



Context-sensitive Analysis

Part II

Chapter 4 (up to Section 4.3)



Attribute Grammars

Add rules to compute the decimal value of a signed binary number

<i>Productions</i>	<i>Attribution Rules</i>
<i>Number</i> → <i>Sign List</i>	$List.pos \leftarrow 0$ If <i>Sign.neg</i> then $Number.val \leftarrow - List.val$ else $Number.val \leftarrow List.val$
<i>Sign</i> → +	$Sign.neg \leftarrow false$
-	$Sign.neg \leftarrow true$
<i>List</i> ₀ → <i>List</i> ₁ <i>Bit</i>	$List_1.pos \leftarrow List_0.pos + 1$ $Bit.pos \leftarrow List_0.pos$ $List_0.val \leftarrow List_1.val + Bit.val$
<i>Bit</i>	$Bit.pos \leftarrow List.pos$ $List.val \leftarrow Bit.val$
<i>Bit</i> → 0	$Bit.val \leftarrow 0$
1	$Bit.val \leftarrow 2^{Bit.pos}$



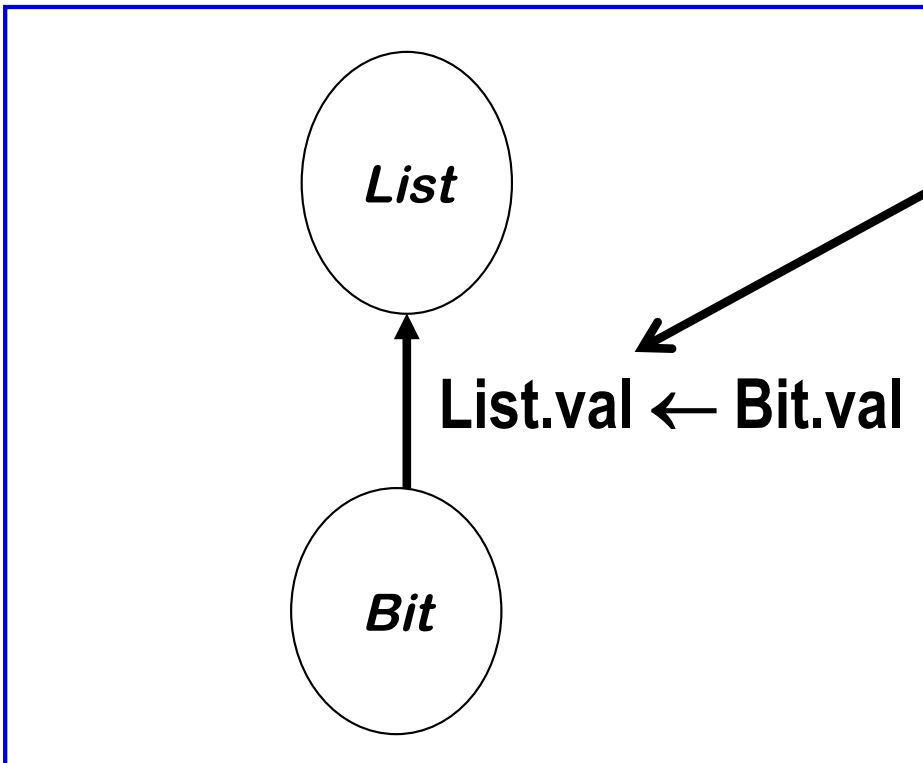
Two kinds of Attributes

- Synthesized attribute
 - Bottom-Up flow of values
 - Depends on values from the node itself, children, or constants
- Inherited attribute
 - Top-down flow of values
 - Depends on values from siblings, parent and constants

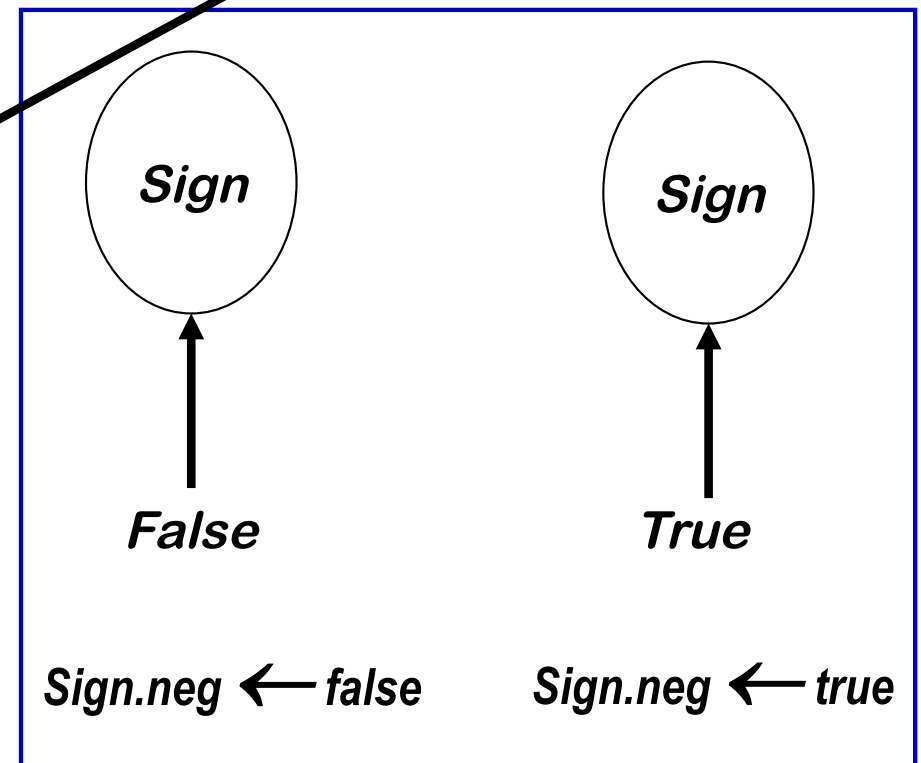
Synthesized Attributes

Depends on values from the node itself, children, or constants

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$List_0 \rightarrow List_1\ Bit$	$List_1.pos \leftarrow List_0.pos + 1$ $Bit.pos \leftarrow List_0.pos$ $List_0.val \leftarrow List_1.val + Bit.val$
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$Bit \rightarrow 1$	$Bit.val \leftarrow 2^{Bit.pos}$



Bottom-Up flow (Children)

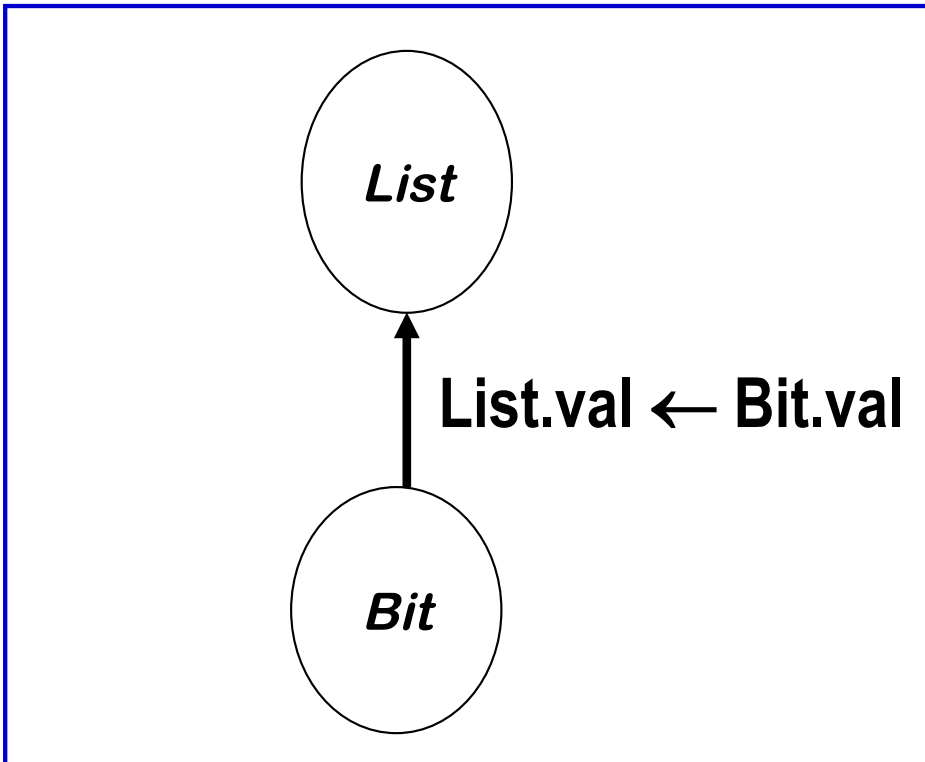


Constants

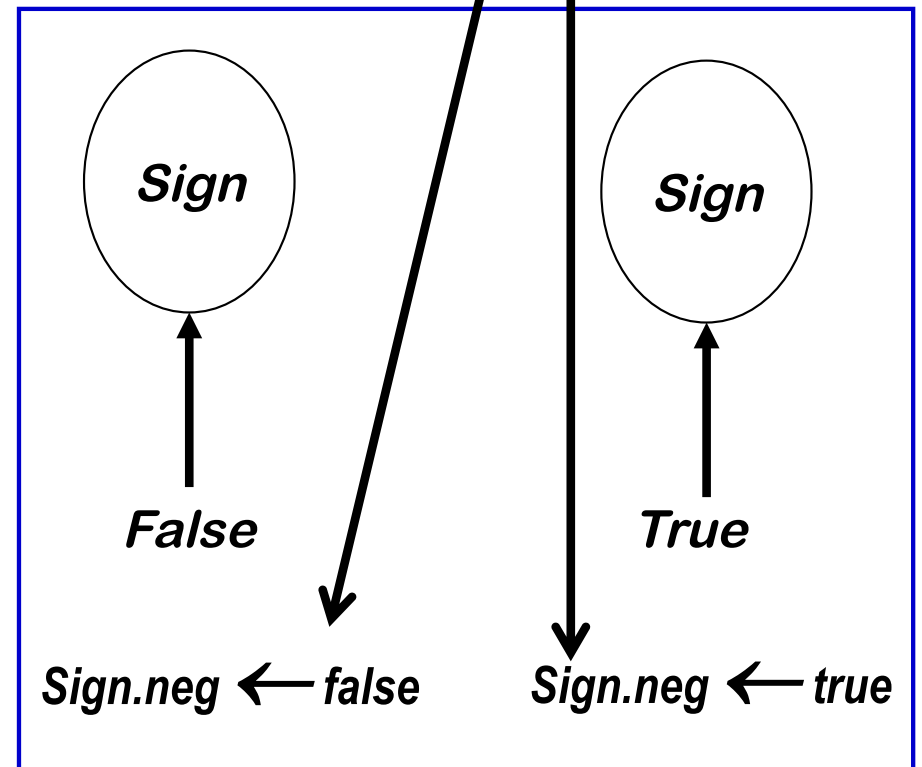
Synthesized Attributes

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Bottom-Up flow (Children)

