characterization technique using a timed extension of the Wp-method [9]. Higashino et al. [10] define several kinds of test sequence executability for real-time systems and present an algorithm for verifying if a test sequence is executable. Cardell-Oliver and Glover [4] propose a method based on the model of Timed Transition Systems (TTSs) [2].

A major goal of these methods is to limit the number of tests, which otherwise may become prohibitively large; hence, each technique offers a means to reduce the test suite size. The reader may consult the relevant papers [4, 6, 10, 16] for more details.

The new model presented in this paper offers several advantages over the TA-based modeling:

- it is tailored-designed only for testing purposes, which does not require to perform full reachability analysis;
- it allows more intuitive modeling of an IUT and testing procedure (each input/output exchange is assigned certain time to realize; there are no instantaneous transitions as in TA);
- it makes it possible to define a timer length as a constant or variable rather than a fixed value as in TA, with which many properties such as service delivery, proper timeout settings, etc. can be modeled and tested.

# 3. NOVEL MODEL FOR TESTING SYSTEMS WITH TIMERS

A protocol can be modeled as a deterministic, completely specified FSM (Mealy) represented by a directed graph G(V, E) and a set of timers  $K = \{tm_1, \ldots, tm_{|K|}\}$ . As part of this model, we also introduce a set of constants and the set of variables  $\mathcal{V} = \{T_1, f_1, \ldots, T_{|K|}, f_{|K|}, L_1, \ldots, L_{|V|}, t_{1,1}^s, \ldots, t_{|V|, M_{|V|}}\}$ , as defined below.

For each timer  $tm_j$ , we introduce the following parameters:

- $T_j \in \{0, 1\}$ —boolean variable indicating if the timer is running.  $T_j = 1$  if  $tm_j$  is running;  $T_j = 0$  otherwise
- $D_j \in \mathcal{R}^+$ —the timeout value (i.e., timer length) for  $tm_j$

•  $f_j \in \mathcal{R}^+ \cup \{0\} \cup \{-\infty\}$ —time-keeping variable denoting the current time of  $tm_j$ . If  $0 \leq f_j < D_j$ , then  $tm_j$  is running; if  $f_j \geq D_j$  or  $f_j = -\infty$ ,  $tm_j$  is not running. (It is expired or stopped).  $f_j$  is set to 0 when  $tm_j$  is started; it is set to  $-\infty$  when  $tm_j$  is stopped or has expired.

Let us define  $\text{EX}(T_1, \ldots, T_{|K|})$  as the set of all boolean expressions on  $T_1, \ldots, T_{|K|}$ . Let a time formula  $\phi$  be defined as an element of EX.

A transition  $e_i \in E$  is associated with the following parameters:

- $c_i \in \mathcal{R}^+$ —the time needed to traverse  $e_i$
- time condition  $\langle \phi_i \rangle e_i$  can trigger only if its associated time formula  $\phi_i$  is satisfied; if no time formula is associated with  $e_i$ , its time condition is  $\langle 1 \rangle$ . For example, if  $e_i$ 's time condition involves  $\phi_i = T_1 \land \neg T_3$ , the transition can trigger only if  $tm_1$  is running and  $tm_3$  is not running, regardless of the state of other timers
- action list  $\{\varphi_{i,1}, \varphi_{i,2}, \ldots\}$ —each action  $\varphi_{i,k}$  is an ordered pair  $(x \in \mathcal{V}, \text{update}(x) \in \text{EX}(\mathcal{V}, \mathcal{R}, \{+, -, *, /\})$ , where update(x) belongs to the set of all linear expressions involving  $\mathcal{V}$ , the set of real numbers  $\mathcal{R}$ , and arithmetic operands. Expression update(x) is used to update x's value, e.g., the two actions of  $\{T_1 = 1; f_2 = f_2 + 5\}$  start timer  $tm_1$  and increment the value of the time-keeping variable associated with timer  $tm_2$  by 5 units

The following parameters are defined for each state  $v_p \in V$ :

- c<sup>s</sup><sub>p</sub> ∈ R<sup>+</sup>—the time needed to traverse a self-loop of v<sub>p</sub>. The majority of self-loops are inopportune transitions, whose traversal times are therefore comparable and can be approximated with c<sup>s</sup><sub>p</sub>
- $N_{p,l}^{s}$ —a set of merged non-timeout self-loops of  $v_{p}$  sharing the same time condition  $\langle \phi_{p,l} \rangle$ , where  $1 \leq l \leq M_{p}$ . (A self-loop that starts/stops a timer cannot be merged with others)
- $M_p$ —the number of sets of  $N_{p,l}^s$  for node  $v_p$
- $t_{p,l}^s$ —the number of untested self-loops in  $N_{p,l}^s$ .  $t_{p,l}^s$  is initialized to  $|N_{p,l}^s|$
- $L_p \in \{0, 1, 2\}$ —the 'exit' condition for state  $v_p$ . If  $L_p = 0$ , no transition outgoing from  $v_p$  and no timeout transition in  $v_p$  may be traversed; if  $L_p = 1$ , a test sequence may leave  $v_p$  through an outgoing non-timeout transition; if  $L_p = 2$ , any outgoing transitions (including timeouts) may be traversed

In the next three sections, the time-related behavior of the IUT will be modeled by defining proper time constraints and actions for various types of transitions defined in the specification.

## **3.1 TYPES OF TRANSITIONS**

In general, the model distinguishes four types of transitions:

- Type 1: timeout transition  $e_i^j(v_p, v_q)$ , defined for each timer  $tm_j$  ( $e_i^j$  may be a self-loop, i.e., p = q)
- Type 2: non-timeout non-self-loop transition  $e_i(v_p, v_q)$ , where  $p \neq q$
- Type 3: merged self-loop transition  $e_{p,l}(v_p, v_p)$ , defined for each node  $v_p$  and each set  $N_{p,l}^s$
- Type 4: merged self-loop transition  $e_{p,l}^{j}(v_{p}, v_{p})$ , defined for each node  $v_{p}$ , each set  $N_{p,l}^{s}$  that contains more than one self-loop, and each timer  $tm_{j}$

While visiting  $v_p$ , if there is enough time to test all self-loops of  $N_{p,l}^s$  before any timer expires,  $e_{p,l}$  (*Type 3*) will be traversed; otherwise,  $e_{p,l}^j$  (*Type 4*) will be traversed with  $tm_j$  expiring before all self-loops of  $N_{p,l}^s$  can be tested.