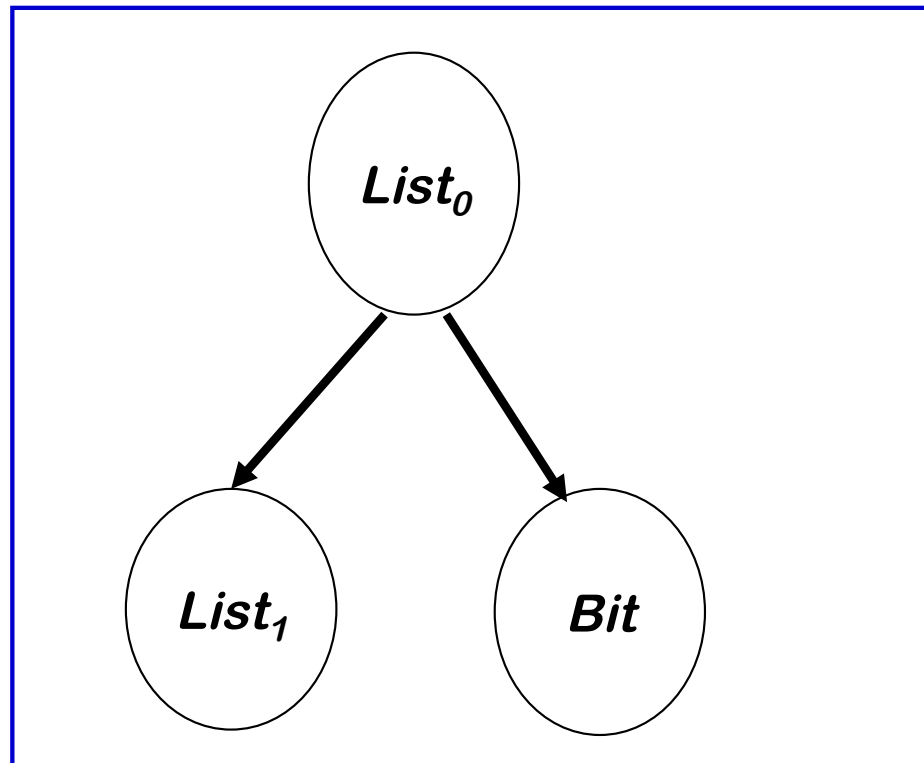


Constants

Inherited Attributes

Depends on values from siblings, parent and constants

Productions	Attribution Rules
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$List_0 \rightarrow List_1 Bit$	$List_1.pos \leftarrow List_0.pos + 1$ $Bit.pos \leftarrow List_0.pos$ $List_0.val \leftarrow List_1.val + Bit.val$
$List_0 \rightarrow Bit$	$Bit.pos \leftarrow List.pos$ $List.val \leftarrow Bit.val$
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Top-down flow

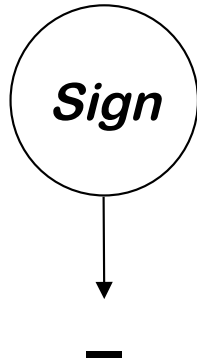
$List_1.pos \leftarrow List_0.pos + 1$
 $Bit.pos \leftarrow List_0.pos$



Back to the Examples

For “-1”

Sign.neg



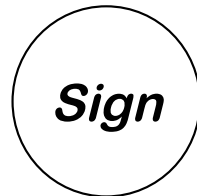
Symbol	Attributes
<i>Number</i>	val
<i>Sign</i>	neg
<i>List</i>	pos, val
<i>Bit</i>	pos, val



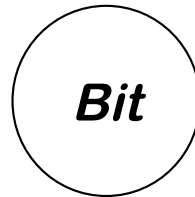
Back to the Examples

For “-1”

Sign.neg



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Bit.pos

Bit.val

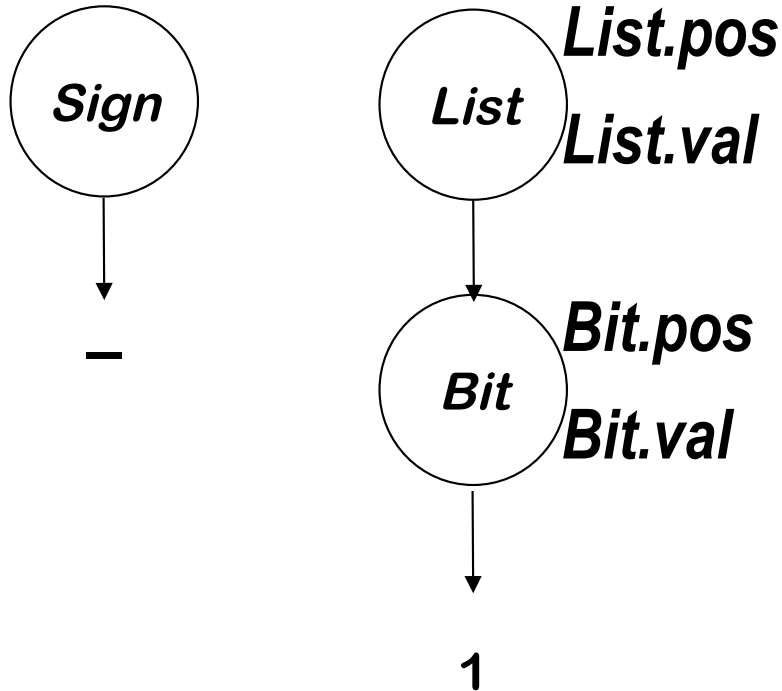
Symbol	Attributes
<i>Number</i>	val
<i>Sign</i>	neg
<i>List</i>	pos, val
<i>Bit</i>	pos, val



Back to the Examples

For “-1”

Sign.neg



Symbol	Attributes
<i>Number</i>	val
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<i>List</i>	pos, val
<i>Bit</i>	pos, val

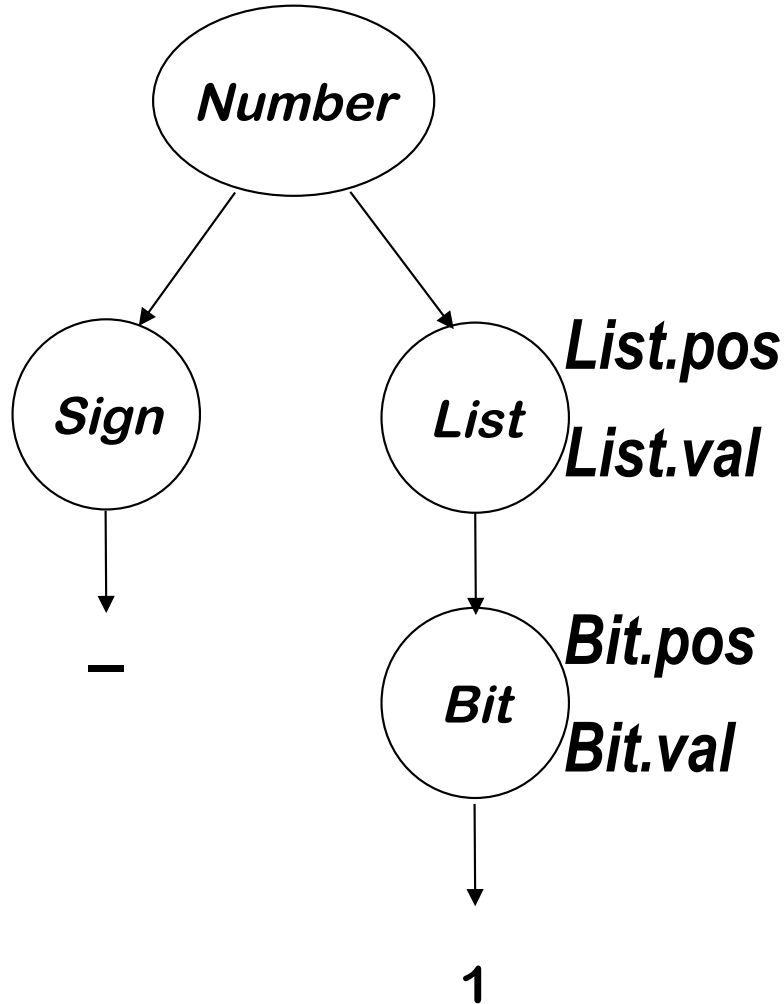


Back to the Examples

For “-1”

Number.val

Sign.neg

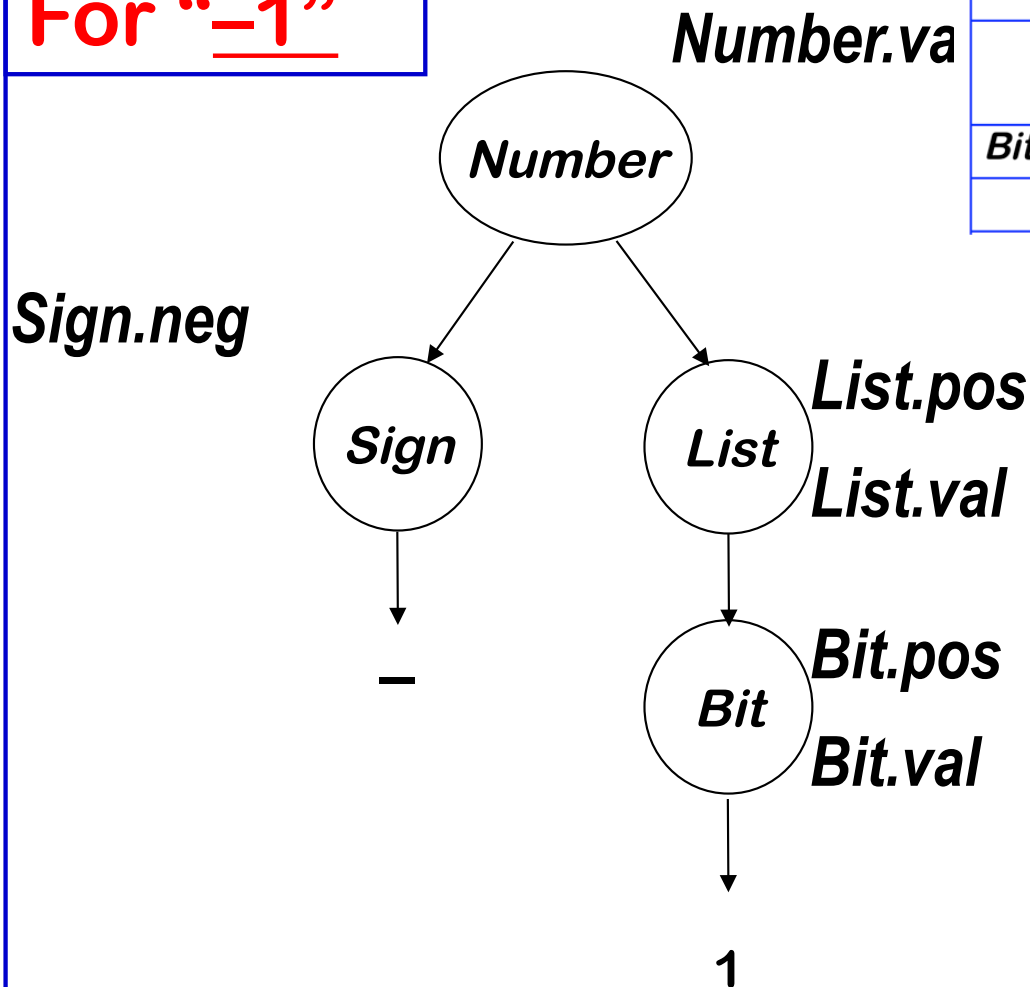


Symbol	Attributes
<i>Number</i>	val
<i>Sign</i>	neg
<i>List</i>	pos, val
<i>Bit</i>	pos, val