#### 3.2 CONDITIONS

A number of timing constraints must be appended to the time conditions for all transitions, as defined below.

For each timeout transition  $e_i^j(v_p, v_q)$  (*Type 1*), the following condition holds for each timer  $tm_{k\neq j}$ : *`exit' condition for timeouts in*  $v_p$  *true* <u>AND</u> *timer*  $tm_j$  *running* <u>AND</u> (*timer*  $tm_k$  *not running* <u>OR</u>  $tm_j$  *expires before*  $tm_k$ ), which is formalized as:

$$\langle (L_p == 2) \land (T_j == 1) \land ((T_j == 0) \lor (D_j - f_j < D_k - f_k)) \rangle \equiv \\ \langle (L_p == 2) \land (T_j == 1) \land (D_j - f_j < D_k - f_k) \rangle$$

For each non-timeout non-self-loop  $e_i(v_p, v_q)$  (Type 2), the following condition holds for each timer  $tm_k$ : 'exit' condition for  $v_p$  true <u>AND</u> (timer  $tm_k$  not running <u>OR</u> there is time left to  $tm_k$ 's timeout). Formally, this condition is:

$$\langle (L_p > 0) \land ((T_j == 0) \lor (f_k < D_k)) \rangle \equiv \langle (L_p > 0) \land (f_k < D_k) \rangle \rangle$$

For each merged self-loop transition  $e_{p,l}$  (*Type 3*), the following condition holds for each timer  $tm_k$ : there are untested self-loops in  $N_{p,l}^s$  <u>AND</u> (timer  $tm_k$  not running <u>OR</u> all untested self-loops of  $N_{p,l}^s$  can be tested before  $tm_k$ expires). For each  $e_{p,l}$ , all self-loops  $N_{p,l}^s$  can be tested by traversing  $e_{p,l}$ . This condition can be formalized as:

$$\begin{array}{l} \langle (t_{p,l}^{s} > 0) \land ((T_{j} == 0) \lor (t_{p,l}^{s} * c_{p}^{s} < D_{k} - f_{k})) \rangle & \equiv \\ & \langle (t_{p,l}^{s} > 0) \land (t_{p,l}^{s} * c_{p}^{s} < D_{k} - f_{k}) \rangle \end{array}$$

For each merged self-loop transition  $e_{p,l}^{j}$  (*Type 4*), the following condition holds for each timer  $tm_{k\neq j}$ : there are untested self-loops in  $N_{p,l}^{s}$  <u>AND</u> (timer  $tm_{j}$  running <u>AND</u> there is enough time left before  $tm_{j}$  expires to test at least one but not all untested self-loops in  $N_{p,l}^{s}$ ) <u>AND</u> (timer  $tm_{k}$  not running <u>OR</u>  $tm_j$  expires before  $tm_k$ ). In other words, only some of the self-loops of  $N_{p,l}^s$  can be tested by traversing  $e_{p,l}^j$ . Formally, this condition is:

$$\begin{array}{l} \langle (t_{p,l}^{s} > 0) \land ((T_{j} = = 1) \land (c_{p}^{s} < D_{j} - f_{j} < t_{p,l}^{s} * c_{p}^{s})) \land ((T_{k} = = 0) \lor \\ (D_{j} - f_{j} < D_{k} - f_{k})) \rangle & \equiv \langle (t_{p,l}^{s} > 0) \land (T_{j} = = 1) \land \\ (c_{p}^{s} < D_{j} - f_{j} < t_{p,l}^{s} * c_{p}^{s}) \land (D_{j} - f_{j} < D_{k} - f_{k}) \rangle \end{array}$$

#### 3.3 ACTIONS

A number of actions must be appended to the action lists for all transitions, as defined below.

For each timeout transition  $e_i^j(v_p, v_q)$  (*Type 1*), for each  $k \neq j$ :

- set variable  $T_i$  to 0 indicating timer expiry:  $T_i = 0$
- increment  $tm_k$ 's current time by the sum of  $e_i$ 's traversal time and the amount of time left until  $tm_j$ 's timeout:  $f_k = f_k + c_i + \max(0, D_j f_j)$
- set  $tm_j$ 's time-keeping variable:  $f_j = -\infty$

Since 'max' is not a linear action, to utilize any test generation technique that allows only linear actions (as in [20]),  $e_i^j$  should be split into  $e_{i,1}^j$  and  $e_{i,2}^j$  as follows:

$$\begin{aligned} e_{i,1}^{j} : & \langle (L_p == 2) \land (T_j == 1) \land (f_j \ge D_j) \land (D_j - f_j < D_k - f_k) \rangle \\ & \{T_j = 0; f_k = f_k + c_i; f_j = -\infty \} \\ e_{i,2}^{j} : & \langle (L_p == 2) \land (T_j == 1) \land (f_j < D_j) \land (D_j - f_j < D_k - f_k) \rangle \\ & \{T_j = 0; f_k = f_k + c_i + D_j - f_j; f_j = -\infty \} \end{aligned}$$

The above concept is illustrated in Figure 1. Timer  $tm_j$  is started at time  $f_j = 0$ . After  $f_j$  reaches a value of  $f_j^0$ , the two feasible transitions are  $e_1$  and  $e_2$ . Consider the case where  $e_1$  triggers and  $f_j$  is advanced to a value of  $f_j^1 = f_j^0 + c_1 < D_j$ . In this case,  $tm_j$ 's timeout corresponds to traversing  $e_{i,2}^j$ , which advances all timers by  $c_i + D_j - f_j^1$ . In the case where  $e_2$  triggers,  $f_j$  is advanced to a value of  $f_j^2 = f_j^0 + c_2 > D_j$ , with  $tm_j$ 's timeout modeled by  $e_{i,1}^j$ . All timers will be advanced by  $e_{i,1}^j$  only by its execution time  $c_i$ , because timer  $tm_j$  expired while  $e_2$  was being traversed.

In addition, a non-self-loop  $e_i^j$  should set the 'exit' condition for its end state  $v_q$  to 1 by the appended action of  $\{L_q = 1\}$ .

For each non-timeout non-self-loop  $e_i(v_p, v_q)$  (*Type 2*):

- set the 'exit' condition for  $e_i$ 's end state  $v_q$  to true:  $L_q = 1$
- for each k, increment  $tm_k$ 's current time by  $e_i$ 's traversal time:  $f_k = f_k + c_i$

For each merged self-loop transition  $e_{p,l}$  (*Type 3*):

• set the 'exit' condition for state  $v_p$  to false:  $L_p = 0$ 



Time dependencies in timeout transition  $e_i^j$ . Figure 1

- for each k, increment  $tm_k$ 's current time by the time needed to traverse all untested self-loops in  $N_{p,l}^s$ :  $f_k = f_k + t_{p,l}^s * c_p^s$ • set the number of untested self-loops in  $N_{p,l}^s$  to 0:  $t_{p,l}^s = 0$

If no self-loops can be traversed (i.e., there are no untested self-loops of  $v_p$ whose time condition is satisfied),  $L_p$  should be set to 2 (from either 0 or 1), enabling timeouts and all outgoing transitions in  $v_p$ . In this case,  $L_p$  will be set to 2 by a so-called observer self-loop transition  $s_p$ , with the following condition:

for each l: 
$$\langle (L_p < 2) \land (t_{p,l}^s = 0 \lor (t_{p,l}^s > 0 \land \neg \phi_{p,l})) \rangle$$
 (1.1)

and an action  $\{L_p = 2\}$ . Condition (1.1) is satisfied when all self-loops of  $v_p$ whose time condition is satisfied are tested (if there are no self-loops defined for  $v_p$ , the condition is trivially true).

For each merged self-loop transition  $e_{p,l}^{j}$  (*Type 4*):

- set the 'exit' condition for state  $v_p$  to true:  $L_p = 2$
- for each k, increment  $tm_k$ 's current time by the time needed to traverse all of the untested self-loops in  $N_{p,l}^s$  that can be tested before  $tm_j$  expires:  $f_k = f_k + c_p^s * \lfloor (D_j - f_j) / c_p^s \rfloor$ • decrement the number of untested self-loops:  $t_{p,l}^s = t_{p,l}^s - \lfloor (D_j - f_j) / c_p^s \rfloor$

The 'exit' condition  $L_p$  works as follows. A test sequence comes to state  $v_p$  through an incoming edge, which sets  $L_p$  to 1. Then the test sequence may leave immediately through an outgoing non-timeout edge, or take Type 3 and/or Type 4 edges. Once Type 3 edge is taken, it sets  $L_p$  to 0, preventing a test sequence from leaving a state and timeouts from occurring. Then the test sequence may include either a Type 4 edge (which sets  $L_p$  to 2, thus enabling timeouts and outgoing edges) or traverse further Type 3 edges. If neither Type 3 nor Type 4 edges can be traversed (this includes the case where none are defined for  $v_p$ ), the observer edge  $s_p$  sets  $L_p$  to 2.

Condition (1.1) results in  $2^{M_p}$  parallel edges due to the presence of  $M_p$  number of "OR" statements. Clearly, the technique does not scale well. To prevent the exponential growth of the number of parallel edges,  $s_p$  will be replaced with the set of vertices and edges as depicted in Figure 2. The appended conditions and actions of the edges in Figure 2 are derived from (1.1) as follows:

$$s'_{n,l} : \langle L_p < 2 \land t^s_{n,l} == 0 \rangle \{\}, \qquad \check{s}_p : \langle 1 \rangle \{L_p = 2\}$$
(1.2)

$$s_{p,l}'': \langle L_p < 2 \land (t_{p,l}^s > 0 \land \neg \phi_{p,l}) \rangle \{\}$$
(1.3)

Condition (1.1) is satisfied when a feasible path exists from  $v_p$  to  $w_{p,M_p}$ . Since the edges of  $s'_{p,k}$  and  $s''_{p,k}$  are mutually exclusive, only one such a path is possible. The outgoing edge of  $w_{p,M_p}$ , i.e.,  $\check{s}_p$ , sets the 'exit' condition to true.



Figure 2 Graph extension to make an observer transition  $s_p$  scalable.

# MODEL REFINEMENT MODIFYING NONLINEAR ACTIONS

As can be seen, *Type 4* actions are non-linear, since the number of self-loop traversals before a timeout is computed in  $e_{p,l}^j$ 's actions by rounding down a fractional value to an integer  $z = \lfloor (D_j - f_j)/c_p^s \rfloor$ . Since VHDL inconsistencies removal algorithms are applicable only to linear actions, this nonlinearity will be removed by avoiding the computation of z. Instead, a test sequence is forced to traverse one of a number of extra edges with the index of the traversed extra edge equal to z.

To employ this idea, the following steps are taken. Let us first note that  $Z_{p,l}$ , the number of self-loops of  $N_{p,l}$  that can be traversed in any *Type 4* transition, is upper bounded by the cardinality of  $N_{p,l}^s$  and the maximum number of self-loop traversals allowed by timers, as defined in (1.4). The maximum number of self-loop traversals at any time during the execution of a test sequence is therefore obtained by (1.4).

$$Z = \max_{p,l} Z_{p,l}^{s}, \quad \text{where} \quad Z_{p,l}^{s} = \min(|N_{p,l}^{s}| - 1, \max_{k \le |K|} \lfloor D_{k} / c_{p}^{s} \rfloor) \quad (1.4)$$

Having computed the value of Z, we define additional variables D,  $c^s$ , z, and r, and extend graph G(V, E) with two vertices  $u_1$  and  $u_2$ , as depicted in Fig-

ure 3. Next, each  $e_{p,l}^j(v_p, v_p)$  is replaced with  $\hat{e}_{p,l}^j(v_p, u_1)$ , with the unchanged conditions, and the following actions:

- memorize which set of  $N_{p,l}$  is represented: r = p.l
- set the cost of a self-loop traversal:  $c^s = c_p^s$
- set the time remaining until timeout:  $D = D_j f_j$



Figure 3 Graph extension to remove nonlinear actions.

Vertices  $u_1$  and  $u_2$  are connected with extra edges  $h_1, \ldots, h_Z$ , with the following condition for  $h_m$ : there is enough time left before a timer expires to test m but not m + 1 untested self-loops. Using the additional variables, this condition can be formalized as  $\langle m + 1 \rangle D/c^s \geq m \rangle$ . The action of  $h_m$  sets the value of z to  $h_m$ 's index m:  $\{z = m\}$ . In this way, since the conditions of  $h_1, \ldots, h_Z$  are mutually exclusive, only one transition  $h_m$  indicating the proper number m of allowed self-loop traversals will be traversed (setting z to a value of m).