Back to the Examples

Productions	Attribution Rules
$Number \rightarrow Sign List$	$List.pos \leftarrow 0$ If $Sign.neg$ then $Number.val \leftarrow - List.val$ else $Number.val \leftarrow List.val$
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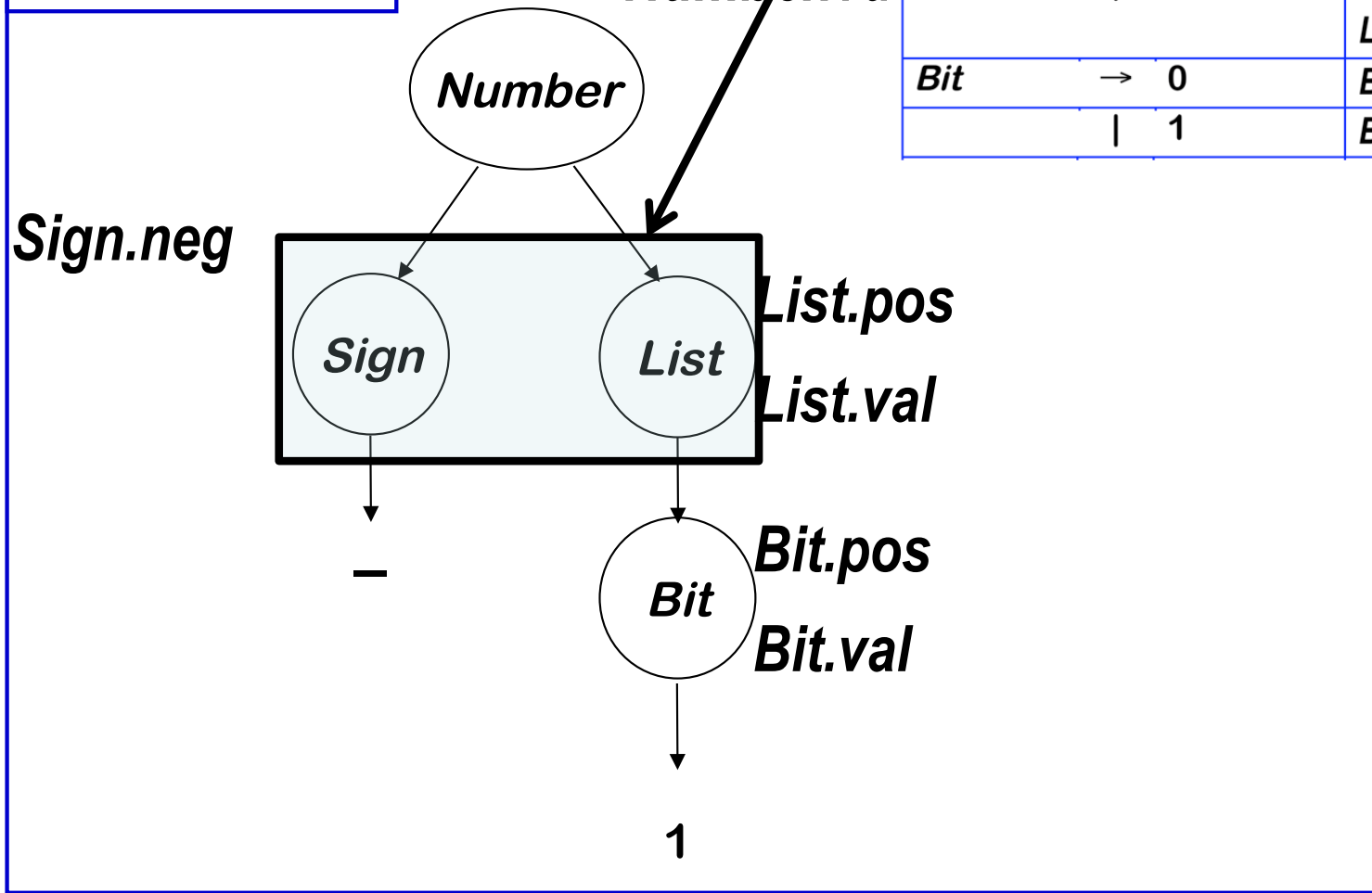
For “-1”