Finally,  $M_p$  edges of  $\hat{e}_{p,l}(u_2, v_p)$  are added from  $u_2$  to each  $v_p$  with Type 4 edges, with the condition of  $\langle r == p.l \rangle$ , which allows a test sequence that left  $v_p$  through  $\hat{e}_{p,l}^j$  to return to the same  $v_p$ , and decrement the proper  $t_{p,l}^s$ . The linear actions of  $\hat{e}_{p,l}$  replace the nonlinear actions of  $e_{p,l}^j$  as follows:

- set 'exit' condition for  $v_p$  to true:  $L_p = 2$
- for each k, increment  $tm_k$ 's current time by the time needed to traverse all of the untested self-loops in  $N_{p,l}^s$  that can be tested before timeout:  $f_k = f_k + c^s * z$
- decrement the number of untested self-loops:  $t_{p,l}^s = t_{p,l}^s z$

#### 4.2 DELAYING START OF TIMERS

Every transition  $e_i$  has the appended conditions and actions as defined in Section 3.. In addition, if  $e_i$  stops timer  $tm_j$ , the actions of  $\{T_j = 0; f_j = -\infty\}$  must be appended to  $e_i$ 's action list. If  $e_i$  starts timer  $tm_j$ , the two actions of  $\{T_i = 1; f_j = 0\}$  must be appended to  $e_i$ 's action list.

To have good test coverage, a test sequence should traverse all feasible transitions of an IUT. Some edges in the IUT graph are reachable only if a transition(s) that starts a timer is *delayed* in the test sequence by certain amount of time. The action of delaying such transitions allows us to explore various ordering of timers' expirations by causing certain timers to expire before others.



Figure 4 Delaying transition  $e_i$ : (a) all timers inactive, no delay; (b)  $tm_a$  to expire first, delay less than  $D_a - f_a$ ; (c)  $tm_a$  to expire first, delay greater than  $D_a - f_a$  cannot be applied due to  $tm_a$ 's timeout.

Suppose that  $e_i = (v_p, v_q)$  starts timer  $tm_j$ . Before  $e_i$  is traversed, one of the timers—say  $tm_a$ —is to expire first. Let  $d_i^m$  be the amount of time by which  $e_i$  is delayed in this case. It is clear that if  $e_i$  is to be traversed instead of  $tm_a$ 's timeout,  $d_i^m$  must be less than  $D_a - f_a$  (Figure 4 (b)). In the case where none of the timers are running before traversing  $e_i$  (Figure 4 (a)),  $d_i^m$  may be set to 0 because time passage does not affect system behavior if all timers are inactive.

Based on the above observations, each  $e_i$  will be replaced by two sets of transitions. The first one, which handles the case with  $d_i^m$  set to 0 where all timers are inactive before traversing  $e_i$ , contains transition  $e_i^0$ . Transition  $e_i^0$  has the following appended condition for each timer  $tm_k$ : timer  $tm_k$  not running. Formally, this condition is  $\langle T_k == 0 \rangle$ .

The second set, which handles the case where  $d_i^m$  is upper bounded by a running timer  $tm_a$  with the shortest time to expire, contains transitions  $e_i^a$ , defined for each  $a : 1 \le a < |K|$ . The transitions  $e_i^a$  have the following appended condition that holds for each timer  $tm_{k\neq a}$ : timer  $tm_a$  running <u>AND</u> timer  $tm_a$  is to expire before  $tm_k$ . Formally, this condition is:

$$\langle (T_a == 1) \land (D_a - f_a < D_k - f_k) \rangle$$

Each  $e_i^a$  also has the following appended action:

• for each k, increment  $tm_k$ 's current time by the introduced delay:  $f_k = f_k + d_i^m$ , where  $0 \le d_i^m < D_a - f_a$ In the above conversion,  $e_i$  is replaced with |K| + 1 transitions, out of which

In the above conversion,  $e_i$  is replaced with |K| + 1 transitions, out of which only one has a consistent condition, i.e.,  $e_i^0$  if no timer is running, or  $e_i^a$  for a particular  $tm_a$  that is to expire first.

The delay of  $d_i^m$  is involved in actions as a parameter with lower (0) and upper  $(D_a - f_a)$  bounds. During an application of the inconsistencies removal algorithm, the two inequalities of  $d_i^m \ge 0$  and  $d_i^m < D_a - f_a$  must be included in the consistency check of conditions involving  $d_i^m$ . The actual instantiation of  $d_i^m$ , i.e., assigning a particular value from between  $d_i^m$ 's bounds, takes place after generating a test sequence.

#### 5. APPLICATION TO EXAMPLE FSM

The FSM in Figure 5 consists of three states  $v_0$  (the initial state),  $v_1$ , and  $v_2$ , and eight transitions  $e_1$  through  $e_8$ . Transition  $e_3$  takes 3sec and the remaining transitions each take 1sec to traverse. There are two timers defined for the FSM:  $tm_1$  (started by  $e_2$ ) with the length of  $D_1 = 5.5$  and the timeout transition  $e_8$ , and  $tm_2$  (started by  $e_4$  and stopped by  $e_2$ ) with the length of  $D_2 = 3.7$ and the timeout transition  $e_7$ . Transition  $e_1$  is associated with time condition  $\langle T_1 == 0 \land T_2 == 1 \rangle$ , transitions  $e_5$  and  $e_6$  are associated with time condition  $\langle T_1 == 1 \land T_2 == 1 \rangle$ , and, for simplicity, the remaining transitions have the time condition  $\langle 1 \rangle$ .



Figure 5 FSM with conflicting timers  $tm_1$  and  $tm_2$ .

State  $v_t$  is introduced as the system initialization state, where a test sequence originates and terminates. A test sequence would start in state  $v_t$  with edge  $e_{\text{on}}$ :  $\langle 1 \rangle \{T_1 = 0; T_2 = 0; f_1 = -\infty; f_2 = -\infty; t_{0,1} = 1; t_{1,1} = 1; t_{2,1} = 2; L_0 = 1\}$ , which initializes all timers and the variables of  $t_{p,l}$ . A test sequence would terminate when, after arriving at  $v_0$ , edge  $e_{\text{off}} : \langle T_1 = 0 \land T_2 = 0 \rangle \{\}$  is traversed, bringing the IUT back to state  $v_t$ . The time condition of  $e_{\text{off}}$  ensures that all timers are inactive when the test sequence is terminated. Note that, unlike the regular states  $v_0$  through  $v_{|V|}, v_t$  is not split by the inconsistencies removal algorithm—the final inconsistency-free graph contains only one copy of  $v_t$ .