Back to the Examples

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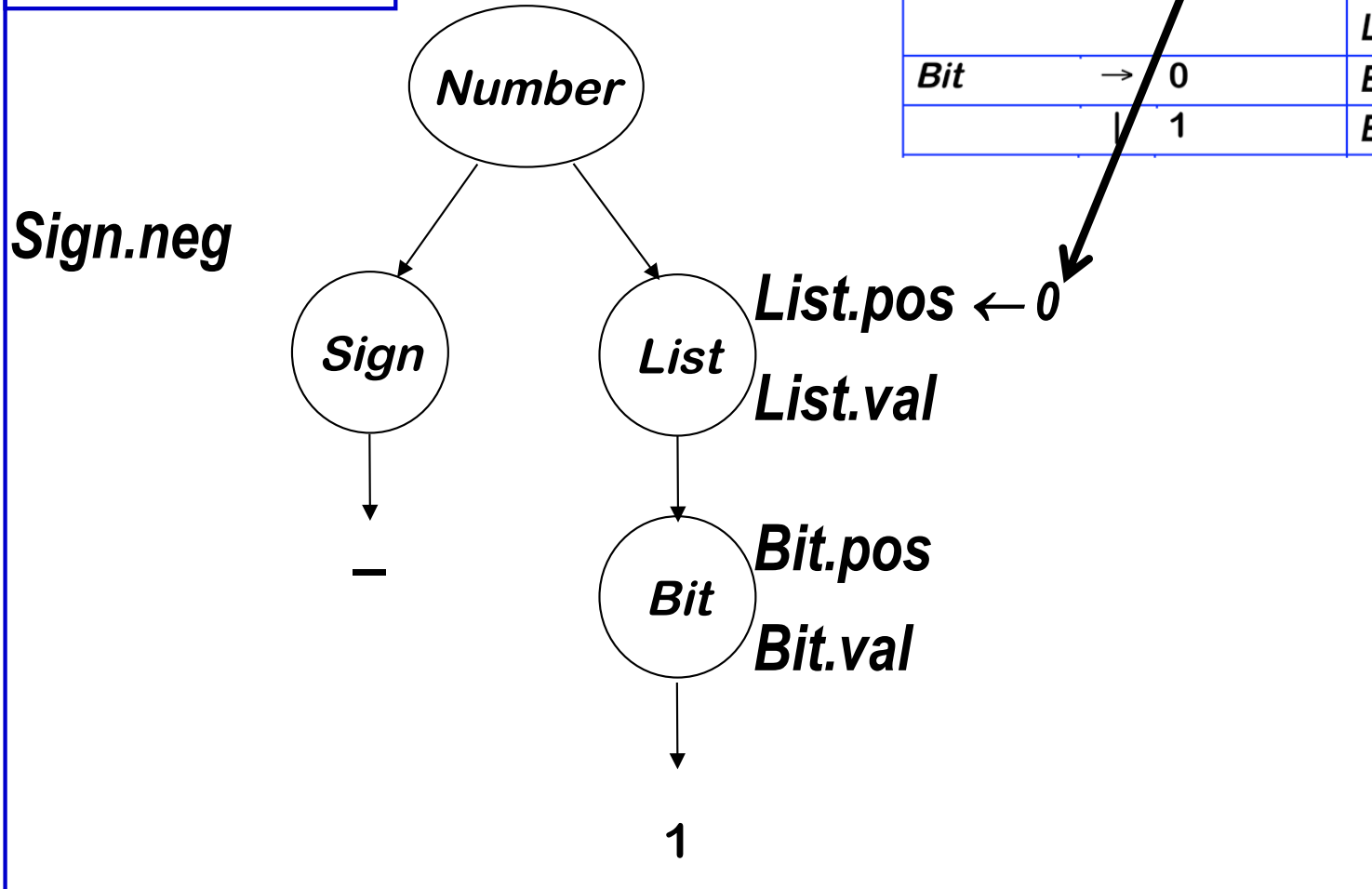
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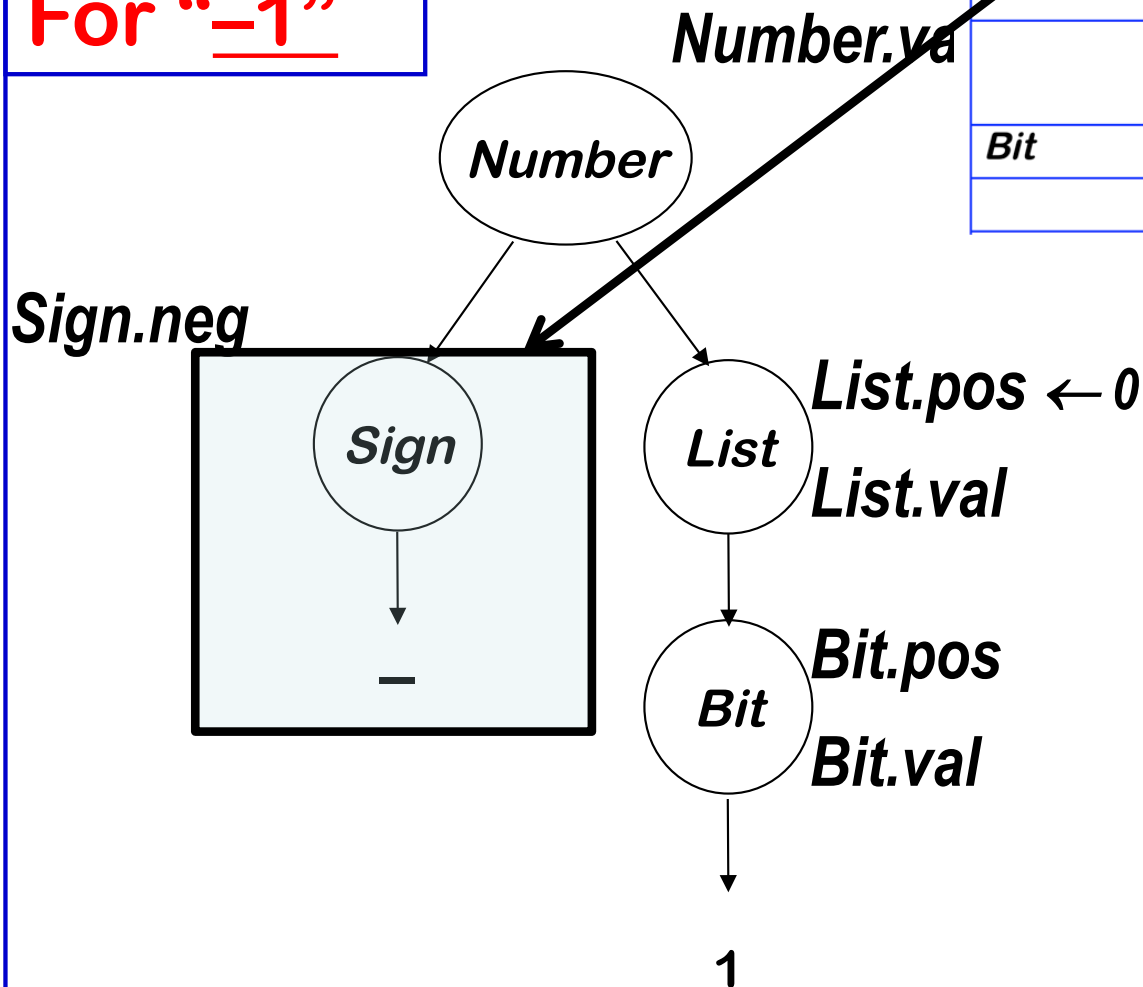
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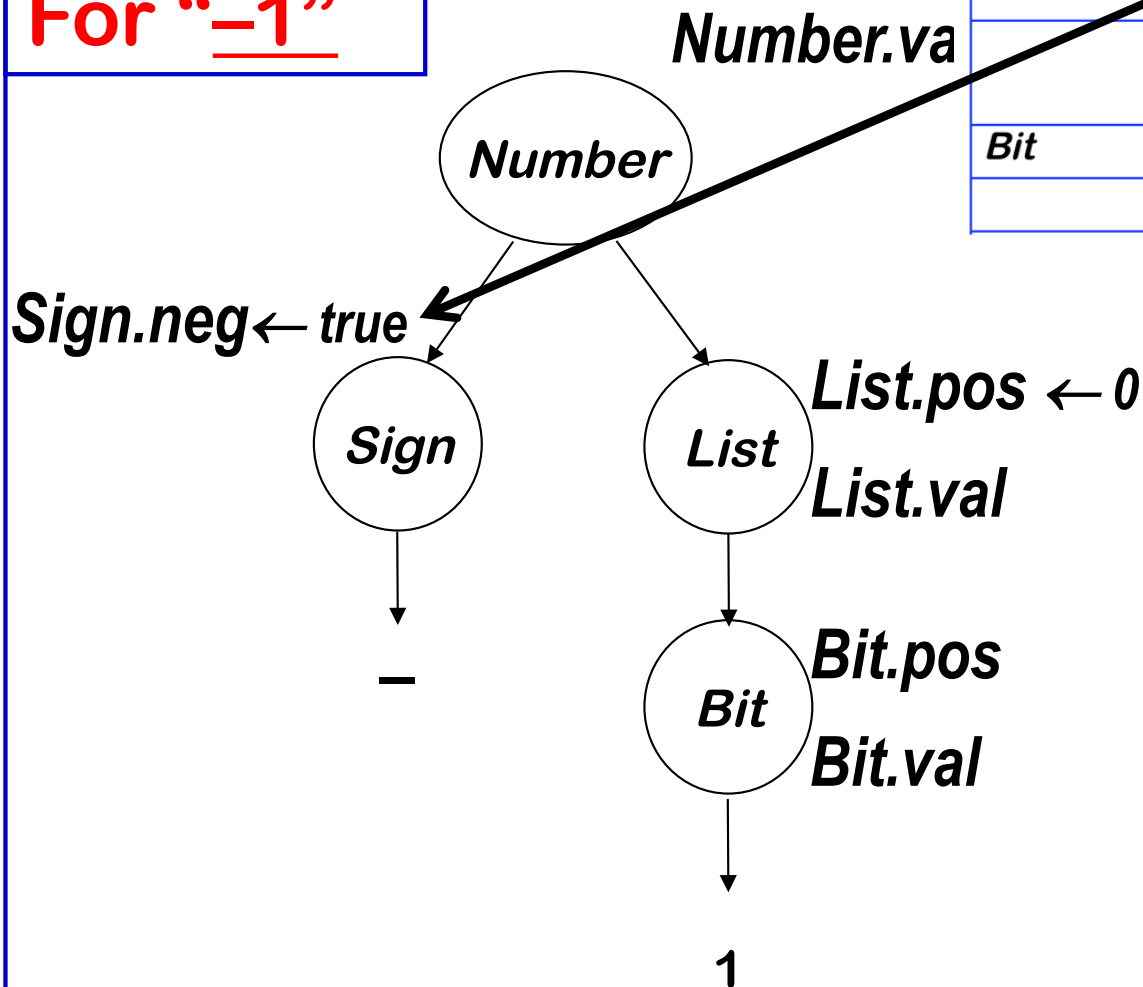
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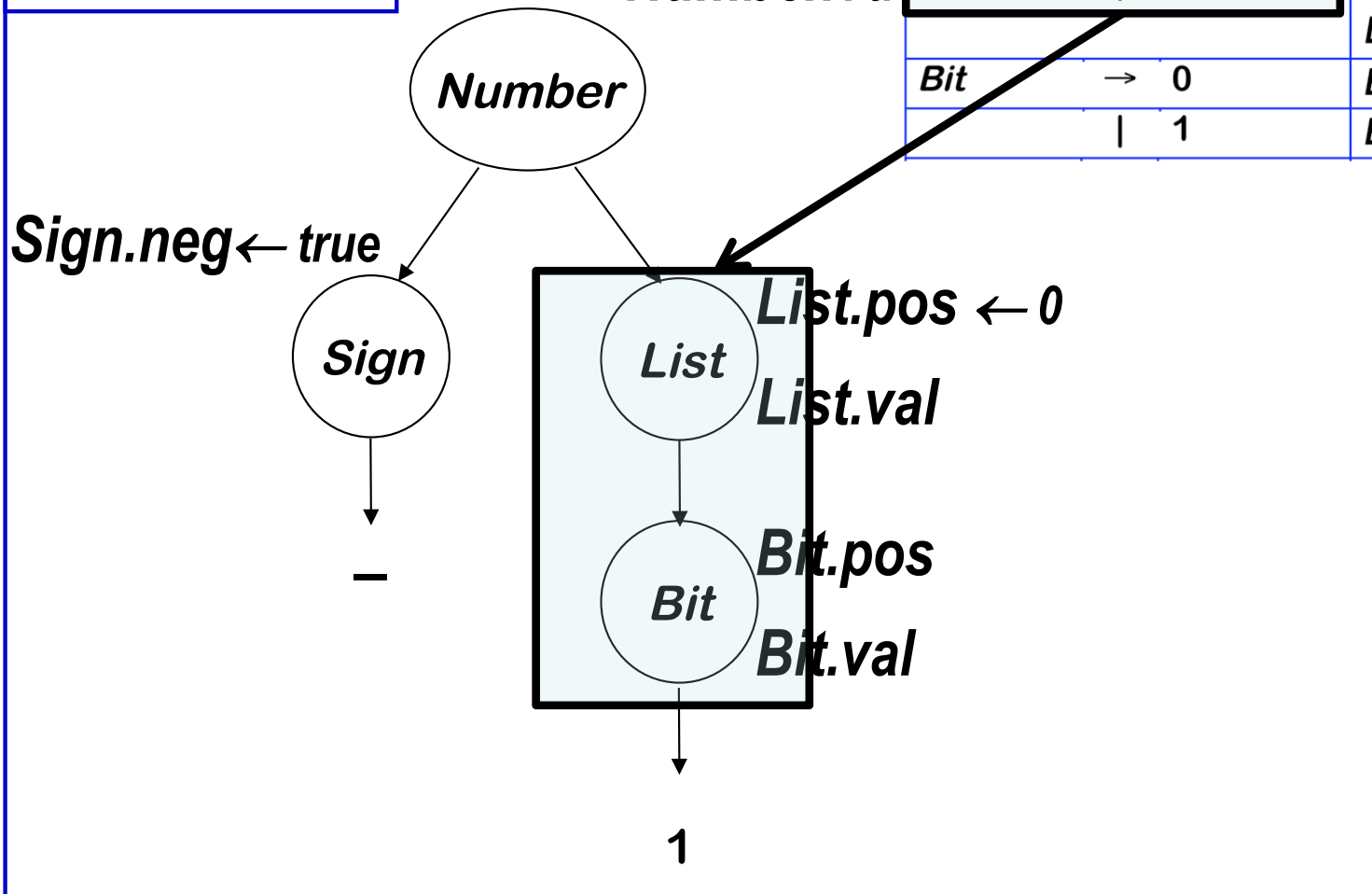
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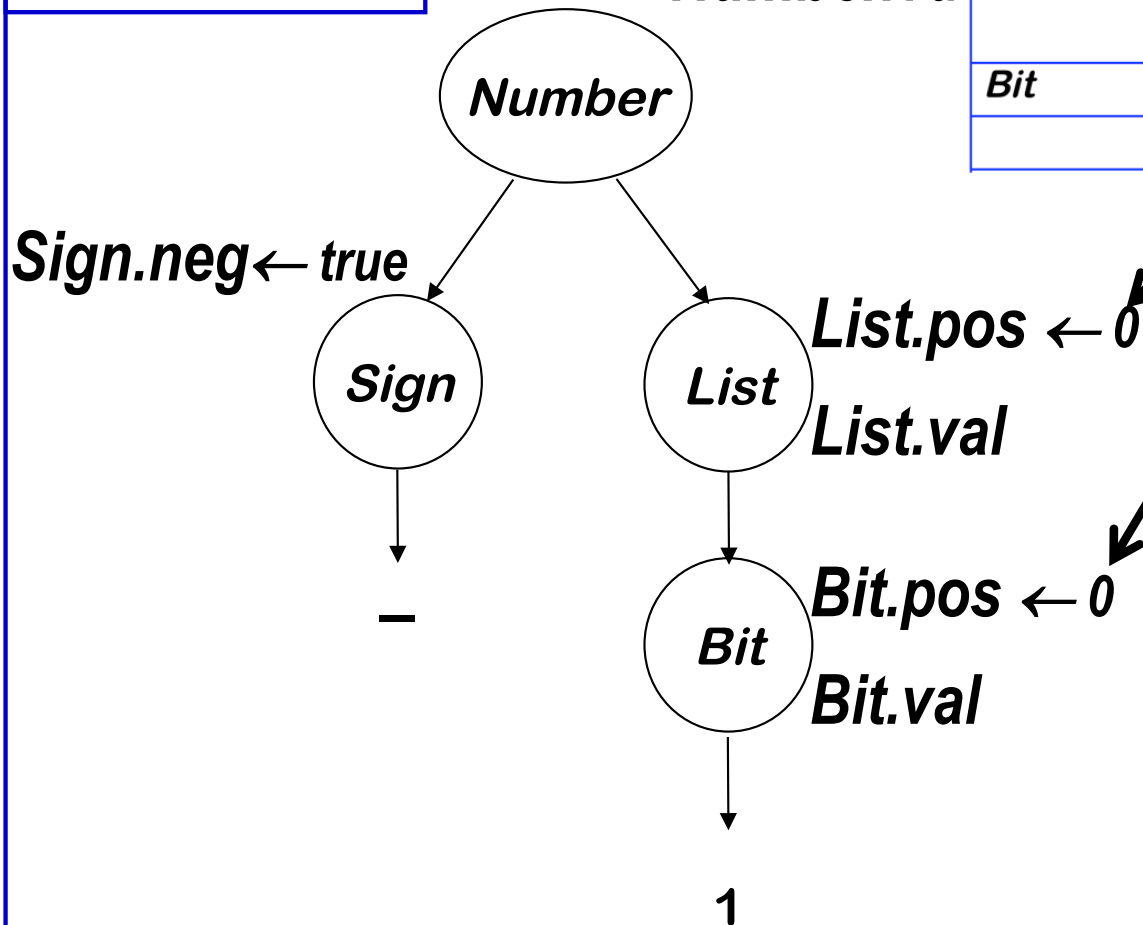
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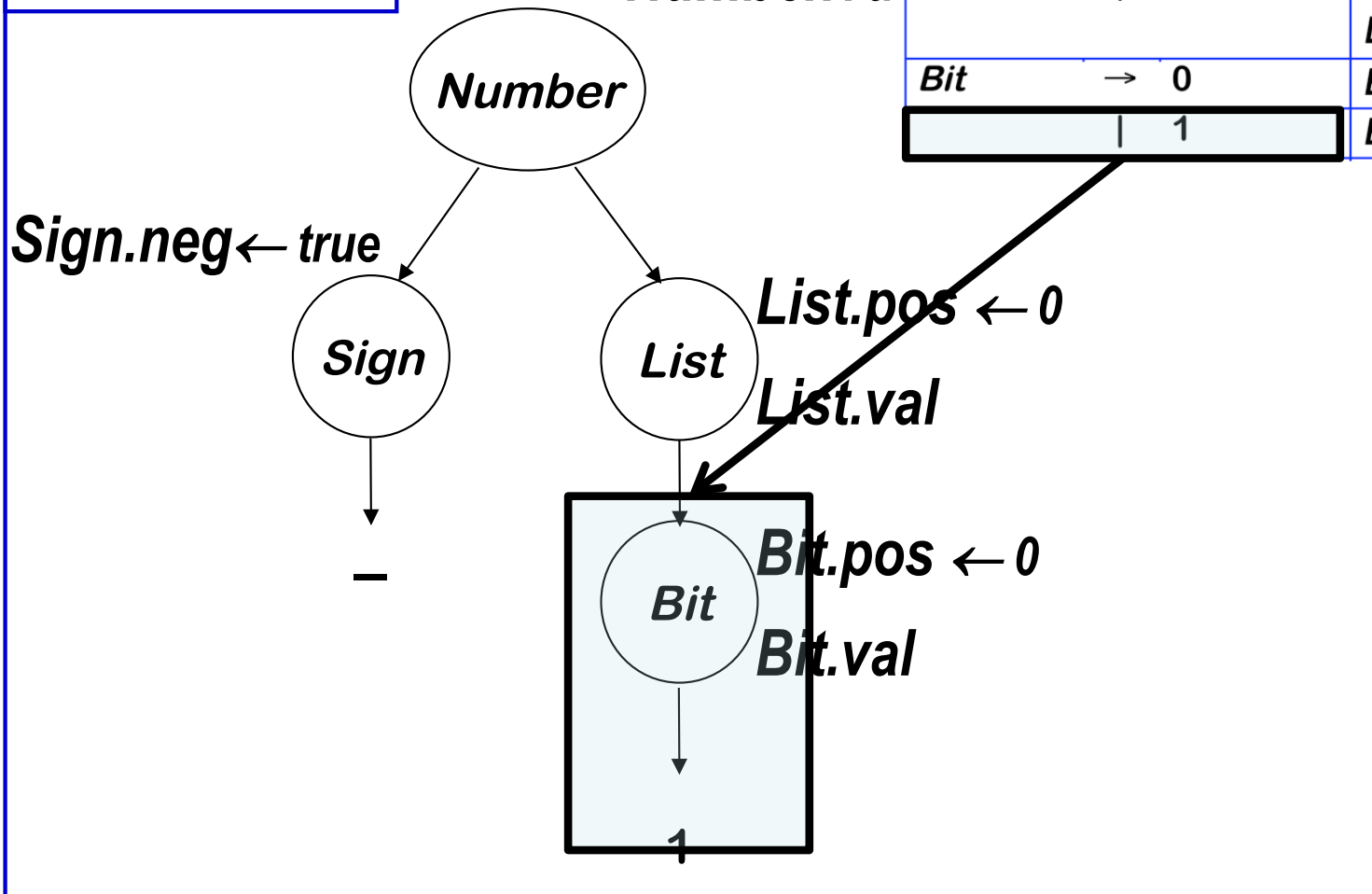
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For “-1”