One can give examples of invalid test sequences for the FSM of Figure 5. A test sequence beginning with  $(e_{on}, e_1, e_2, ...)$  does not satisfy the time condition for  $e_1$ :  $\langle T_1 == 0 \land T_2 == 1 \rangle$ , since after traversing  $e_{on}$  (initial power-up), neither timer is running. Similarly, any test sequence containing  $(\ldots, e_4, e_7, e_5, \ldots)$  is invalid, because  $e_5$ 's time condition requires that both timers be running, which does not hold after  $tm_2$  expires in  $e_7$ .

Let us first consider transitions of *Type 1* ( $e_7, e_8$ ). Transition  $e_7$  has the following appended conditions and actions (the conditions and actions for  $e_8$ )

are analogous):

$$\begin{split} e_{7,1}^2 : & \langle L_2 == 2 \land f_2 \geq 3.7 \land (3.7 - f_2 < 5.5 - f_1) \land T_2 == 1 \rangle \\ & \{L_2 = 1; T_2 = 0; f_1 = f_1 + 1; f_2 = -\infty \} \\ e_{7,2}^2 : & \langle L_2 == 2 \land f_2 < 3.7 \land (3.7 - f_2 < 5.5 - f_1) \land T_2 == 1 \rangle \\ & \{L_2 = 1; T_2 = 0; f_1 = f_1 - f_2 + 4.7; f_2 = -\infty \} \end{split}$$

For transitions of *Type 2* ( $e_2$ ,  $e_4$ ), the appended conditions and actions are as follows:

$$\begin{array}{l} e_{2}: \langle L_{0} > 0 \ \land \ f_{1} < 5.5 \ \land \ f_{2} < 3.7 \rangle \\ \{f_{1} = f_{1} + 1; f_{2} = f_{2} + 1; L_{1} = 1; T_{1} = 1; f_{1} = 0; T_{2} = 0; f_{2} = -\infty \} \\ e_{4}: \langle L_{1} > 0 \ \land \ f_{1} < 5.5 \ \land \ f_{2} < 3.7 \rangle \\ \{L_{2} = 1; f_{1} = f_{1} + 1; f_{2} = f_{2} + 1; T_{2} = 1; f_{2} = 0 \} \end{array}$$

Vertex  $v_2$  has two merged self-loops in  $N_{2,1}^s = \{e_5, e_6\}$ . Therefore, transitions of both *Type 3*  $(e_{2,1})$  and *Type 4*  $(e_{2,1}^1, e_{2,1}^2)$  are defined in  $v_2$ . The value of Z is obtained from (1.4) as  $Z = Z_{2,1} = \min(1, \max(3, 5)) =$ 

The value of Z is obtained from (1.4) as  $Z = Z_{2,1} = \min(1, \max(3, 5)) = 1$ . The only extra edge  $h_1$  has the condition of  $\langle 2 * c^s \rangle D \geq c^s \rangle$ , and the action of  $\{z = 1\}$ . Edge  $\hat{e}_{2,1}$  has the condition of  $\langle r = 2.1 \rangle$ , and the actions of  $\{L_p = 2; f_k = f_k + c^s * z; t_{2,1}^s = t_{2,1}^s - z\}$ . Edge  $e_{2,1}^1$  is replaced with  $\hat{e}_{2,1}^1$ , with the unchanged conditions and the following actions:  $\{r = 2.1; c^s = 1; D = 5.5 - f_1\}$ . Similarly, the actions of  $\hat{e}_{2,1}^2$  replacing  $e_{2,1}^2$  are  $\{r = 2.1; c^s = 1; D = 3.7 - f_2\}$ .

In this example, the above augmentation is unnecessary, since z = 1 implies that, in any *Type 4* in  $v_2$ ,  $\lfloor 5.5 - f_1 \rfloor = 1$  and  $\lfloor 3.7 - f_2 \rfloor = 1$ . Therefore, the appended conditions and actions are as follows:

$$\begin{split} e_{2,1} &: \langle t_{2,1}^s > 0 \land (T_1 == 1 \land T_2 == 1) \land \\ &(t_{2,1}^s < 5.5 - f_1) \land (t_{2,1}^s < 3.7 - f_2) \rangle \\ &\{L_2 = 0; f_1 = f_1 + t_{2,1}^s; f_2 = f_2 + t_{2,1}^s; t_{2,1}^s = 0\} \\ e_{2,1}^1 &: \langle (T_1 == 1 \land (1 < 5.5 - f_1 < t_{2,1}^s)) \land t_{2,1}^s > 0 \land \\ &(5.5 - f_1 < 3.7 - f_2) \land (T_1 == 1 \land T_2 == 1) \rangle \\ &\{L_2 = 2; f_1 = f_1 + 1; f_2 = f_2 + 1; t_{2,1}^s = t_{2,1}^s - 1\} \\ e_{2,1}^2 &: \langle (T_2 == 1 \land (1 < 3.7 - f_2 < t_{2,1}^s)) \land t_{2,1}^s > 0 \land \\ &(3.7 - f_2 < 5.5 - f_1) \land (T_1 == 1 \land T_2 == 1) \rangle \\ &\{L_2 = 2; f_1 = f_1 + 1; f_2 = f_2 + 1; t_{2,1}^s = t_{2,1}^s - 1\} \end{split}$$

Since only a single self-loop is defined in vertices  $v_0$  and  $v_1$ , both vertices will have merged self-loop transitions of *Type 3* only. For  $v_0$  and  $v_1$ , merged

self-loop transitions  $e_{0,1}$  and  $e_{1,1}$  are defined for the sets of  $N_{0,1}^s = \{e_1\}$  and  $N_{1,1}^s = \{e_3\}$ , respectively, with the appended conditions and actions derived as for  $e_{2,1}$ .

Consider the test sequence for the FSM in Figure 5 (Table 1). While the test sequence is being executed, the values of timer-related variables of the model change with the progress of time.