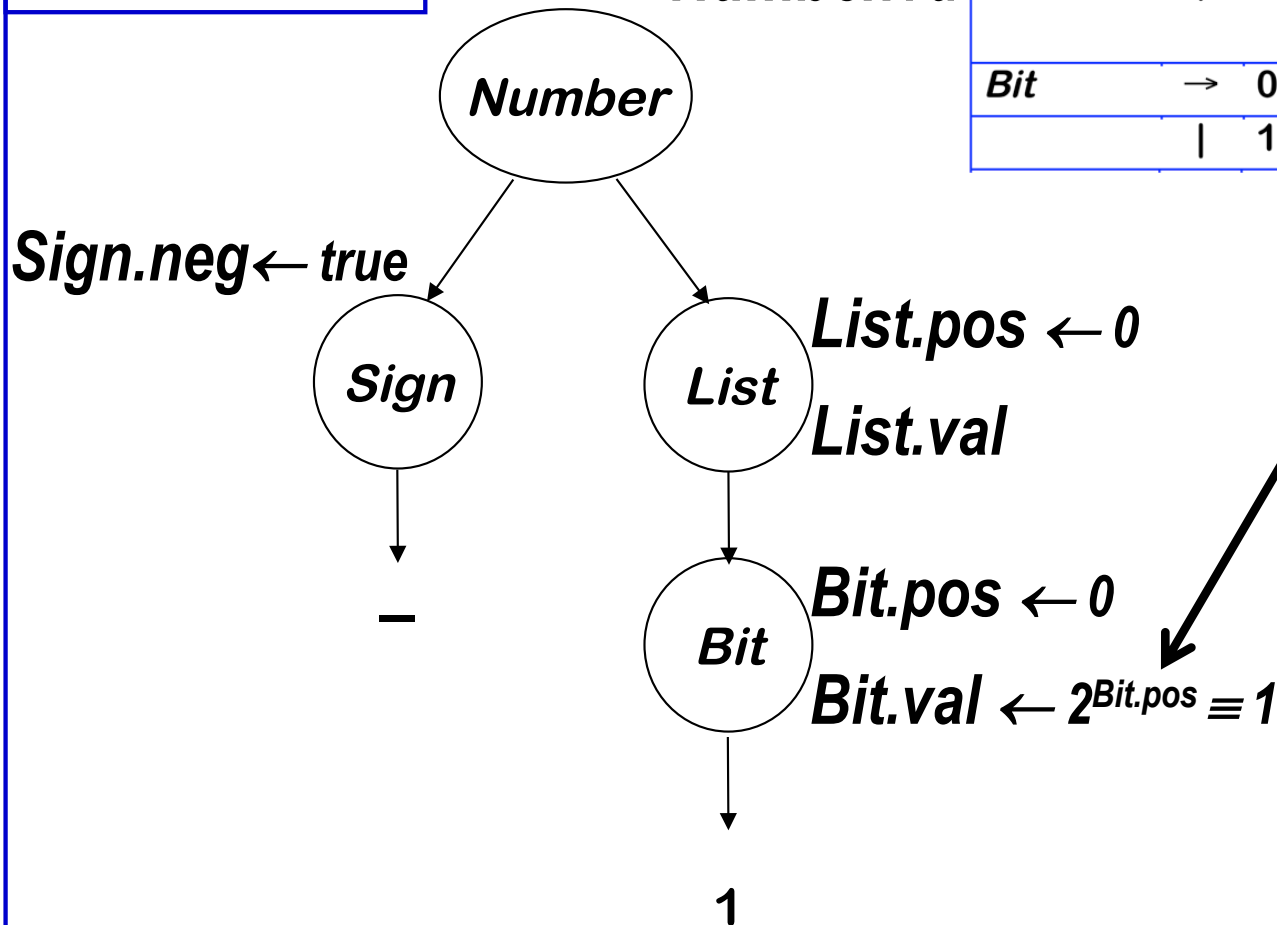


1

Back to the Examples

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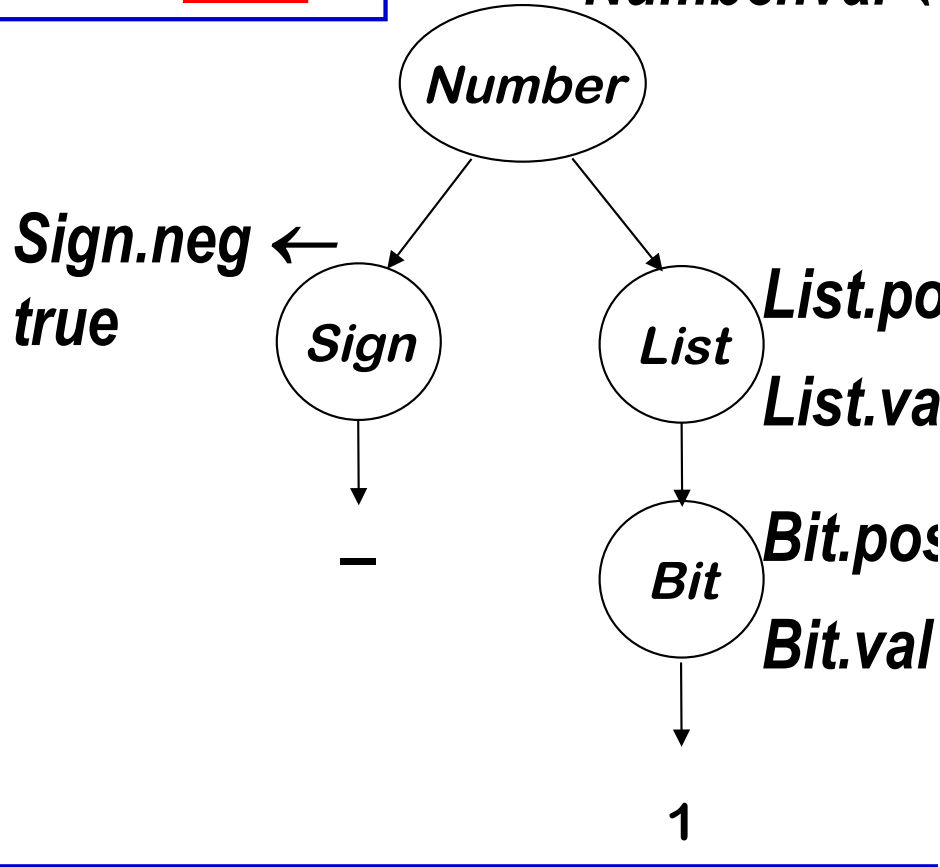
For “-1”



Back to the Examples

For “-1”

$$\text{Number.val} \leftarrow - \text{List.val} \equiv -1$$

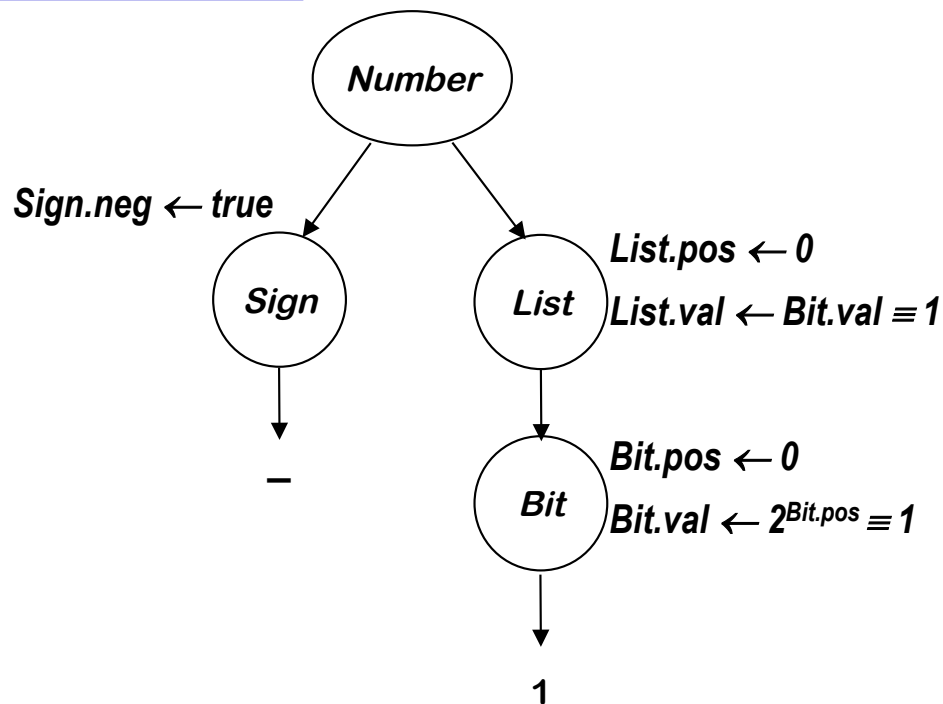


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$\text{Sign} \rightarrow -$	$\text{Sign.neg} \leftarrow \text{true}$
$\text{List}_0 \rightarrow \text{List}_1 \text{Bit}$	$\text{List}_1.\text{pos} \leftarrow \text{List}_0.\text{pos} + 1$ $\text{Bit.pos} \leftarrow \text{List}_0.\text{pos}$ $\text{List}_0.\text{val} \leftarrow \text{List}_1.\text{val} + \text{Bit.val}$
$\text{List}_0 \rightarrow \text{Bit}$	$\text{Bit.pos} \leftarrow \text{List}_0.\text{pos}$ $\text{List}_0.\text{val} \leftarrow \text{Bit.val}$
$\text{Bit} \rightarrow 0$	$\text{Bit.val} \leftarrow 0$
$\text{Bit} \rightarrow 1$	$\text{Bit.val} \leftarrow 2^{\text{Bit.pos}}$

Back to the Examples

For “-1”

$$\text{Number.val} \leftarrow - \text{List.val} \equiv -1$$



One possible evaluation order:

- 1 List.pos
- 2 Sign.neg
- 3 Bit.pos
- 4 Bit.val
- 5 List.val
- 6 Number.val

Other orders are possible

Evaluation order must be consistent with the **attribute dependence graph**



Attributes + Parse Tree

- Attributes associated with nodes in parse tree
- Rules are value assignments associated with productions
- Rules & parse tree define an attribute dependence graph
 - Dependence graph must be non-circular (no cycles)

This produces a high-level, functional specification



Using Attribute Grammars

Attribute grammars can specify context-sensitive actions

- Take values from syntax
- Perform computations with values
- Insert type tests, type inference, logic, ...



Evaluation Methods

Dynamic, dependence-based methods

- Build the parse tree
- Build the dependence graph
- Topological sort the dependence graph
- Define attributes in topological order

Rule-based methods

(treewalk)

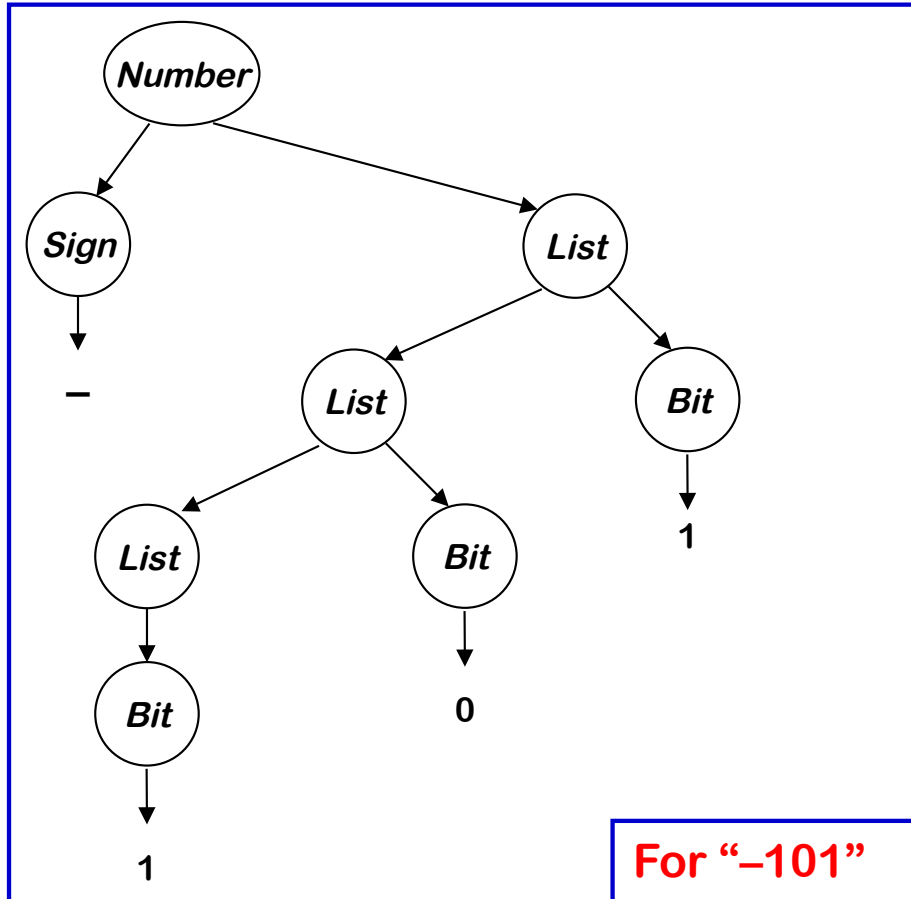
- Analyze rules at compiler-generation time
- Determine a fixed (static) ordering
- Evaluate nodes in that order

Oblivious methods

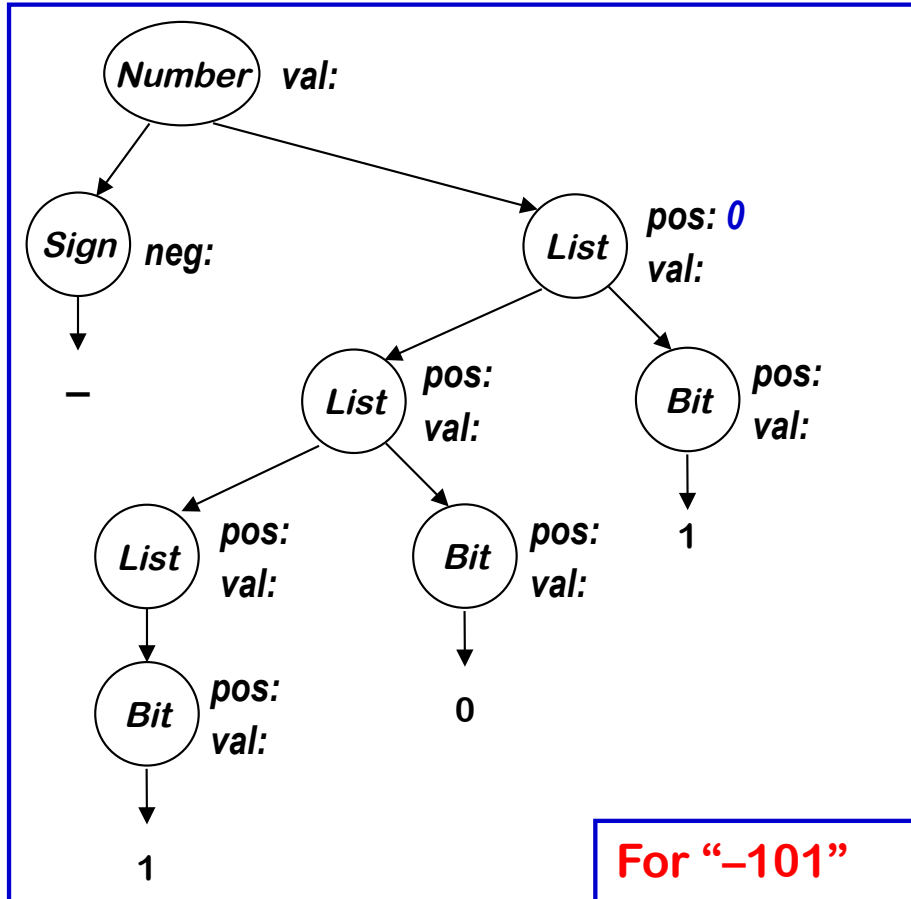
(passes, dataflow)