Test step	Edge name	Edge cost	$T_1$	$T_2$	$f_1$	$f_2$	
(1)	$e_{ m on}$	0	0	0	$-\infty$	$-\infty$	
(2)	$e_2$	1	1	0	0	$-\infty$	
(3)	$e_3$	3	1	0	3	$-\infty$	
(4)	$e_4$	1	1	1	4	0	
(5)	$e_5$	1	1	1	5	1	
(6)	$e_8$	1	0	1	$-\infty$	2.5	
(7)	$e_1$	1	0	1	$-\infty$	3.5	
(8)	$e_2$	1	1	0	0	$-\infty$	
(9)	$e_4$	1	1	1	1	0	
(10)	$e_6$	1	1	1	2	1	
(11)	$e_7$	1	1	0	5.7	$-\infty$	
(12)	$e_8$	1	0	0	$-\infty$	$-\infty$	
(13)	$e_{ m off}$	0	0	0	$-\infty$	$-\infty$	

Table 1 Valid test sequence for the FSM of Figure 5.

Let us now trace the execution of the test sequence. After system initialization by transition  $e_{on}$ , transition  $e_2$  starts timer  $tm_1$ . After arriving at state  $v_1$ , there are 5.5sec left until  $tm_1$ 's timeout; so, transition  $e_{1,1}$  can be tested, which takes 3sec. After leaving  $v_1$ ,  $tm_1$  has 2.5sec left until timeout. In transition  $e_4$ , timer  $tm_2$  is started and the time-keeping variable for  $tm_1$  reaches  $f_1 = 4$ . After the test sequence arrives at state  $v_2$ ,  $tm_1$  and  $tm_2$  have 1.5sec and 3.7sec left until timeout, respectively— $tm_1$  will therefore expire first. There is not enough time to traverse  $e_{2,1}$  (i.e., to test both  $e_5$  and  $e_6$ ); therefore,  $e_{2,1}^1$  is traversed ( $e_5$  is tested). In fact, traversing  $e_{2,1}^{\perp}$  is equivalent to traversing a sequence of edges  $(\hat{e}_{2,1}^1, h_1, \hat{e}_2)$ , which contain only linear actions. This step leaves 0.5sec and 2.7sec until timeouts for  $tm_1$  and  $tm_2$ , respectively. After  $tm_1$  expires, the time-keeping variable for  $tm_2$  is advanced to  $f_2 = 2.5$ , which gives enough time (1.2 sec) to traverse  $e_{0,1}$ . Traversing  $e_{0,1}$  is equivalent to testing  $e_1$  with the time condition of  $\langle T_1 == 0 \land T_2 == 1 \rangle$ . Since at this point  $tm_1$  has expired and  $tm_2$  is running,  $e_1$ 's time condition is satisfied and the transition is tested.

Afterwards,  $e_2$  are  $e_4$  are traversed consecutively without spending time on already tested  $e_3$ . The test sequence arrives again at state  $v_2$ , with 4.5sec and

3.7sec left until timeouts for  $tm_1$  and  $tm_2$ , respectively. Now  $tm_2$  is to expire first, leaving sufficient time to traverse  $e_{2,1}$  (test  $e_6$ ). Then,  $tm_2$  expires and the time-keeping variable for  $tm_1$  is advanced to  $f_1 = 5.7$ , exceeding  $tm_1$ 's length by 0.2. Therefore,  $e_8$  is traversed immediately, since  $tm_1$  expired while  $e_7$  was being traversed. Now the IUT is back in its initial state  $v_0$  with both timers inactive and all transitions tested, so the test sequence returns to the system initialization state  $v_t$  through transition  $e_{\text{off}}$ .

The test sequence shown in Table 1 satisfies all timing constraints imposed by the two timers  $tm_1$  and  $tm_2$ . In addition, the time conditions for all transitions in the FSM are satisfied at any time during the test sequence traversal. Section 6. presents an algorithmic technique to obtain low-cost test sequences satisfying the above criteria.

# 6. INCONSISTENCIES REMOVAL ALGORITHMS

The interdependence among the variables used in the actions and conditions of an EFSM, or an FSM with time variables, may cause various *inconsistencies* among the actions and conditions of the model. For example, in Figure 5, the actions of  $e_7$  set  $T_2$  to 0. Since the time condition of  $e_5$  requires that  $\langle T_2 == 1 \rangle$ ,  $e_7$ 's action causes inconsistency with  $e_5$ 's condition. Similarly, a test sequence that includes both  $e_1$  and  $e_5$  contains condition inconsistency  $e_1$  requires that  $\langle T_1 == 0 \rangle$  and  $e_5$  that  $\langle T_1 == 1 \rangle$ . Both test sequences are therefore infeasible.

Feasible test sequences can be generated from the EFSM models if the inconsistencies are eliminated. The algorithms by Uyar and Duale [5, 19, 20] eliminate inconsistencies from an EFSM in two phases. First, action inconsistencies are detected and eliminated. Next, the algorithms proceed with the detection and elimination of condition inconsistencies by employing linear programming techniques.

In these algorithms, both edge actions and conditions are represented by sets of matrices to analyze their interdependence. In addition, the actions and conditions accumulated along the paths in the graph are represented by sets of *Action Update Matrix (AUM)* pairs and *Accumulated Condition Matrix (ACM)* triplets [5], respectively. While traversing the EFSM graph in a modified breadth-first (MBF) and a depth-first (DF) manner, inconsistencies are eliminated by splitting the nodes and edges of the EFSM graph. During this split, unnecessary growth of the number of states and transitions is avoided. Only the edges with feasible conditions and the nodes that can be reached from the initial node are selected from the split nodes and edges to be included in the resulting FSM. (See paper [5] in these proceedings for a detailed presentation of the inconsistencies removal algorithms.)

In the methodology presented in this paper, the inconsistency removal algorithms are adapted for handling the conflicts caused by multiple timers, and are incorporated in the proposed technique as follows:

#### Step (1)—Graph augmentation:

Augment an original graph with vertex  $v_t$ , edges of  $e_{on}$  and  $e_{off}$ , and a number of observer edges as described in Section 3. (see Figure 6 for an example). Mark and queue vertex  $v_0$  as  $v_{0,0}$ .

#### Step (2)—Inconsistencies removal:

Unqueue vertex  $v_{0,k}$  (copy of the initial state state  $v_0$ ). Apply VHDL inconsistencies removal algorithms in MBF and DF manners starting from  $v_{0,k}$  until  $v_{0,k}$  is reached again through a set of edges denoted by  $E_{0,k}$  (the set of incoming edges of  $v_{0,k}$ ).

#### **Step (3)**—**Initial state splitting:**

Split vertex  $v_{0,k}$  into a set of vertices  $V_{0,k} \cup \{v_{0,k}\}$ ;  $V_{0,k}$ 's cardinality is equal to the number of distinct AUMs associated with edges in  $E_{0,k}$  (note:  $v_{0,k}$  may belong to  $V_{0,k}$ ). The set of  $V_{0,k}$  is further divided into  $V_{0,k}^{\text{inc}}$ , which contains vertices associated with AUMs corresponding to all timers inactive, and  $V_{0,k}^{\text{act}}$ , containing the remaining vertices in  $V_{0,k}$ . The set of edges  $E_{0,k}$  is divided accordingly into  $E_{0,k}^{\text{inc}}$  and  $E_{0,k}^{\text{act}}$ .

Edge  $e_{on}$ , whose traversal is mandatory in the test sequence, is incoming only to vertex  $v_0$ ; an edge  $e_{off}$  is outgoing from each vertex in  $V_{0,k}^{inc}$ . All copies of  $e_{off}$  are optional to traverse—they will be included in the test sequence only when necessary.

#### **Step (4)—Redundant paths pruning:**

Remove from the graph edges in  $E_{0,k}^{\text{inc}}$  using the following two-phase heuristic procedure. First, any edge  $e_i \in E_{0,k}^{\text{inc}}$  is deleted if  $\exists e_j \in E_{0,k}^{\text{inc}}$  such that: •  $AUM_j$  includes  $AUM_i$ . Since all timers are inactive in  $V_{0,k}^{\text{inc}}$ ,

- $AUM_j$  includes  $AUM_i$ . Since all timers are inactive in  $V_{0,k}^{\text{inc}}$ , a sufficient condition for  $AUM_j$  to include  $AUM_i$  is as follows:  $(\forall_{p \leq |V|} \forall_{l \leq M_p}) t_{p,l}^{s(j)} \leq t_{p,l}^{s(i)}$ . This means that  $AUM_j$  allows testing more self-loops than  $AUM_i$ .
- All edges in the paths from  $v_{0,k}$  to vertices in  $V_{0,k}^{\text{inc}}$  associated with  $AUM_i$  have their copies in the paths from  $v_{0,k}$  to vertices in  $V_{0,k}^{\text{inc}}$  associated with  $AUM_j$ .

Second, any edge  $e_i \in E_{0,k}^{inc}$  is deleted if neither of the following conditions is true:

- A new edge can be traversed by keeping  $e_i$  in the graph, i.e., the paths from  $v_{0,k}$  to vertices in  $V_{0,k}^{\text{inc}}$  associated with  $AUM_i$  should contain an edge that has not been traversed before unqueuing  $v_{0,k}$ .
- Some untested self-loops can be traversed by keeping e<sub>i</sub> in the graph, i.e., (∃<sub>p<|V|</sub>∃<sub>l≤M<sub>p</sub></sub>)t<sup>s(j)</sup><sub>p,l</sub> < t<sup>s(0.k)</sup><sub>p,l</sub>.

#### Step (5)—Queueing and marking copies of the initial state:

Queue all unmarked vertices in  $V_{0,k}^{\text{act}}$  and unmarked vertices in  $V_{0,k}^{\text{inc}}$  with at least one undeleted edge in  $E_{0,k}^{\text{inc}}$ . Mark queued vertices.

If the queue is empty, terminate; otherwise, go back to Step (2).  $\Box$ 

Typically, a test sequence is divided into a number of subtours subsequences of a full test sequence that start and stop in  $v_0$ . Each subtour may or may not be preceded by a system power-down/power-up; therefore, when an IUT starts executing, not only should it be brought to state  $v_0$ , in addition, all timers must be inactive. To ensure this behavior, each  $v_0$ 's copy corresponding to an AUM with all timers inactive (i.e., any vertex in  $V_{0,k}^{inc}$ ) may be considered the start state of a subtour.

Let us now apply the above algorithm to the FSM of Figure 5. First, the FSM is augmented with the auxiliary edges of  $e_{on}$  and  $e_{off}$ , and a number of observer edges as shown in Figure 6. The conditions and actions of the observer edges are defined based on (1.2)–(1.3) as follows:

$$\begin{split} s_{0,1}' : \langle L_0 < 2 \land t_{0,1}^s == 0 \rangle \{\}, \quad s_{1,1}' : \langle L_1 < 2 \land t_{1,1}^s == 0 \rangle \{\} \\ s_{2,1}' : \langle L_2 < 2 \land t_{2,1}^s == 0 \rangle \{\} \\ s_{0,1}'' : \langle L_0 < 2 \land (t_{0,1}^s) > 0 \land (T_1 == 1 \lor T_2 == 0)) \rangle \{\} \\ s_{2,1}'' : \langle L_2 < 2 \land (t_{2,1}^s) > 0 \land (T_1 == 0 \lor T_2 == 0)) \rangle \{\} \\ s_0'' : \langle 1 \rangle \{L_0 = 2\}, \quad \check{s}_1 : \langle 1 \rangle \{L_1 = 2\}, \quad \check{s}_2 : \langle 1 \rangle \{L_2 = 2\} \end{split}$$

An application of the algorithm described in this section to the graph of Figure 6 produces the final graph shown in Figure 7. A minimum-cost test sequence, given by (1.5)-(1.7), can be derived as a solution to the Rural Chinese Postman Problem [1] on this final graph. The test sequence of (1.5)-(1.7) consists of three subtours containing the edges defined in the original graph (Figure 5) and the auxiliary edges of  $e_{on}$  and  $e_{off}$ ; the observer edges are dropped. All edges defined in the graph of Figure 5 are included without the explicit delaying of timers  $tm_1$  and  $tm_2$ ; therefore, the technique presented in Section 4. need not be applied in this case. Note that the test sequence of Table 1, which was derived manually, corresponds to Subtour 1 of (1.5).

- $1: e_{on}, e_2, e_3, e_4, e_5, e_8, e_1, e_2, e_4, e_6, e_7, e_8, e_{off}$ (1.5)
- $2: e_{\rm on}, e_2, e_4, e_5, e_6, e_7, e_8 \tag{1.6}$

$$3: e_2, e_3, e_4, e_8, e_1, e_2, e_4, e_7, e_8, e_{\text{off}}$$

$$(1.7)$$

## 7. CONCLUSION

As a recent result of on-going collaboration between UD and CCNY, this paper presents the study of conformance test generation when multiple timers



Figure 6 Augmented graph for the FSM of Figure 5.