- Ignore rules & parse tree
- Pick a convenient order (at design time) & use it

Back to the Example

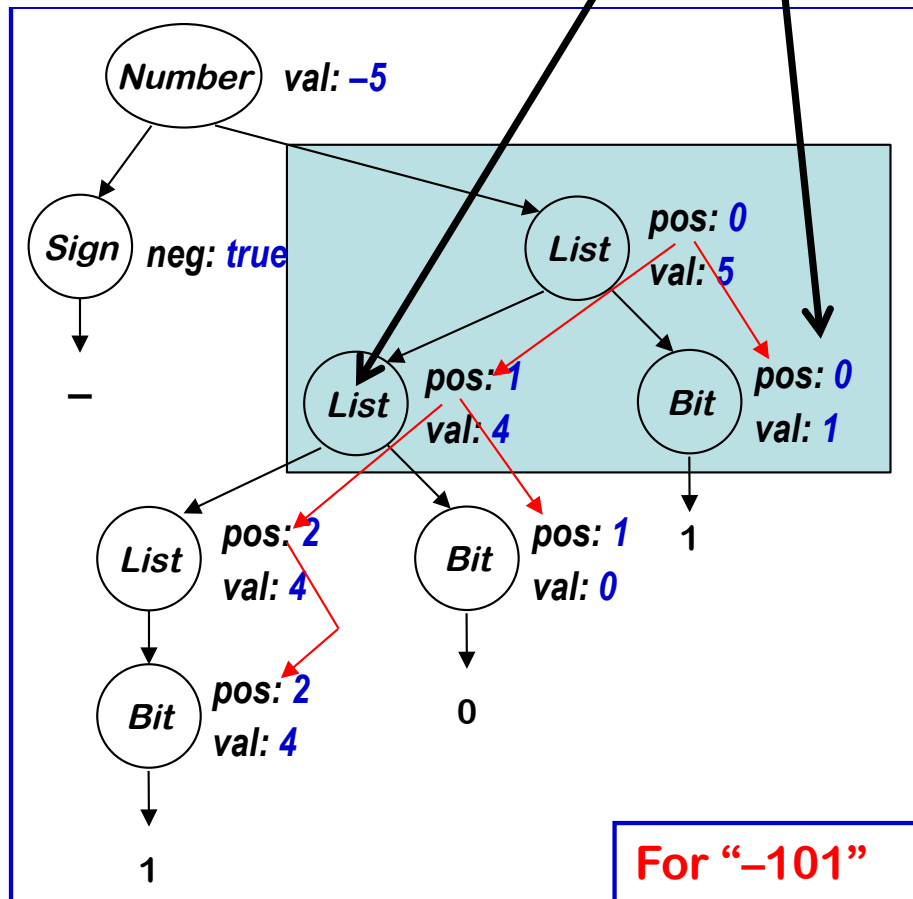


Back to the Example



Back to the Example

$List_0$	\rightarrow	$List_1$ Bit	$List_1.pos \leftarrow List_0.pos + 1$ $Bit.pos \leftarrow List_0.pos$ $List_0.val \leftarrow List_1.val + Bit.val$
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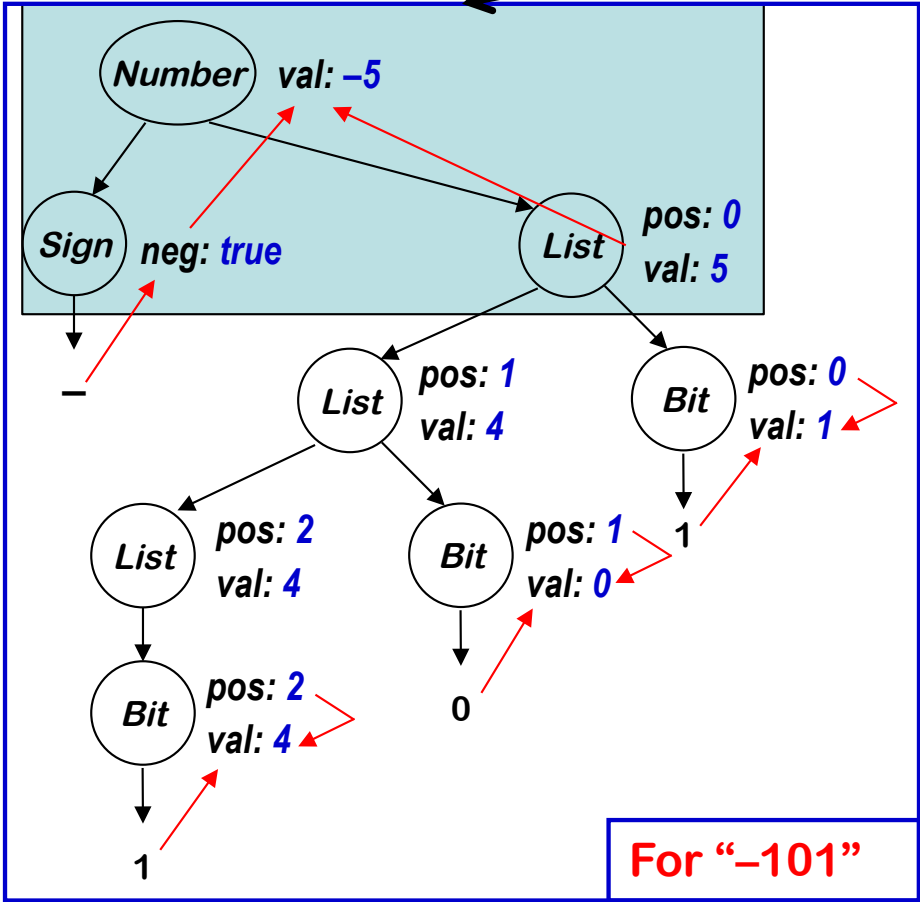


Inherited Attributes

Note: downward flow (pointing arrows) of information

Back to the Example

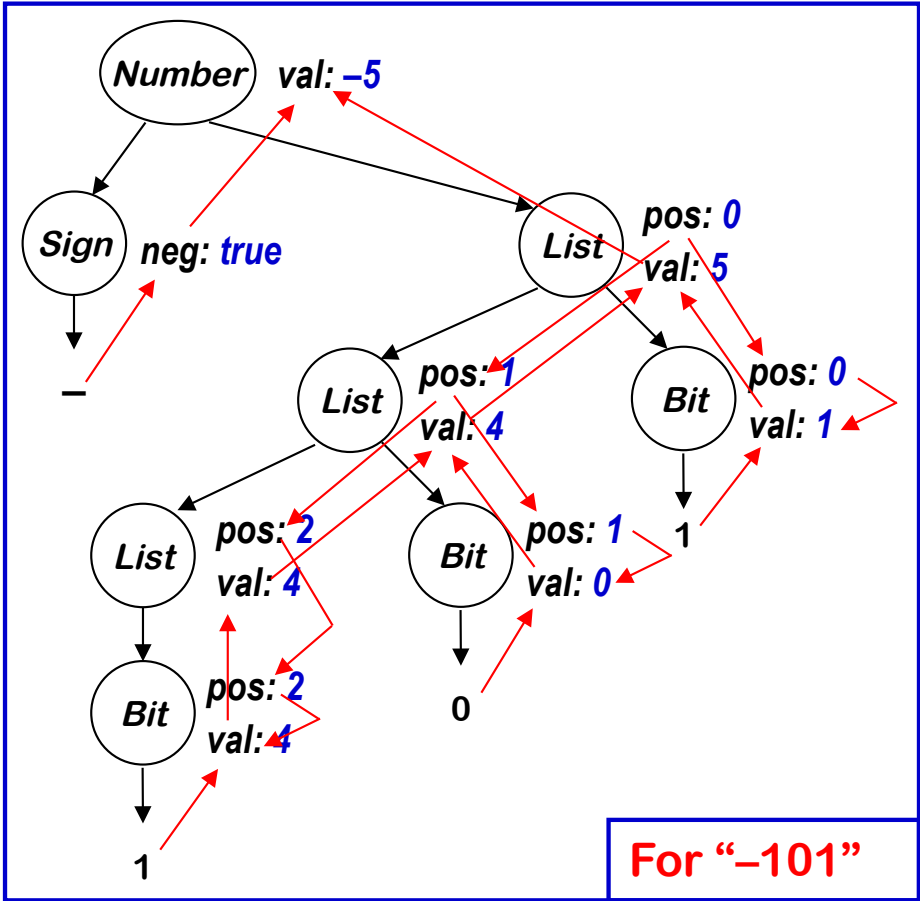
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Synthesized attributes

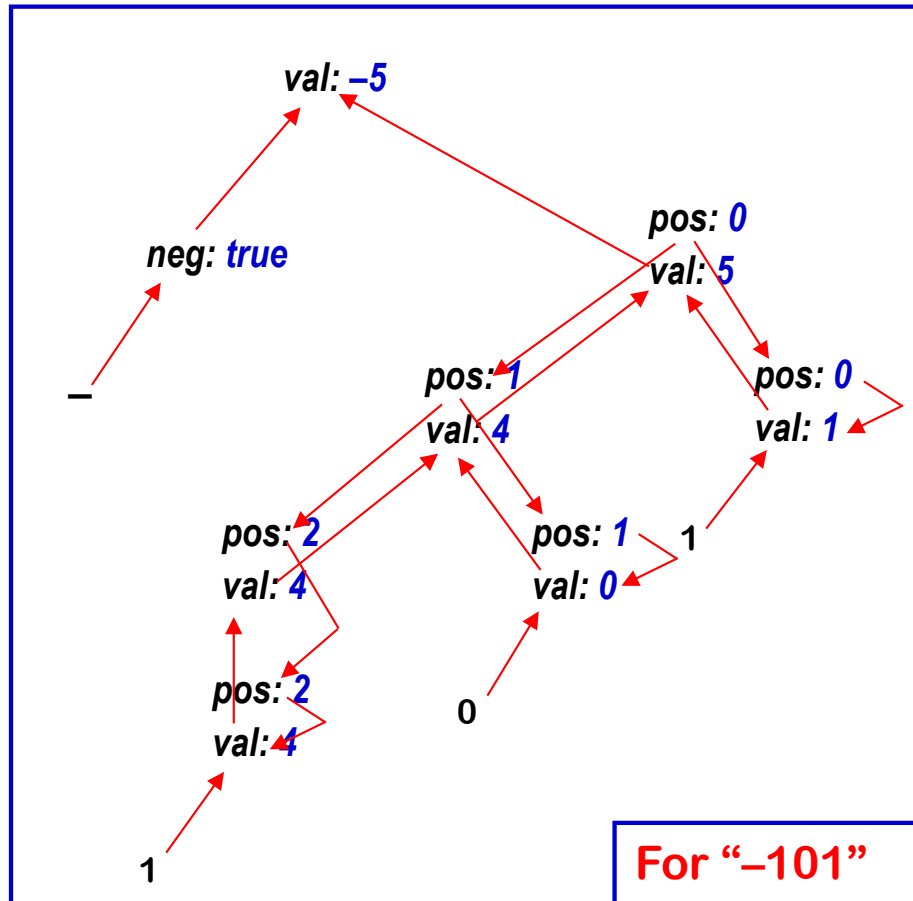
Note: upward flow (pointing arrows) of information and the flow from node's (self) attributes

Back to the Example



If we show the computation ...
then peel away the parse tree ...