Figure 7 The final graph for the FSM of Figure 5.

are running simultaneously. CCNY's inconsistency removal algorithms are applied to a new model for testing real-time protocols with multiple timers. As introduced in this paper, the new model captures complex timing dependencies by using simple linear expressions. This modeling technique, combined with the inconsistency removal algorithms, is expected to significantly shorten the test sequences without compromising their fault coverage. Currently, a software tool applying inconsistency removal algorithms to EFSMs models is being implemented at CCNY. Completion of this software project will enable the application of the presented methodology to MIL-STD 188-220.

The methodology presented in this paper is expected to detect transfer and output faults, where an IUT moves into a wrong state (a state other than the one specified) or generates a wrong output (an output other than the one specified) to a given input. As future work, fault detection issues will be pursued further. In particular, a fault model taking into account specific faults caused by the violation of timing constraints and time conditions should be considered. Computing the fault coverage of the presented methodology also needs to be investigated. <sup>1</sup>

## Notes

1. The views and conclusions contained in this document are those of the authors and should not be interpreted as representing the official policies, either expressed or implied, of the Army Research Laboratory or the U.S. Government.

#### References

- A. V. Aho, A. T. Dahbura, D. Lee, and M. U. Uyar. An optimization technique for protocol conformance test generation based on UIO sequences and rural Chinese postman tours. *IEEE Trans. Commun.*, 39(11):1604–1615, Nov. 1991.
- [2] R. Alur and D. L. Dill. A theory of timed automata. *Theoret. Comput. Sci.*, 126:183–235, 1994.
- [3] L. Cacciari and O. Rafiq. Controllability and observability in distributed testing. In K. Saleh and R. Robert, eds, *Communications Software Engineering*, vol. 41(11-12) of *Inform. Softw. Techn.*, pp. 767–780. Sept. 1999.
- [4] R. Cardell-Oliver and T. Glover. A practical and complete algorithm for testing real-time systems. In *Proc. Int'l Symp. Formal Techn. Real-Time Fault-Toler. Syst. (FTRTFT)*, vol. 1486 of *LCNS*, pp. 251–261, Lyngby, Denmark, Sept. 1998. Springer-Verlag.
- [5] A. Y. Duale and M. U. Uyar. Generation of feasible test sequences for EFSM models. In H. Ural, R. L. Probert, and G. v. Bochmann, eds, *Proc. IFIP Int'l Conf. Test. Communicat. Syst. (TestCom)*, Ottawa, Canada, Aug.–Sept. 2000. Boston, MA: Kluwer Academic Publ.
- [6] A. En-Nouaary, R. Dssouli, F. Khendek, and A. Elqortobi. Timed test cases generation based on state characterisation technique. In *Proc. IEEE Real-Time Syst. Symp. (RTSS)*, pp. 220–229, Madrid, Spain, Dec. 1998.
- [7] M. A. Fecko, M. U. Uyar, P. D. Amer, A. S. Sethi, T. J. Dzik, R. Menell, and M. McMahon. A success story of formal description techniques: Estelle specification and test generation for MIL-STD 188-220. In R. Lai, ed, *FDTs in Practice*, vol. 23(12) of *Comput. Commun.*, pp. 1196–1213. July 2000.

- [8] M. A. Fecko, M. U. Uyar, A. S. Sethi, and P. D. Amer. Conformance testing in systems with semicontrollable interfaces. In S. Budkowski and E. Najm, eds, *Protocol Engineering: Part 2*, vol. 55(1-2) of *Annals Telecommun.* Jan.–Feb. 2000.
- [9] S. Fujiwara, G. v. Bochmann, F. Khendek, M. Amalou, and A. Ghedamsi. Test selection based on finite state models. *IEEE Trans. Softw. Eng.*, 17(6):591–603, June 1991.
- [10] T. Higashino, A. Nakata, K. Taniguchi, and A. R. Cavalli. Generating test cases for a timed I/O automaton model. In G. Csopaki, S. Dibuz, and K. Tarnay, eds, *Proc. IFIP Int'l Wksp Test. Communicat. Syst. (IWTCS)*, pp. 197–214, Budapest, Hungary, Sept. 1999. Boston, MA: Kluwer Academic Publ.
- [11] D. Hogrefe. On the development of a standard for conformance testing based on formal specifications. *Comput. Stand. Interf.*, 14(3):185–190, 1992.
- [12] R. Lanphier, A. Rao, and H. Schulzrinne. Real time streaming protocol (RTSP). RFC 2326, Internet Eng. Task Force, Apr. 1998.
- [13] L. Leonard and G. Leduc. An introduction to ET-LOTOS for the description of timesensitive systems. *Comput. Networks ISDN Syst.*, 29(3):271–290, 1997.
- [14] G. Luo, G. v. Bochmann, and A. F. Petrenko. Test selection based on communicating nondeterministic finite state machines using a generalized Wp-method. *IEEE Trans. Softw. Eng.*, 20(2):149–162, 1994.
- [15] H. Schulzrinne, S. Casner, R. Frederick, and V. Jacobson. RTP: A transport protocol for real-time applications. RFC 1889, Internet Eng. Task Force, Jan. 1996.
- [16] J. Springintveld, F. Vaandrager, and P. R. D'Argenio. Testing timed automata. Technical Report CTIT-97-17, Univ. of Twente, the Netherlands, 1997. (Invited talk at TAP-SOFT'97, Lille, France, Apr 1997).
- [17] J. Tretmans. Conformance testing with labelled transitions systems: Implementation relations and test generation. *Comput. Networks ISDN Syst.*, 29(1):49–79, 1996.
- [18] H. Ural. Formal methods for test sequence generation. *Comput. Commun.*, 15(5):311– 325, June 1992.
- [19] M. U. Uyar and A. Y. Duale. Modeling VHDL specifications as consistent EFSMs. In Proc. IEEE Military Commun. Conf. (MILCOM), Monterey, CA, Nov. 1997.
- [20] M. U. Uyar and A. Y. Duale. Resolving inconsistencies in EFSM-modeled specifications. In Proc. IEEE Military Commun. Conf. (MILCOM), Atlantic City, NJ, Nov. 1999.
- [21] M. U. Uyar, M. A. Fecko, A. S. Sethi, and P. D. Amer. Testing protocols modeled as FSMs with timing parameters. *Comput. Networks*, 31(18):1967–1988, Sept. 1999.