Back to the Example



All that is left is the attribute dependence graph. This succinctly represents the flow of values in the problem instance.

The dependence graph **must** be acyclic (no cycles!)



An Extended Example

Grammar for a basic block

$Block_0$	\rightarrow	$Block_1$ Assign
		Assign
Assign	\rightarrow	Ident = Expr ;
Expr ₀	\rightarrow	Expr ₁ + Term
		Expr ₁ - Term
		Term
Term ₀	\rightarrow	Term ₁ * Factor
		Term ₁ / Factor
		Factor
Factor	\rightarrow	(Expr)
		Number
		Identifier

An Extended Example

Grammar for a basic block

$Block_0$	\rightarrow	$Block_1$ Assign
		Assign
$Assign$	\rightarrow	$Ident = Expr ;$
$Expr_0$	\rightarrow	$Expr_1 + Term$
		$Expr_1 - Term$
		$Term$
$Term_0$	\rightarrow	$Term_1 * Factor$
		$Term_1 / Factor$
		$Factor$
$Factor$	\rightarrow	$(Expr)$
		$Number$
		$Identifier$



An Extended Example

Grammar for a basic block

$Block_0$	\rightarrow	$Block_1$ Assign
		Assign
Assign	\rightarrow	Ident = Expr ;
$Expr_0$	\rightarrow	$Expr_1 + Term$
		$Expr_1 - Term$
		Term
$Term_0$	\rightarrow	$Term_1 * Factor$
		$Term_1 / Factor$
		Factor
Factor	\rightarrow	(Expr)
		Number
		Identifier



An Extended Example

Grammar for a basic block

$Block_0$	\rightarrow	$Block_1 Assign$
		$Assign$
$Assign$	\rightarrow	$Ident = Expr ;$
$Expr_0$	\rightarrow	$Expr_1 + Term$
		$Expr_1 - Term$
		$Term$
$Term_0$	\rightarrow	$Term_1 * Factor$
		$Term_1 / Factor$
		$Factor$
$Factor$	\rightarrow	$(Expr)$
		$Number$
		$Identifier$

Example basic block

```
a = -5
b = a * 17
c = b / 2
d = a + b - c
```

How many clock cycles will this block take to execute?



An Extended Example

Grammar for a basic block

$Block_0$	\rightarrow	$Block_1$ $Assign$
		$Assign$
$Assign$	\rightarrow	$Ident = Expr ;$
$Expr_0$	\rightarrow	$Expr_1 + Term$
		$Expr_1 - Term$
		$Term$
$Term_0$	\rightarrow	$Term_1 * Factor$
		$Term_1 / Factor$
		$Factor$
$Factor$	\rightarrow	$(Expr)$
		$Number$
		$Identifier$

Simple *Attribute Grammar*

Estimate cycle count for the block of instructions

- Each operation has a **COST**
- Add them, bottom up
- Assume a load per value
- Assume no reuse



An Extended Example

(continued)

Adding attribution rules **All these attributes are synthesized!**

$Block_0 \rightarrow Block_1 \text{ Assign}$	$Block_0.cost \leftarrow Block_1.cost + Assign.cost$
$\quad \text{ Assign}$	$Block_0.cost \leftarrow Assign.cost$
$Assign \rightarrow Ident = Expr ;$	$Assign.cost \leftarrow COST(store) + Expr.cost$
$Expr_0 \rightarrow Expr_1 + Term$	$Expr_0.cost \leftarrow Expr_1.cost + COST(add) + Term.cost$
$\quad \text{ Expr}_1 - Term$	$Expr_0.cost \leftarrow Expr_1.cost + COST(add) + Term.cost$
$\quad \text{ Term}$	$Expr_0.cost \leftarrow Term.cost$
$Term_0 \rightarrow Term_1 * Factor$	$Term_0.cost \leftarrow Term_1.cost + COST(mult) + Factor.cost$
$\quad \text{ Term}_1 / Factor$	$Term_0.cost \leftarrow Term_1.cost + COST(div) + Factor.cost$
$\quad \text{ Factor}$	$Term_0.cost \leftarrow Factor.cost$
$Factor \rightarrow (Expr)$	$Factor.cost \leftarrow Expr.cost$
$\quad \text{ Number}$	$Factor.cost \leftarrow COST(loadI)$
$\quad \text{ Identifier}$	$Factor.cost \leftarrow COST(load)$



An Extended Example

(continued)

Adding attribution rules **All these attributes are synthesized!**

$Block_0 \rightarrow Block_1 \text{ Assign}$	$Block_0.cost \leftarrow Block_1.cost + Assign.cost$
$Assign$	$Block_0.cost \leftarrow Assign.cost$
$Assign \rightarrow Ident = Expr ;$	$Assign.cost \leftarrow COST(store) + Expr.cost$
$Expr_0 \rightarrow Expr_1 + Term$	$Expr_0.cost \leftarrow Expr_1.cost + COST(add) + Term.cost$
$Expr_1 - Term$	$Expr_0.cost \leftarrow Expr_1.cost + COST(add) + Term.cost$
$Term$	$Expr_0.cost \leftarrow Term.cost$
$Term_0 \rightarrow Term_1 * Factor$	$Term_0.cost \leftarrow Term_1.cost + COST(mult) + Factor.cost$
$Term_1 / Factor$	$Term_0.cost \leftarrow Term_1.cost + COST(div) + Factor.cost$
$Factor$	$Term_0.cost \leftarrow Factor.cost$
$Factor \rightarrow (Expr)$	$Factor.cost \leftarrow Expr.cost$
$Number$	$Factor.cost \leftarrow COST(loadI)$
$Identifier$	$Factor.cost \leftarrow COST(load)$



An Extended Example

(continued)

Adding attribution rules **All these attributes are synthesized!**

$Block_0 \rightarrow Block_1 \text{ Assign}$	$Block_0.cost \leftarrow Block_1.cost + Assign.cost$
$Assign$	$Block_0.cost \leftarrow Assign.cost$
$Assign \rightarrow Ident = Expr ;$	$Assign.cost \leftarrow COST(store) + Expr.cost$
$Expr_0 \rightarrow Expr_1 + Term$	$Expr_0.cost \leftarrow Expr_1.cost + COST(add) + Term.cost$
$Expr_1 - Term$	$Expr_0.cost \leftarrow Expr_1.cost + COST(add) + Term.cost$
$Term$	$Expr_0.cost \leftarrow Term.cost$
$Term_0 \rightarrow Term_1 * Factor$	$Term_0.cost \leftarrow Term_1.cost + COST(mult) + Factor.cost$
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$Identifier$	$Factor.cost \leftarrow COST(load)$



An Extended Example

(continued)

Adding attribution rules **All these attributes are synthesized!**

$Block_0 \rightarrow Block_1 \text{ Assign}$	$Block_0.cost \leftarrow Block_1.cost + Assign.cost$
$\quad \text{ Assign}$	$Block_0.cost \leftarrow Assign.cost$
$Assign \rightarrow Ident = Expr ;$	$Assign.cost \leftarrow COST(store) + Expr.cost$
$Expr_0 \rightarrow Expr_1 + Term$	$Expr_0.cost \leftarrow Expr_1.cost + COST(add) + Term.cost$
$\quad \text{ Expr}_1 - Term$	$Expr_0.cost \leftarrow Expr_1.cost + COST(add) + Term.cost$
$\quad \text{ Term}$	$Expr_0.cost \leftarrow Term.cost$
$Term_0 \rightarrow Term_1 * Factor$	$Term_0.cost \leftarrow Term_1.cost + COST(mult) + Factor.cost$
$\quad \text{ Term}_1 / Factor$	$Term_0.cost \leftarrow Term_1.cost + COST(div) + Factor.cost$
$\quad \text{ Factor}$	$Term_0.cost \leftarrow Factor.cost$
$Factor \rightarrow (Expr)$	$Factor.cost \leftarrow Expr.cost$
$\quad \text{ Number}$	$Factor.cost \leftarrow COST(loadI)$
$\quad \text{ Identifier}$	$Factor.cost \leftarrow COST(load)$



An Extended Example

Properties of the example grammar

- All attributes are synthesized \Rightarrow S-attributed grammar
- Rules can be evaluated bottom-up in a single pass
 - \rightarrow Good fit to bottom-up, shift/reduce parser
- Easily understood solution
- Seems to fit the problem well

What about an improvement? (see backup slides)

- Values are loaded only once per block (not at each use)
- Need to track which values have been already loaded

Backup Slides





A Better Execution Model

Adding load tracking

- Need sets *Before* and *After* for each production
- Must be initialized, updated, and passed around the tree

Factor → (Expr)	Factor.cost ← Expr.cost ; Expr.Before ← Factor.Before ; Factor.After ← Expr.After
Number	Factor.cost ← COST(load _i) ; Factor.After ← Factor.Before
Identifier	If (Identifier.name ∉ Factor.Before) then Factor.cost ← COST(load); Factor.After ← Factor.Before ∪ Identifier.name else Factor.cost ← 0 Factor.After ← Factor.Before

This looks more complex!



A Better Execution Model

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This looks more complex!



A Better Execution Model

- Load tracking adds complexity
- Every production needs rules to copy *Before & After*

A sample production

$\text{Expr}_0 \rightarrow \text{Expr}_1 + \text{Term}$	$\text{Expr}_0.\text{cost} \leftarrow \text{Expr}_1.\text{cost} + \text{COST}(\text{add}) + \text{Term}.\text{cost};$
	$\text{Expr}_1.\text{Before} \leftarrow \text{Expr}_0.\text{Before};$
	$\text{Term}.\text{Before} \leftarrow \text{Expr}_1.\text{After};$
	$\text{Expr}_0.\text{After} \leftarrow \text{Term}.\text{After}$

Lots of work, lots of space, lots of rules to write



An Even Better Model

What about accounting for finite register sets?

- *Before & After* must be of limited size
- Adds complexity to *Factor* → *Identifier*
- Requires more complex initialization

Jump from tracking loads to tracking registers is small

- Copy rules are already in place
- Some local code to perform the allocation